

International Debt Deleveraging

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This draft: November 2013

First draft: November 2012

Abstract

I provide a framework for understanding debt deleveraging in a group of financially integrated countries. During an episode of international deleveraging world consumption demand is depressed and the world interest rate is low, reflecting a high propensity to save. If exchange rates are allowed to float, deleveraging countries can depreciate their nominal exchange rate to increase production and mitigate the fall in consumption associated with debt reduction. The key insight of the paper is that in a monetary union this channel of adjustment is shut off, and therefore the falls in consumption demand and in the world interest rate are amplified. Hence, monetary unions are especially prone to hit the zero lower bound on the nominal interest rate and enter a liquidity trap during deleveraging. In a liquidity trap deleveraging gives rise to a union-wide recession, which is particularly severe in high-debt countries. The model suggests several policy interventions that mitigate the negative impact of deleveraging on output in monetary unions.

JEL Classification Numbers: E31, E44, E52, F32, F34, F41, G01, G15.

Keywords: Global Debt Deleveraging, Liquidity Trap, Monetary Union, Precautionary Savings, Debt Deflation.

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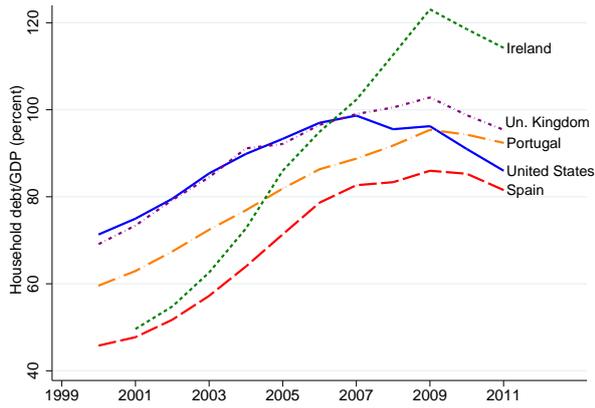
1 Introduction

Episodes of global debt deleveraging are rare, but when they occur they come with deep recessions and destabilize the international monetary system. In the Great Depression of the 1930s the world entered a period of global debt reduction and experienced the most severe recession in modern history. The cornerstone of the international monetary system, the Gold Standard, came under stress and was abandoned in 1936, when the remaining countries belonging to the Gold Block gave up their exchange rate pegs against gold. Almost 80 years later, history seems to be repeating itself. Following the 2007-2008 turmoil in financial markets several advanced economies experienced an abrupt reduction in capital inflows and embarked in a process of private debt deleveraging (figure 1), accompanied by a deep economic downturn, the Great Recession. Once again, the status quo in the international monetary system is challenged, and this time the survival of the Eurozone is called into question. These events might suggest that fixed exchange arrangements, such as monetary unions, are hard to maintain during times of global debt deleveraging, but more research is needed to understand exactly why this chain of events is set in motion during deleveraging episodes.

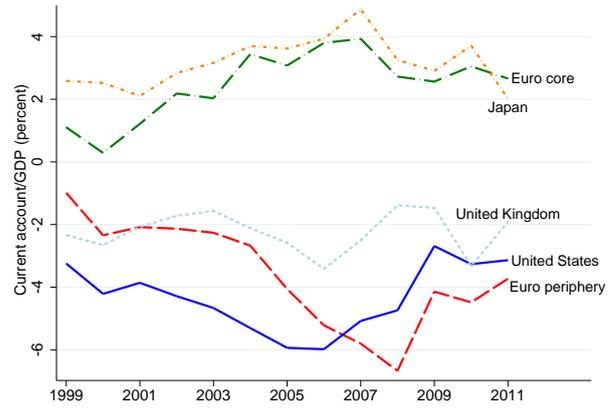
My objective in this paper is to develop a framework for the study of the implications of debt deleveraging among financially integrated countries. During an episode of international deleveraging world demand for consumption is depressed and the world interest rate is low, reflecting a high propensity to save. If exchange rates are allowed to float, deleveraging countries can rely on a depreciation to increase production and mitigate the fall in consumption associated with debt reduction. The key insight of the paper is that in a monetary union this channel of adjustment is shut off, because high-debt countries cannot depreciate against the other countries in the monetary union, and therefore the falls in the demand for consumption and in the interest rate are amplified. Hence, during an episode of deleveraging monetary unions are especially prone to hit the zero lower bound on the nominal interest rate and enter a liquidity trap. In a liquidity trap standard monetary policy tools are ineffective and deleveraging gives rise to a deflationary recession. This effect contributes to explain why episodes of debt deleveraging are particularly painful for monetary unions.

The model features a continuum of small open economies trading with each other. Each economy is inhabited by households which borrow and lend to smooth the impact of temporary, country-specific, productivity shocks on consumption, in the spirit of the Bewley (1977) closed economy model. Foreign borrowing and lending arise endogenously as households use the international credit market to insure against country-specific productivity shocks.

Each household is subject to an exogenous borrowing limit. I study an episode of delever-



(a) Household debt in percent of GDP



(b) Current account in percent of GDP

Figure 1: Motivating facts. Notes: data are from Eurostat and the OECD.

aging triggered by a tightening of the borrowing limit, which I call a *deleveraging shock*. To isolate the role of the exchange rate regime in shaping the response to a deleveraging shock I compare the adjustment under two different versions of the model. I start by considering a model without nominal rigidities. I then analyze the case of a monetary union with nominal wage rigidities.

In both versions of the model, the process of debt reduction generates a fall in the world interest rate, which overshoots its long run value. The drop in the world interest rate is due to two different effects. On the one hand, the most indebted countries are forced to increase savings in order to reduce their debt and satisfy the new borrowing limit. On the other hand, the countries starting with a low stock of debt, as well as those starting with a positive stock of foreign assets, want to increase precautionary savings as a buffer against the risk of hitting the borrowing limit in the future. Both effects lower consumption demand and generate a rise in the propensity to save. As a result, the world interest rate must fall to guarantee that the rest of the world absorbs the forced savings of high-debt borrowing-constrained economies.

In absence of nominal rigidities the deleveraging process also entails a rise in production in high-debt economies. Households can repay their debts not only by cutting consumption, but also by working more to increase their labor income. Thus, households living in high-debt countries increase their labor supply in response to the deleveraging shock. If wages are flexible, the rise in labor supply generates a drop in real wages and a rise in employment and output in high-debt countries.

