

# Excessive Volatility in Capital Flows: A Pigouvian Taxation Approach

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This paper presents a welfare case for prudential controls on capital flows to emerging markets as a form of Pigouvian taxation that aims to reduce the externalities associated with the deleveraging cycle. We argue that restricting capital inflows during boom times reduces the potential outflows during busts. This mitigates the feedback cycle during such deleveraging episodes, when tightening financial constraints on borrowers and collapsing prices of collateral assets mutually reinforce each other. As a result, macroeconomic volatility is smoothed and welfare is unambiguously increased.

A number of emerging market economies have recently imposed or considered imposing controls on capital inflows in the face of fierce capital flow bonanzas (see e.g. Financial Times, 2009). For example, Brazil imposed a 2% levy on foreign investments in Brazilian stocks and fixed-income securities on Oct. 24, 2009 after experiencing a 36% appreciation of its currency earlier during the year, and Taiwan followed suit with a similar measure in November.<sup>1</sup> However, while policymakers around the world are clearly concerned about the effects of volatility in capital flows, the theoretic welfare case for such intervention has been less clear. The existing literature has studied how capital flow volatility can trigger feedback cycles that work through the depreciation of the real exchange rate. See e.g. Javier Bianchi (2010) and Anton Korinek (2009, 2010). This paper contributes to the debate by providing a theoretic welfare rationale for the taxation of capital flows based on a more general mechanism that involves asset price deflation.

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<sup>1</sup>Capital controls had also been imposed by Chile over the period of 1991-98, amid mixed reviews. See e.g. Francisco Gallego et al. (2002) for a discussion.

## I. Model

We describe a small open economy in a one-good world with three time periods  $t = 0, 1, 2$ . The economy is populated by a continuum of atomistic identical consumers, with a mass normalized to one. The consumer issues debt in period 0 and repays it in periods 1 and 2. In period 1, his ability to roll over debt may be affected by a collateral constraint. Period 2 represents the long term. Optimism about the future may lead to a large volume of debt inflows in period 0, making the economy vulnerable to a sudden stop/credit crunch in period 1.

The utility of the representative consumer is given by

$$u(c_0) + u(c_1) + c_2.$$

The riskless world interest rate is normalized to zero. Thus the first-best level of consumption is the same in periods 0 and 1 and is given by  $c^*$  satisfying  $u'(c^*) = 1$ .

Domestic income involves two components, an endowment  $e$  that is obtained in period 1 and is not pledgeable to foreign creditors, and the return  $y$  on an asset that materializes in period 2 and can be pledged as collateral on loans from foreign investors. (We assume that the asset is not acquired by foreign investors because residents have a strong comparative disadvantage in operating it). Each domestic consumer owns one unit of the asset, and the price of the asset at time  $t$  is denoted by  $p_t$ . For simplicity, we assume that the asset return  $y$  and the endowments are deterministic, except for  $e$ , which is revealed in period 1. Because of a credit constraint, low realizations of  $e$  may trigger countercyclical capital outflows or "sudden stops".<sup>2</sup>

Under these assumptions the budget constraints of

<sup>2</sup>We could also assume that  $y$  is stochastic, leading to a model in which booms and busts in capital flows are driven by the price of domestic assets (see Olivier Jeanne and Anton Korinek, 2009).

a domestic consumer are given by

$$\begin{cases} c_0 = d_1, \\ c_1 + d_1 = e + d_2, \\ c_2 + d_2 = y, \end{cases}$$

where  $d_t$  is the debt to be repaid at the beginning of period  $t$ . The interest rate is equal to zero because there is no default in equilibrium. Each consumer faces a collateral constraint of the form

$$(1) \quad d_2 \leq \theta_1 p_1,$$

where  $\theta_1$  is the quantity of domestic collateral held by the consumer at the beginning of period 1. Domestic consumers can buy or sell the asset in a perfectly competitive domestic market but in a symmetric equilibrium we must have  $\theta_1 = 1$ . The micro-foundation for constraint (1) is that a consumer could walk away and foreign creditors could seize his asset and sell it to other consumers in the domestic market.<sup>3</sup>

## II. Laissez-faire equilibrium

We solve for the equilibrium going backwards.<sup>4</sup> Decentralized agents first solve for the period-1 equilibrium, taking initial liquid net worth  $m_1 = e - d_1$  as given:

$$V_{lf}(m_1) = \max_{d_2} \{u(c_1) + c_2\} \text{ s.t. } d_2 \leq p_1$$

In equilibrium, the period-1 price of the asset is equal to its expected return times the marginal utility of period-2 consumption (1) divided by the marginal utility of period-1 consumption,

$$(2) \quad p_1 = \frac{y}{u'(c_1)}.$$

The first-order condition to the period 1 maximiza-

<sup>3</sup>As we show in Olivier Jeanne and Anton Korinek (2009), the constraint can also involve the end-of-period collateral and be written  $d_2 \leq \phi \theta_2 p_1$  with  $\phi < 1$ . The only thing that matters is that the collateral constraint depend on the current price of the asset,  $p_1$ .