A large body of evidence, reviewed below, suggests that nominal wages adjust slowly to shocks. In particular nominal wages do not fall much during deep recessions, in spite of sharp rises in unemployment. With nominal wage rigidities I show that nominal exchange

rate flexibility can substitute for nominal wage flexibility.¹ But in a monetary union exchange rates between members are fixed and the adjustment in real wages cannot be achieved through movements in the nominal exchange rate. I focus on this case in the main part of the paper.

The combination of nominal wage rigidities and fixed exchange rates prevents any increase in employment and production in high-debt economies in response to the deleveraging shock. Households living in the high-debt countries of the monetary union have to reduce their debt solely by decreasing consumption. The deep fall in consumption demand coming from high-debt countries amplifies the increase in the propensity to save and the fall in the world interest rate during deleveraging. Because of this effect, the chances that an episode of deleveraging gives rise to a liquidity trap are particularly high for monetary unions.

When the central bank of the monetary union is constrained by the zero lower bound on the nominal interest rate deleveraging gives rise to a deflationary union-wide recession. Because the interest rate cannot fall enough to guarantee market clearing, firms decrease prices in order to eliminate excess supply. Given the sticky nominal wages, the fall in prices translates into a rise in real wages that reduces employment and production. Moreover, if debt is denominated in nominal terms deflation causes a redistribution of wealth from debtor to creditor countries that further reduces consumption demand and production.² The recession hits high-debt countries particularly hard, but the economic downturn also spreads to the countries that are not financially constrained, because the common interest rate and trade linkages tie all the countries of the union together. I show that plausible values of the deleveraging shock hitting part of a monetary union produce quantitatively relevant union-wide recessions. For example, a deleveraging shock that generates a fall in capital inflows toward high-debt countries similar to the one experienced in 2009 by peripheral Eurozone countries produces over two years a cumulated fall in the output of the whole monetary union equal to 11 percent of steady state production.

Finally, I discuss policy interventions that mitigate the recession during deleveraging in monetary unions. First, I show that if the central bank of the monetary union has a higher inflation target the fall in output during deleveraging is smaller. When the nominal interest rate hits the zero bound the real interest rate is equal to the inverse of expected inflation, and so a higher inflation target implies a lower real interest rate, which stimulates consumption demand and production. Second, I consider the impact of a transfer from creditor to debtor countries. Since debtor countries have a higher propensity to consume out of income than creditors, the transfer stimulates aggregate demand and limits the drop in output during deleveraging.

¹In fact, when exchange rates are adjusted optimally the allocations with flexible and rigid wages coincide.

²This is the debt-deflation effect emphasized by Fisher (1933) in the context of the Great Depression.

This paper is related to several strands of the literature. First, the paper is about liquidity traps. Early works studying liquidity traps in micro-founded models, such as Krugman (1998), Eggertsson and Woodford (2003) and Svensson (2003), were motivated by the weak economic performance of Japan during the 1990s, occurring in the context of low inflation and nominal interest rates stuck at zero. The precipitous fall in policy rates experienced by advanced economies during the current crisis has renewed the interest in liquidity traps.³ While traditionally the literature has relied on preference shocks to generate liquidity traps, recently a few contributions have drawn the connection between deleveraging and drops in the interest rate. Guerrieri and Lorenzoni (2011) and Eggertsson and Krugman (2012) study the impact of deleveraging shocks on the interest rate in closed economies, while Benigno and Romei (2012) consider deleveraging in a two-country model. My paper contributes to this literature by demonstrating that monetary unions are more likely to enter a liquidity trap during deleveraging.

A key feature of the model I propose is the presence of nominal wage rigidities. There is extensive evidence in support of the existence of nominal wage rigidities, both at the macro and at the micro level. From a macro perspective, there is evidence that wage contracts are set on average once a year in OECD countries. This observation has been used by Olivei and Tenreyro (2007, 2010) to show empirically that nominal wage rigidities play a key role in transmitting monetary policy shocks to the real economy.⁴ There is also evidence suggesting that nominal wages adjust slowly to changes in prices and unemployment during deep recessions. In their empirical studies, Eichengreen and Sachs (1985) and Bernanke and Carey (1996) find that nominal wage rigidities contributed substantially to the fall in output during the Great Depression, in particular among countries belonging to the Gold Block.⁵ More recently, Schmitt-Grohé and Uribe (2011) have documented the importance of nominal wage rigidities in the context of the 2001 Argentine crisis and of the Great Recession in countries at the Eurozone periphery.⁶ Another strand of the literature shows the relevance of nominal wage rigidities using micro data. For example, Fehr and Goette (2005), Gottschalk (2005) and

³See Robert Hall's presidential address at the 2011 AEA meeting (Hall, 2011). See also Jeanne (2009) and Cook and Devereux (2011), who use a two-country model to study a global liquidity trap.

⁴A similar conclusion is reached by Christiano et al. (2005) using an estimated medium scale DSGE model of the US economy.

⁵The importance of nominal wage rigidities in the US during the Great Depression is discussed in more detail in Bordo et al. (2000).

⁶In addition, several authors, including Shimer (2010), Hall (2011) and Midrigan and Philippon (2011), have emphasized the key role of real wage rigidities in rationalizing the 2008-2009 recession following the turmoil in financial markets. More broadly, Michailat (2012) shows that real wage rigidities are important in explaining unemployment during recessions in the US. In this paper real wage rigidities arise from the combination of nominal wage rigidities and fixed exchange rates.

Barattieri et al. (2010) use worker-level data to show that changes in nominal wages, especially downward, happen infrequently. Fabiani et al. (2010) obtain similar results using firm-level data from several European countries.

The paper also relates to the literature studying precautionary savings in incomplete-market economies with idiosyncratic shocks. The literature includes the seminal works of Bewley (1977), Deaton (1991), Huggett (1993), Aiyagari (1994) and Carroll (1997), who consider closed economies in which consumers borrow and lend to self-insure against idiosyncratic income shocks.⁷ Guerrieri and Lorenzoni (2011) use a Bewley model to study the impact of deleveraging on the interest rate in a closed economy. My paper shares with their work the focus on precautionary savings. Starting from Clarida (1990), some authors have used multi-country models with idiosyncratic shocks and incomplete markets to study international capital flows. Examples are Castro (2005), Bai and Zhang (2010) and Chang et al. (2013). This is the first paper that employs a multi-country Bewley model to study the interactions between deleveraging, the exchange rate regime and liquidity traps.

The current events in the Eurozone have revived the literature on the macroeconomic management of monetary unions. Recent contributions build on the multi-country framework developed by Gali and Monacelli (2008).⁸ Their framework abstracts from financial frictions, a key element in my analysis. Another recent work that relates to the Eurozone crisis is Schmitt-Grohé and Uribe (2011). The authors highlight how the combination of downward nominal wage rigidities in the non-tradable sector and fixed exchange rates can generate involuntary unemployment and recessions in small open economies. Their focus is on a single small open economy that takes the world interest rate as given, while in my paper the endogenous determination of the world interest rate is crucial.

From an empirical perspective, this paper is linked to the work of Lane and Milesi-Ferretti (2012), who look at the adjustment in the current account balances during the Great Recession. They find that the compression in the current account deficits was larger for those countries that were relying more heavily on external financing before the crisis. Moreover, they find that most of the adjustment passed through a compression in domestic demand, contributing to the severity of the crisis in deficit countries. My model rationalizes these facts.⁹

⁷There is also a literature relating precautionary savings and the business cycle. The classic contribution is Krusell and Smith (1998), while recent works are Guerrieri and Lorenzoni (2012) and Challe and Ragot (2012). Rather than focusing on business cycles, this paper considers the response of precautionary savings to a large financial shock.

⁸Examples are Werning and Farhi (2012), who look at the optimal management of fiscal policy in a monetary union, and Farhi et al. (2011), who derive a set of fiscal measures able to substitute for exchange rate flexibility inside a currency union. Instead, Benigno (2004) uses a two-country model to study monetary unions.

⁹The paper is also related to the empirical literature on the rise of precautionary savings during the Great Recession. See Carroll et al. (2012) and Mody et al. (2012).

This paper also speaks to the empirical findings of Mian et al. (2011) and Mian and Sufi (2012). These authors find that the fall in consumption and employment in the US during the 2008-2009 recession was stronger in those counties where the pre-crisis expansion in credit driven by the rise in house prices was more pronounced. This evidence is consistent with the results of my paper, if the monetary union version of the model is interpreted as a large country composed of many different regions. Midrigan and Philippon (2011) also address this evidence using an approach complementary to mine. They look at a cash-in-advance model in which credit can be used as a substitute for fiat money. In their model, the fall in consumption is generated by a decrease in the provision of private credit that tightens households' cash-in-advance constraints, while here the emphasis is on intertemporal debt and liquidity traps. Another empirical work that relates to this paper is Nakamura and Steinsson (2011). Their results on fiscal stimulus across US states lend support to models of monetary unions in which aggregate demand has an impact on production.

The rest of the paper is structured as follows. Section 2 introduces the model and briefly analyzes the steady state. Section 3 considers the adjustment following a deleveraging shock in an economy without nominal rigidities. Section 4 shows that the depressive impact of deleveraging on the interest rate is stronger in a monetary union with nominal wage rigidities. Section 5 describes the role of the zero lower bound in translating a deleveraging episode into a recession. Section 6 introduces a version of the model parameterized at quarterly frequency and performs policy experiments. Section 7 concludes.

2 Model

Consider a world composed of a continuum of measure one of small open economies. Each economy can be thought of as a country.¹⁰ Time is discrete and indexed by t . Each country is populated by a continuum of measure one of identical infinitely lived households and by a large number of firms. All economies produce two consumption goods: a homogeneous tradable good and a non-tradable good. Countries face idiosyncratic shocks in their production technologies, while the world economy has no aggregate uncertainty. Households borrow and lend on the international credit markets in order to smooth the impact of productivity shocks on consumption. There is an exogenous limit on how much each household can borrow. I start by analyzing the steady state of the model, in which the borrowing limit is held constant. The next section studies the transition after an unexpected shock that tightens the borrowing limit.

¹⁰Another possibility is to think of an economy as a region inside a large country, for example a US state or county.

Households. Households derive utility from the consumption of a tradable good C^T and of a non-tradable good C^N and experience disutility from labor effort L . The expected lifetime utility of the representative household in a generic country i is

$$E_0 \left[\sum_{t=0}^{\infty} \beta^t U(C_{i,t}^T, C_{i,t}^N, L_{i,t}) \right]. \quad (1)$$

In this expression, $E_t[\cdot]$ is the expectation operator conditional on information available at time t and β is the subjective discount factor. The period utility function $U(\cdot)$ is assumed to be increasing in the first two arguments, decreasing in the third argument, strictly concave and twice continuously differentiable.

Each household can trade in one period risk-free bonds. Bonds are denominated in units of the tradable consumption good and pay the gross interest rate R_t . The interest rate is common across countries and can be interpreted as the world interest rate.

There are no trade frictions and the price of the tradable good is the same in every country. Normalizing the price of the traded good to 1, the household budget constraint expressed in units of the tradable good is

$$C_{i,t}^T + p_{i,t}^N C_{i,t}^N + \frac{B_{i,t+1}}{R_t} = w_{i,t} L_{i,t} + B_{i,t} + \Pi_{i,t}^T + \Pi_{i,t}^N. \quad (2)$$

The left-hand side of this expression represents the household's expenditure. p_i^N denotes the price of a unit of non-tradable good in terms of the tradable good in country i .¹¹ Hence, the term $C_i^T + p_i^N C_i^N$ is the total expenditure of the household in consumption expressed in units of the tradable good. $B_{i,t+1}$ denotes the purchase of bonds made by the household at time t at price $1/R_t$. If $B_{i,t+1} < 0$ the household is a borrower.

The right-hand side captures the household's income. $w_i L_i$ is the household's labor income. Labor is immobile across countries and hence the wage w_i is country-specific. $B_{i,t}$ is the gross return on investment in bonds made at time $t - 1$. Finally, Π_i^T and Π_i^N are the profits received from firms operating respectively in the tradable and in the non-tradable sector. All domestic firms are wholly owned by domestic households and equity holdings within these firms are evenly divided among them.