<sup>4</sup>While the main steps of the derivation are reported below, some details have been omitted and can be found in a technical appendix available at [...]

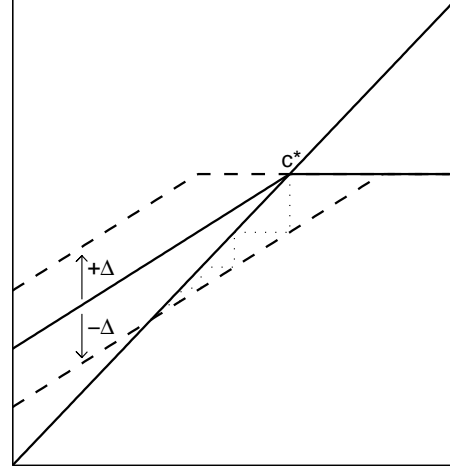


FIGURE 1: DYNAMICS OF FINANCIAL AMPLIFICATION

tion problem is

$$u'(c_1) = 1 + \lambda_{lf}.$$

If the equilibrium is unconstrained, then  $c_1 = c^*$  and  $p_1 = y$ . The equilibrium is indeed unconstrained if and only if the value of collateral is sufficiently high to cover  $d_2 = c^* - e_1 + d_1 \leq y$ , that is, if net worth is higher than a threshold

$$m_1 \geq m^* \equiv c^* - y.$$

If this condition is violated, the equilibrium is constrained and is characterized by

$$(3) \quad c_1 = m_1 + \frac{y}{u'(c_1)}.$$

Both sides of equation (3) are increasing with  $c_1$ . When the constrained value of  $c_1$  reaches  $c^*$ , the equilibrium is unconstrained. In figure 1 we illustrate the resulting equilibrium. Since both lines are upward-sloping in the constrained region, small shocks to liquid net worth can lead to large movements in consumption and asset prices. The dotted zigzag line in the figure illustrates how the economy reacts to a small change in the endowment  $e$  by  $-\Delta$ , as indicated by the downward shift in the dashed line: For the original level of consumption, the borrowing constraint would be violated, hence consumption has to decline. But this reduces the asset price  $p_1 = y/u'(c_1)$  and

therefore tightens the borrowing constraint, leading to a downward spiral of declining consumption and dropping asset prices. This is the the general mechanism behind standard models of financial acceleration or debt deflation. In the unconstrained region, by contrast, a change in endowment by  $+\Delta$  (as illustrated by the upper dashed line) does not affect consumption  $c_1$ .

We restrict our attention to the case where equation (3) is satisfied by at most one  $c_1$  because the derivative of the r.h.s. with respect to  $c_1$  is strictly smaller than 1,

$$(4) \quad y \frac{d(1/u'(c))}{dc} < 1 \quad \forall y, \forall c \leq c^*.$$

If this condition is not satisfied there might be multiple equilibria, in which a fall in the price of the domestic asset is self-fulfilling because it depresses domestic consumption.<sup>5</sup> Equation (3) has a solution  $c_1$  if and only if the debt coming to maturity can be repaid with the available liquid net worth ( $m_1 > 0$ ), and this solution is unique. In reduced form, we can write the period-1 level of consumption and the price of the asset as increasing functions of net worth,  $c(m_1)$  and  $p(m_1)$ .

In the unconstrained regime, capital inflows are decreasing in  $e$  as a higher endowment shock reduces the need of consumers to borrow abroad. Conversely, if the economy is credit-constrained (in the "sudden stop regime"), capital flows become pro-cyclical, i.e., a lower endowment shock  $e$  leads to a lower value of the collateral asset, reduced borrowing from abroad.