There is a limit on how much each household is able to borrow. In particular, debt repay-

¹¹ p_i^N is not necessarily equalized across countries because the non-traded good is, by definition, not traded internationally.

ment cannot exceed the exogenous limit κ , so that the bond position has to satisfy¹²

$$B_{i,t+1} \geq -\kappa. \quad (3)$$

This constraint captures in a simple form a case in which a household cannot credibly commit in period t to repay more than κ units of the tradable good to its creditors in period $t + 1$.¹³

The household's optimization problem is to choose $C_{i,t}^T$, $C_{i,t}^N$, $L_{i,t}$ and $B_{i,t+1}$ to maximize the expected present discounted value of utility (1), subject to the budget constraint (2) and the borrowing limit (3), taking the initial bond holdings $B_{i,0}$ and prices R_t , $p_{i,t}^N$, $w_{i,t}$ as given. The household's first-order conditions can be written as

$$p_{i,t}^N = \frac{U_{C_{i,t}^N}}{U_{C_{i,t}^T}} \quad (4)$$

$$-U_{L_{i,t}} = w_{i,t} U_{C_{i,t}^T} \quad (5)$$

$$\frac{U_{C_{i,t}^T}}{R_t} = \beta E_t \left[U_{C_{i,t+1}^T} \right] + \mu_{i,t} \quad (6)$$

$$B_{i,t+1} \geq -\kappa, \quad \text{with equality if } \mu_{i,t} > 0, \quad (7)$$

where U_x denotes the first derivative of the utility function with respect to x and μ_i is the non-negative Lagrange multiplier associated with the borrowing limit. The optimality condition (4) equates the marginal rate of substitution of the two consumption goods, tradables and non-tradables, to their relative price. Equation (5) is the optimality condition for labor supply. Equation (6) is the Euler equation for bonds. When it binds, the borrowing constraint generates a wedge between the marginal utility from consuming in the present and the marginal utility from consuming next period, given by the shadow price of relaxing the borrowing constraint μ_i . Finally, equation (7) is the complementary slackness condition associated with the borrowing limit.

Firms. Firms rent labor from households and produce both consumption goods, taking prices as given. A typical firm in the tradable sector in country i maximizes profits

$$\Pi_{i,t}^T = Y_{i,t}^T - w_{i,t} L_{i,t}^T,$$

¹²Throughout the analysis I assume that the exogenous borrowing limit κ is tighter than the natural borrowing limit.

¹³In reality tight access to credit may manifest itself through high interest rates, rather than through a quantity restriction on borrowing. In appendix B I show that it is possible to recast the borrowing limit (3) in terms of positive spreads over the world interest rate without changing any of the results.

where Y_i^T is the output of tradable good and L_i^T is the amount of labor employed by the firm. The production function is

$$Y_{i,t}^T = A_{i,t}^T (L_{i,t}^T)^{\alpha_T},$$

where $0 < \alpha_T < 1$.¹⁴ A_i^T is a productivity shock affecting all firms in the tradable sector in country i . This is the source of idiosyncratic uncertainty that gives rise to cross-country financial flows in steady state. Profit maximization implies

$$\alpha_T A_{i,t}^T (L_{i,t}^T)^{\alpha_T - 1} = w_{i,t}.$$

This expression says that at the optimum firms equalize the marginal profit from an increase in labor, the left-hand side of the expression, to the marginal cost, the right-hand side.

Similarly, firms in the non-tradable sector maximize profits

$$\Pi_{i,t}^N = p_{i,t}^N Y_{i,t}^N - w_{i,t} L_{i,t}^N,$$

where Y_i^N is the output of non-tradable good and L_i^N is the amount of labor employed in the non-tradable sector. Labor is perfectly mobile across sectors within a country and hence firms in both sectors pay the same wage w_i . The production function available to firms in the non-tradable sector is

$$Y_{i,t}^N = A^N (L_{i,t}^N)^{\alpha_N},$$

where $0 < \alpha_N < 1$. The term A^N determines the productivity of firms in the non-tradable sector. To reduce the number of state variables and save on computation costs, I assume that A^N is constant and common across all countries.¹⁵ The optimal choice of labor in the non-tradable sector implies

$$p_{i,t}^N \alpha_N A^N (L_{i,t}^N)^{\alpha_N - 1} = w_{i,t}.$$

Just as firms in the tradable sector, at the optimum firms in the non-tradable sector equalize the marginal benefit from increasing employment to its marginal cost.¹⁶

Market clearing. Since households inside a country are identical, we can interpret equilibrium quantities as either household or country specific. For instance, the end-of-period

¹⁴To introduce constant returns-to-scale in production we can assume a production function of the form $Y_{i,t}^T = A_{i,t}^T (L_{i,t}^T)^{\alpha_T} K^{1-\alpha_T}$, where K is a fixed production factor owned by the firm, for example physical or organizational capital. The production function in the main text corresponds to the normalization $K = 1$.

¹⁵Empirically, productivity in the non-tradable sectors is much less volatile than in the tradable sectors. For example, see Stockman and Tesar (1995).

¹⁶Throughout the paper I focus on equilibria in which production always occurs in both sectors. Given the functional forms used in the numerical simulations, it is indeed optimal for firms to always operate in both sectors.

net foreign asset position of country i is equal to the end-of-period holdings of bonds of the representative household divided by the world interest rate¹⁷

$$NFA_{i,t} = \frac{B_{i,t+1}}{R_t}.$$

Market clearing for the non-tradable consumption good requires that in every country consumption is equal to production, that is $C_{i,t}^N = Y_{i,t}^N$. Moreover, equilibrium on the labor market implies that in every country the labor supplied by the households is equal to the labor demanded by firms, $L_{i,t} = L_{i,t}^T + L_{i,t}^N$.

These two market clearing conditions, in conjunction with the budget constraint of the household and the expressions for firms' profits, give the market clearing condition for the tradable consumption good in country i

$$C_{i,t}^T = Y_{i,t}^T + B_{i,t} - \frac{B_{i,t+1}}{R_t}.$$

This expression can be rearranged to obtain the law of motion for the stock of net foreign assets owned by country i , i.e. the current account

$$NFA_{i,t} - NFA_{i,t-1} = CA_{i,t} = Y_{i,t}^T - C_{i,t}^T + B_{i,t} \left(1 - \frac{1}{R_{t-1}}\right),$$

As usual, the current account is given by the sum of net exports, $Y_{i,t}^T - C_{i,t}^T$, and net interest payments on the stock of net foreign assets owned by the country at the start of the period, $B_{i,t}(1 - 1/R_{t-1})$.

Finally, in every period the world consumption of the tradable good has to be equal to the world production, $\int_0^1 C_{i,t}^T di = \int_0^1 Y_{i,t}^T di$. This equilibrium condition implies that bonds are in zero net supply at the world level, $\int_0^1 B_{i,t+1} di = 0$.

2.1 Equilibrium

Given a sequence of prices $\{R_t, w_{i,t}, p_{i,t}^N\}_{t=0}^\infty$, define the optimal decisions of the household as $C^T(B, A^T)$, $C^N(B, A^T)$ and $L(B, A^T)$ and the optimal labor demand decisions as $L^T(A^T)$ and L^N , in a country with bond holdings $B_{it} = B$ and productivity $A_{i,t}^T = A^T$. Notice that these decision rules fully determine the transition for bond holdings.

Define $\Psi_t(B, A^T)$ as the joint distribution of bond holdings and current productivity across countries. The optimal decision rules for bond holdings together with the process for produc-

¹⁷I follow the convention of netting interest payments out of the net foreign asset position.

tivity yield a transition probability for the country-specific states (B, A^T) . This transition probability can be used to compute the next period distribution $\Psi_{t+1}(B, A^T)$, given the current distribution $\Psi_t(B, A^T)$. We can now define an equilibrium.

Definition 1 *An equilibrium is a sequence of prices $\{R_t, w_{i,t}, p_{i,t}^N\}_{t=0}^\infty$, a sequence of policy rules $C^T(B, A^T)$, $C^N(B, A^T)$, $L(B, A^T)$, $L^T(A^T)$, L^N and a sequence of joint distributions for bond holdings and productivity $\Psi_t(B, A^T)$, such that given the initial distribution $\Psi_0(B, A^T)$ in every period t*

- $C^T(B, A^T)$, $C^N(B, A^T)$, $L(B, A^T)$, $L^T(A^T)$, L^N are optimal given $\{R_t, w_{it}, p_{it}^N\}_{t=0}^\infty$
- $\Psi_t(B, A^T)$ is consistent with the decision rules
- Markets for consumption and labor clear in every country i

$$C_{i,t}^N = Y_{i,t}^N$$

$$C_{i,t}^T = Y_{i,t}^T + B_{i,t} - \frac{B_{i,t+1}}{R_t}$$

$$L_{i,t} = L_{i,t}^T + L_{i,t}^N.$$

- The market for bonds clears at the world level

$$\int_0^1 B_{i,t+1} di = 0.$$

2.2 Parameters

The model cannot be solved analytically and I analyze its properties using numerical simulations. I employ a global solution method in order to deal with the nonlinearities involved by a large shock such as the deleveraging shock studied in the next section. Appendix A describes the numerical solution method.

I assume a utility function separable in consumption and labor and a Cobb-Douglas aggregator for consumption

$$U(C^T, C^N, L) = \frac{C^{1-\gamma}}{1-\gamma} - \frac{L^{1+\psi}}{1+\psi}$$

$$C = (C^T)^\omega (C^N)^{1-\omega}.$$

These functional forms are commonly used in the literature on monetary economics.¹⁸

¹⁸See, for example, Galí (2009).

Table 1: Parameters

	Value	Source/Target
Risk aversion	$\gamma = 2$	Standard value
Discount factor	$\beta = 0.9755$	$R = 1.025$
Frisch elasticity of labor supply	$1/\psi = 1$	Kimball and Shapiro (2008)
Labor share in tradable sector	$\alpha_T = 0.65$	Standard value
Labor share in non-tradable sector	$\alpha_N = 0.65$	Standard value
Share of tradables in consumption	$\omega = 0.5$	Stockman and Tesar (1995)
TFP process	$\sigma_{AT} = 0.0194, \rho = 0.84$	Benigno and Thoenissen (2008)
Initial borrowing limit	$\kappa = 0.85$	World debt/GDP = 22%

To illustrate transparently the key mechanisms of the model, I start by considering an economy in which a period corresponds to one year.¹⁹ The risk aversion is set to $\gamma = 2$, a standard value. The discount factor is set to $\beta = 0.9755$ in order to match a real interest rate in the initial steady state of 2.5 percent. This is meant to capture the low interest rate environment characterizing the US and the Euro area in the years preceding the start of the 2007 crisis. The Frisch elasticity of labor supply $1/\psi$ is set equal to 1, in line with evidence by Kimball and Shapiro (2008). The labor share in production in both sectors is set to $\alpha_T = \alpha_N = 0.65$, a value in the range of those commonly used in the literature. The share of tradable goods in consumption is set to $\omega = 0.5$, in accordance with the estimates of Stockman and Tesar (1995).

Productivity in the tradable sector A^T follows a normal AR(1) process $A_{i,t}^T = \rho A_{i,t-1}^T + \epsilon_{i,t}$. This process is approximated with the quadrature procedure of Tauchen and Hussey (1991) using 7 nodes.²⁰ The first order autocorrelation ρ and the standard deviation of the TFP process σ_{AT} are set respectively to 0.84 and to 0.0194, following the estimates of Benigno and Thoenissen (2008).²¹

The existing literature offers little guidance on how to set κ , the borrowing limit in the initial steady state. One of the key variables determined by κ is the stock of gross world debt, that is the sum of the net foreign asset positions of debtor countries.²² I set $\kappa = 0.85$ to match a world gross debt-to-GDP ratio of 22 percent. This target corresponds to the sum of the net external debt positions of the euro area debtor countries in 2008, expressed as a fraction of the euro area GDP.²³ I choose this target because the euro area developed significant imbalances

¹⁹In section 6 I study an economy parameterized at quarterly frequency to illustrate some dynamic effects induced by deleveraging.

²⁰I use the weighting function proposed by Flodén (2008), which delivers a better approximation to high-persistence AR(1) processes than the weighting function originally suggested by Tauchen and Hussey (1991).

²¹These values are in the range of those commonly used in the literature on international risk sharing. See, for example, Corsetti et al. (2008).