In period 0, decentralized agents solve the maximization problem  $\max u(c_0) + E_0 V_{lf}(m_1)$ . Using  $V'_{lf}(m_1) = u'(c_1)$ , this yields the first-order condition

$$(5) \quad u'(c_0) = E_0 [u'(c_1)].$$

The left-hand-side and right-hand-side of this equation are respectively decreasing and increasing in  $d_1$ . The equation uniquely determines the equilibrium level of  $d_1$  under laissez-faire.

### III. Social planner equilibrium

We compare the laissez-faire equilibrium with the allocations chosen by a constrained social planner

<sup>5</sup>In the following we abstract from multiplicity for the sake of simplicity.

who internalizes the asset pricing equation in the economy (2) and realizes that changes in aggregate consumption entail changes in asset prices, which in turn affect the borrowing constraint. In period 1, the social planner chooses the same allocation as under laissez-faire. The social planner sets  $d_1$  in period 0 to maximize expected welfare  $u(c_0) + E_0 V_{sp}(e - d_1)$  where the planner's measure of period-1 welfare is given by

$$V_{sp}(m_1) = \max_{d_2} \{u(c_1) + c_2 + \lambda_{sp} [p(m_1) - d_2]\},$$

where  $p(m_1) = y/u'(c_1)$ , and  $\lambda_{sp}$  denotes the shadow price on the credit constraint for the social planner. The first-order condition with respect to  $d_2$  remains  $u'(c_1) = 1 + \lambda_{sp}$ . The difference with laissez-faire is that the social planner internalizes the endogeneity of the price to the aggregate level of liquid wealth,  $m_1$ , which decentralized agents take as given. By implication the social planner recognizes that the marginal value of liquid wealth in period 1 is

$$V'_{sp}(m_1) = u'(c_1) + \lambda_{sp} \cdot p'(m_1).$$

In the constrained regime, the social marginal value of liquid wealth is larger than its private marginal value because it includes the impact of aggregate wealth on the price of collateral.

The planner's first-order condition with respect to first-period debt  $d_1$  is therefore

$$(6) \quad u'(c_0) = E_0 [u'(c_1) + \lambda_{sp} \cdot p'(m_1)].$$

Whenever there are states in which the borrowing constraint is binding in period 1, both the shadow price  $\lambda_{sp}$  and the derivative  $p'(m_1)$  are positive, and hence the social planner makes the economy consume less and issue less debt in period 0 than under laissez-faire (compare with (5)). This can be interpreted as a macro- (or systemic) precautionary motive: the social planner internalizes the impact of aggregate debt on the probability and severity of a sudden stop.

The optimal level of debt could be implemented in a decentralized way by a tax  $\tau$  on debt inflows that is rebated in lump sum fashion. The first-order condition on  $d_1$  under such a tax  $u'(c_0) = (1 + \tau)E_0[u'(c_1)]$  implies that the optimal tax is given by

$$\tau = \frac{E_0 [\lambda_{sp} \cdot p'(m_1)]}{E_0 [u'(c_1)]}.$$

#### IV. Illustration

We assume that utility is logarithmic ( $u(c) = \log c$ ) and that  $e$  is uniformly distributed over the interval  $[\bar{e} - \varepsilon, \bar{e} + \varepsilon]$ . The logarithmic utility implies  $c^* = 1$ . As shown in the technical appendix, under those assumptions the model can be solved almost entirely in closed form (except for  $d_1$ ). We assume  $m^* = 0.8$  and  $\bar{e} = 1.3$ .

Figure 2 shows how the probability of a sudden stop (under laissez-faire and with the social planner) and the optimal tax  $\tau$  vary with the maximum size of the endowment shock  $\varepsilon$ . For  $\varepsilon < \bar{e} - m^* - 1 = 0.1$ , the economy is never constrained under laissez-faire so that the optimal tax is equal to zero. If  $\varepsilon > 0.1$ , the probability of a sudden stop is positive and increasing in the downside risk—it reaches almost 20 percent for  $\varepsilon = 0.3$  under laissez-faire. Meanwhile the expected consumption gap  $(c^* - c_1)/c^*$  conditional on a sudden stop increases from zero to about 28 percent (not shown on the figure).

The figure illustrates the extent to which the social planner insures the economy against the risk of a sudden stop. For  $\varepsilon \simeq 0.13$ , the probability of sudden stop is reduced from 10 percent under laissez-faire to 6.8 percent by the social planner with a rather moderate tax of  $\tau \simeq 1.3$  percent.<sup>6</sup> The optimal tax increases more than proportionately with the probability of a sudden stop because large sudden stops are costly in terms of domestic welfare. If  $\varepsilon = 0.3$ , the social planner imposes a hefty tax of about 10 percent on debt inflows so as to reduce the probability of a sudden stop from 19 to 12 percent.