²²Given that bonds are in zero net supply at the world level, the stock of gross world debt also corresponds to the sum of the net foreign asset positions of creditor countries.

²³Spain is, by far, the country that had the highest net foreign debt-to-euro area GDP ratio in 2008, equal

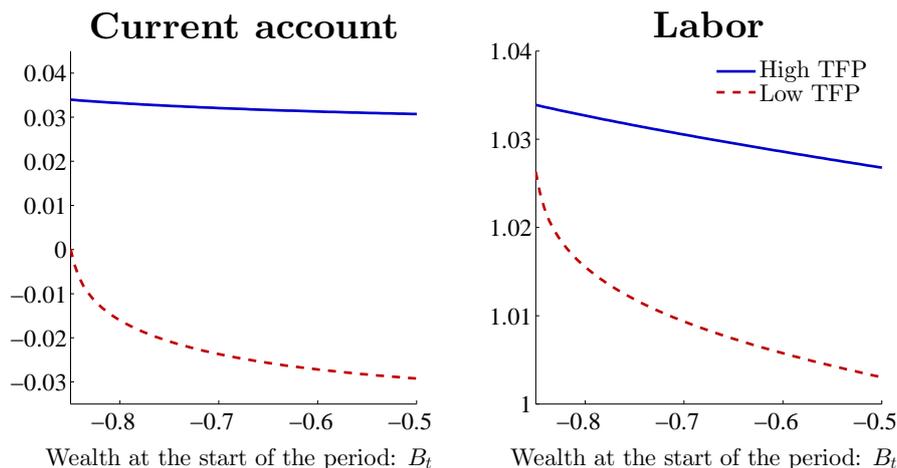


Figure 2: Policy functions in steady state.

across its members in the run-up to the global financial crisis, and because in section 6 I use the sharp contraction in capital inflows experienced in 2009 by euro area debtor countries to calibrate the deleveraging shock.

2.3 Steady state

Before proceeding with the analysis of the deleveraging episode, this section briefly describes the steady state policy functions and the stationary distribution of the net foreign asset-to-GDP ratio.

Figure 2 displays the optimal choices for the current account and labor as a function of B_t , the stock of wealth at the start of the period, for an economy hit by a good productivity shock, solid lines, and by a bad productivity shock, dashed lines.²⁴ The left panel shows the current account. As it is standard in models in which the current account is used to smooth consumption over time, a country runs a current account surplus and accumulates foreign assets when productivity is high, while it runs a current account deficit and reduces its stock of foreign assets when productivity is low.²⁵ Intuitively, fluctuations in productivity generate fluctuations

to 9 percent. Other countries that in 2008 had sizable net foreign debt positions expressed as a fraction of euro area GDP are France, Greece, Ireland, Italy and Portugal. Austria and Finland both had a negative net foreign asset position in 2008, but their external debt was very small compared to euro area GDP. Taking 2007 as the base year would give a very similar target, precisely a world gross debt-to-GDP ratio of 23 percent. Data are from Lane and Milesi-Ferretti (2007).

²⁴Specifically, the high (low) TFP lines refer to economies hit by a productivity shock about two standard deviations above (below) the mean.

²⁵This effect generates a positive steady state correlation between the current account and GDP, while in the data the current account is typically countercyclical. There are several approaches that could correct this counterfactual implication of the model. One possibility would be to introduce endogenous capital accumulation. Modeling capital accumulation would make the framework more realistic, but at the cost of making it much more complicated to solve, and I leave this relevant extension for future work. Another possibility would be to introduce “saving” shocks, for example in the form of shocks to the discount factor β . I explored this

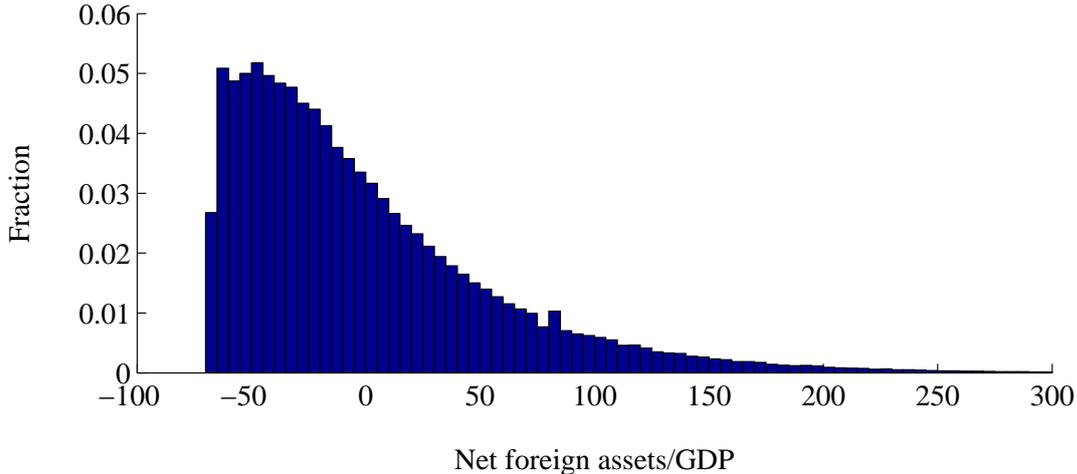


Figure 3: Steady state distribution of net foreign assets/GDP.

in wages and profits, and so in households' income. For instance, when productivity is low also income is low, and households borrow to mitigate the impact of the temporarily low income on consumption, giving rise to a current account deficit. Conversely, when productivity is high income is high, and households save generating a current account surplus. However, the borrowing limit interferes with consumption smoothing because it restricts the amount of new debt that an already indebted household can take in response to a negative income shock. This feature of the economy explains why the deficits in the current account associated with a low realization of the productivity shock decrease as the start-of-period wealth falls.²⁶

The right panel illustrates the optimal choice of labor. In general, equilibrium labor is higher when productivity is high. Intuitively, when productivity is higher firms are able to pay higher wages and this induces households to supply more labor. But as the start-of-period wealth decreases the impact of productivity on equilibrium labor falls, due to the fact that highly indebted households cannot rely extensively on borrowing to smooth the impact of a negative shock on consumption. Instead, highly indebted households mitigate the decrease in consumption due to a negative shock by increasing their labor supply.

Figure 3 shows the steady state distribution of the net foreign asset-to-GDP ratio. The distribution is truncated and skewed toward the left. Both of these features are due to the borrowing limit. In fact, while there is no limit to the positive stock of net foreign assets that a country can accumulate, the borrowing constraint imposes a bound on the negative net foreign asset position that a country can reach. In particular, the largest net foreign debt position-to-

possibility and the introduction of saving shocks does not affect significantly the behavior of the economy during deleveraging. I chose to focus on productivity shocks because they are easier to quantify.

²⁶Indeed, when the borrowing limit is hit households cannot increase their debt further and the change in net foreign assets following a low realization of the productivity shock is equal to zero.

GDP ratio that a country can reach in the initial steady state is close to 70 percent.²⁷

3 Deleveraging without nominal rigidities

This section analyzes the response of the economy to a deleveraging shock, defined as a tightening of the borrowing limit.²⁸ I consider a world economy that starts in steady state with $\kappa = 0.85$, and that in period 0 experiences a large, unexpected and permanent fall in the borrowing limit. For illustrative purposes, in this section I consider a drop in the borrowing limit of 25 percent, so that the new borrowing limit κ' is set to $\kappa' = 0.75\kappa = 0.6375$, taking place in a single period. The drop in the borrowing limit generates a reduction in the steady state world gross debt-to-GDP ratio of about 5 percentage points.

Figure 4 displays the transitional dynamics of the world economy following the deleveraging shock. The figure shows the path for the exogenous borrowing limit and the response of the world gross debt-to-GDP ratio, the world interest rate and the world production of tradable and non-tradable goods.

The tightening of the borrowing limit triggers a decrease in the foreign debt position of highly indebted countries. At the same time, surplus countries are forced to reduce their positive net foreign asset position, which is the counterpart of foreign debt in indebted countries. The result is a progressive compression of the net foreign asset distribution. As showed by the the top-right panel of figure 4, on impact the world debt-to-GDP ratio falls by around 0.5 percent. Afterward, the world slowly transits toward the new steady state debt distribution, in which the world debt-to-GDP ratio is equal to 17 percent.

The world interest rate drops sharply in response to the deleveraging shock and overshoots its value in the new steady state.²⁹ The fall in the interest rate signals an increase in the desire to save, or equivalently a fall in the desire to consume. This is due to two distinct effects. First, countries that start with a high level of foreign debt, more precisely countries that start with a stock of bonds $-\kappa \leq B_{i,0} < -\kappa'$, are forced to reduce their foreign debt position. This forced reduction in debt corresponds to a forced increase in savings that depresses the demand for consumption in high-debt countries. Second, even the countries that are sufficiently wealthy so that they are not directly affected by the tightening of the borrowing limit, the unconstrained

²⁷For comparison, the net foreign debt-to-GDP ratio in Spain in 2008 was 75 percent.

²⁸The model is silent about the causes behind the drop in the borrowing limit. For example, access to credit could be restricted because of a banking crisis. Or alternatively, a drop in house prices, perhaps due to the bursting of a bubble as in Martin and Ventura (2012), could reduce the value of collateral in the hands of households and lead to a reduction in their ability to borrow.

²⁹The interest rate in the final steady state is lower compared to its value in the initial steady state, but quantitatively the difference is minuscule.

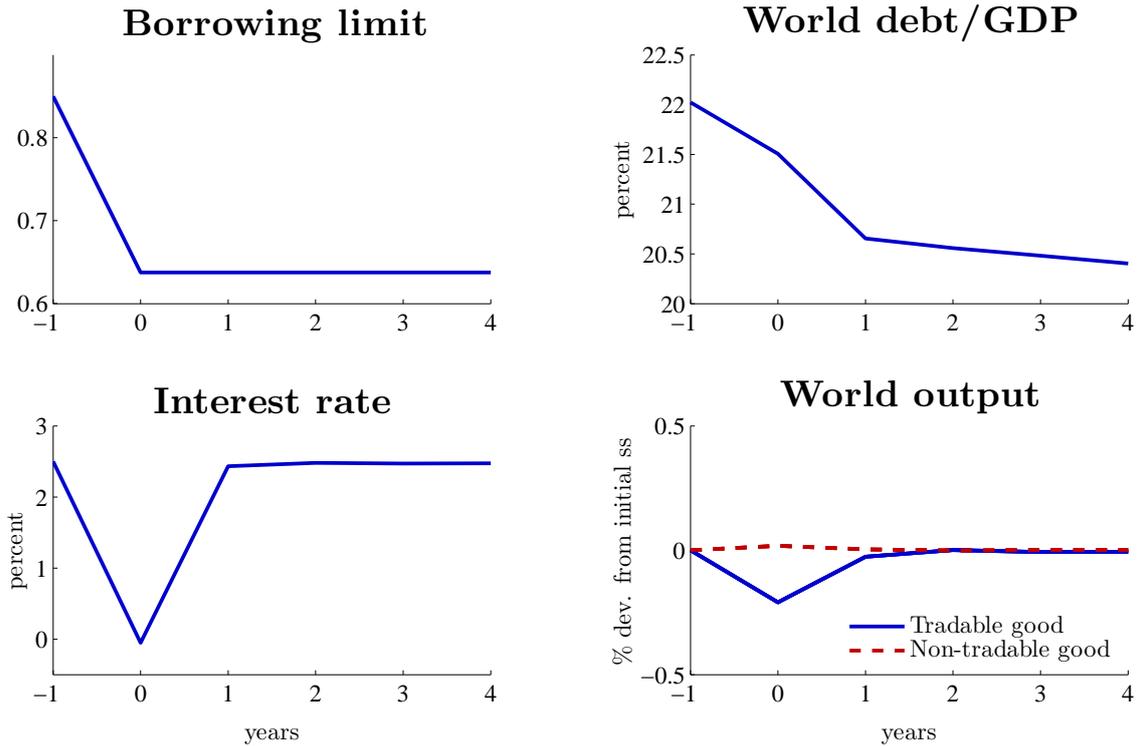


Figure 4: Response to deleveraging shock - flexible wages.

countries, experience an increase in the propensity to save. In fact, unconstrained countries want to accumulate precautionary savings to self-insure against the risk of hitting the now-tighter borrowing limit in the future. Both these effects imply an increase in the propensity to save at the world level.³⁰ In order to reach equilibrium on the bond market the world interest rate has to fall, so as to induce the unconstrained countries to absorb the forced savings coming from high-debt, borrowing-constrained economies.