#### V. Discussion

*Contingent Liabilities* If other forms of liability are available, the amplification dynamics in the economy are mitigated, and so are the resulting externalities. However, in practice risk markets are often incomplete due to problems such as asymmetric information, and international debt flows are pervasive. Even if decentralized agents have access to ex ante complete insurance markets, there may be reasons why they choose to expose themselves to binding constraints and trigger inefficient financial accelerator

<sup>6</sup>The social planner reduces not only the probability but also the average size of the sudden stops. The expected consumption gap conditional on a sudden stop is lowered from 6.8 percent to 4.6 percent by the tax.

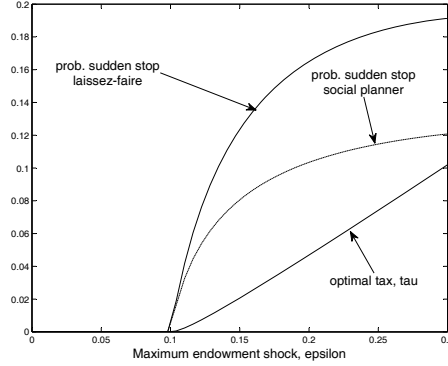


FIGURE 2: PROBABILITY OF SUDDEN STOP AND OPTIMAL TAX

dynamics in some states of nature. This is the case for instance if lenders are risk-averse, as discussed in more detail in Korinek (2009, 2010).

*Bailouts* Our analysis above assumed that the only intervention available to a social planner was the imposition of ex-ante taxes on borrowing. In the real world, another common policy instrument is bailouts that aim to loosen binding constraints by directly transferring resources to constrained agents. In our setup above, a one dollar transfer to constrained agents would relax constraints and trigger positive amplification effects that lead to a total increase in consumption by  $1 + p'(m_1) = 1 + \frac{y}{m^*} = \frac{1}{m^*}$  in the log-utility example.

However, there are two important limitations to bailouts: First, a self-financing bailout, i.e. a bailout that does not involve a permanent resource transfer from outside the economy, is only possible if the planner has either accumulated resources *ex ante* or has a superior capacity *ex post* to collect repayments after the bailout.<sup>7</sup> Secondly, to the extent that bailouts are anticipated, they create significant moral hazard concerns, i.e., they induce decentralized agents to increase their borrowing *ex ante*, making it more likely that constraints will be binding and crises will occur.

<sup>7</sup>In other words, the bailout loan will only be repaid if lending by the planner is not subject to constraint (1).

## VI. Conclusion

This paper presents a simple model of collateralized international borrowing, in which the value of collateral assets endogenously depends on the state of the economy. When financial constraints are binding in such a setup, financial amplification effects (sudden stops) arise as declining collateral values, tightening financial constraints and falling consumption mutually reinforce each other.

Such amplification effects are not internalized by individual borrowers and constitute a negative externality that provides a natural rationale for the Pigouvian taxation of international borrowing. In a sample calibration we found the optimal Pigouvian tax on foreign debt to be 1.3 percent per dollar borrowed for an economy that experiences sudden stops with 10 percent probability. A fuller characterization of the externalities stemming from financial amplification effects in an infinite-horizon DSGE framework as well as the resulting optimal Pigouvian taxes are presented in Jeanne and Korinek (2010).

## REFERENCES

- Bianchi, Javier.** 2010. "Overborrowing and Systemic Externalities in the Business Cycle," Unpublished.
- Financial Times.** 2009. "Worried nations try to cool hot money," *November 19*, 6.
- Galleo, Francisco, Leonardo Hernandez and Klaus Schmidt-Hebbel.** 2002. "Capital Controls in Chile: Were They Effective?" In *Banking, Financial Integration, and Crises*, ed. Leonardo Hernandez and Klaus Schmidt-Hebbel. Santiago: Central Bank of Chile.
- Jeanne, Olivier and Anton Korinek.** 2010. "Managing Credit Booms and Busts: A Pigouvian Taxation Approach," NBER Working Paper.
- Korinek, Anton.** 2009. "Excessive Dollar Borrowing in Emerging Markets: Balance Sheet Effects and Macroeconomic Externalities", Unpublished.
- Korinek, Anton.** 2010. "Regulating Capital Flows to Emerging Markets: An Externality View," Unpublished.