Concerning output, there is not much action going on at the world level. On impact, the world output of the tradable good decreases by about 0.2 percentage points below its value in the initial steady state, while there is an almost imperceptible rise in the world output of non-tradable goods. However, the lack of aggregate movements in world output masks important country-level composition effects, to which we turn next.

Figure 5 illustrates how the response to the deleveraging shock in period 0 varies across the initial distribution of net foreign assets.³¹ The figure shows the response, that is the change

³⁰Guerrieri and Lorenzoni (2011) describe these two effects in the context of a closed economy. The first effect is also present in Eggertsson and Krugman (2012) and in Benigno and Romei (2012).

³¹To construct this figure, I first computed the response in period 0 to the deleveraging shock for every possible realization of the state variables $\{A_0^T, B_0\}$. Then I computed an aggregate response as a function of B_0 by taking the weighted average of the single country responses. The weights are given by the fraction of countries having a given realization of A_0^T conditional on B_0 .

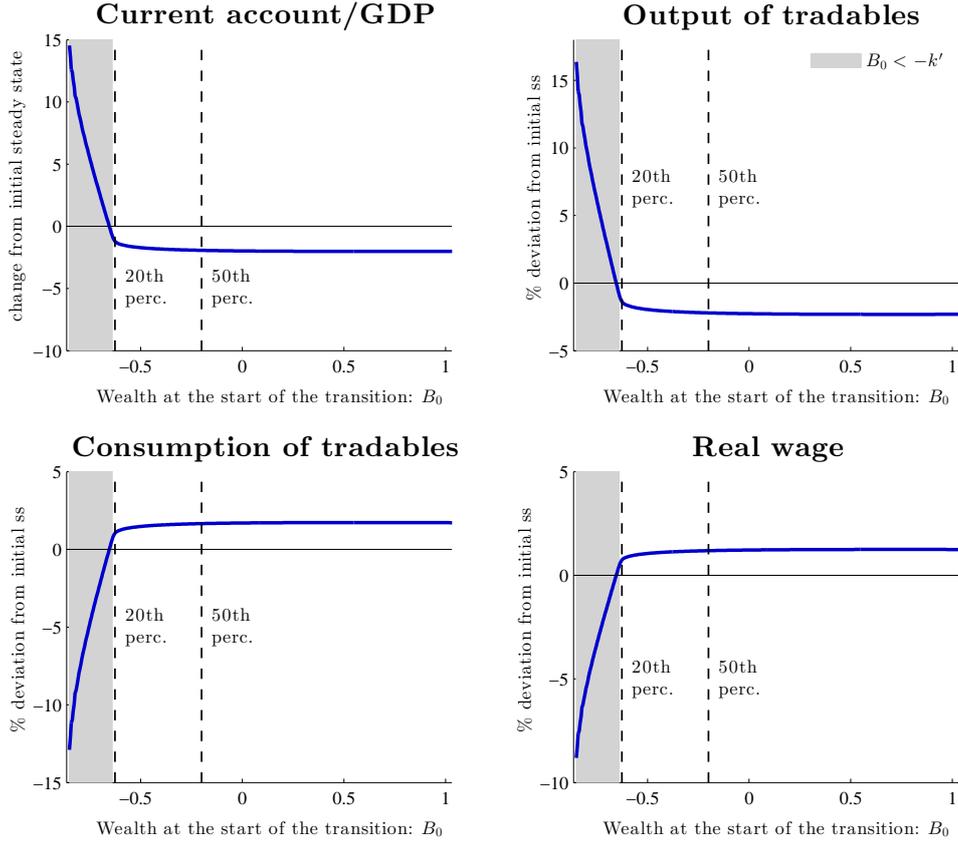


Figure 5: Impact responses to deleveraging shock across the NFA distribution - flexible wages.

with respect to the initial steady state value, of the current account-to-GDP ratio, the output of the traded good, the consumption of the traded good and the real wage, that is the wage expressed in units of tradable good. To ease interpretation the figure also displays the position of the 20th and the 50th percentile of the initial bond distribution.³² The shaded areas denote the countries that start the transition with $B_{i,0} < -\kappa'$ and hence are forced to improve their bond position by the tightening of the borrowing constraint. They represent roughly 20 percent of the countries in the world.

The figure indicates that the sign of the response to the deleveraging shock essentially depends on whether the country is forced to reduce its stock of debt by the tightening of the borrowing limit. This asymmetry in the response to the deleveraging shock is due to the fact that borrowing constrained countries are directly affected by the tightening of the borrowing limit, while the response of the rest of the world is mainly dictated by the behavior of the world interest rate.

The top-left panel of figure 5 shows that the tightening of the borrowing limit forces high-debt countries to improve their foreign asset position by increasing their current account bal-

³²To improve readability, the figure is truncated at the 90th percentile of the bond distribution.

ances, as is typical in countries hit by a sudden stop in capital inflows. To understand the macroeconomic implications, it is useful to go back to the equation describing the current account

$$CA_{i,t} = Y_{i,t}^T - C_{i,t}^T + B_{i,t} \left(1 - \frac{1}{R_{t-1}} \right).$$

This expression makes clear that an economy can improve its current account by increasing its output of the tradable good, by decreasing the consumption of the tradable good or through a combination of both. The top-right and bottom-left panels of figure 5 show that constrained countries adjust both through the output and the consumption margins. Hence, a decrease in capital inflows due to a tightening of the borrowing constraint has an expansionary impact on the production of the traded good in high-debt countries.³³ Later, we will see that the combination of nominal wage rigidities and fixed exchange rates overturns this counterfactual implication of the model.

The countries that are not directly affected by the tightening of the constraint follow an opposite adjustment pattern. The decrease in the world interest rate induces unconstrained countries to reduce their stock of foreign assets by running current account deficits, which are achieved through a combination of lower production of the tradable good and higher consumption.

Hence, following a deleveraging shock the model without nominal rigidities displays a shift of production of tradable goods from wealthy unconstrained countries toward high-debt constrained ones. This change in the pattern of production plays a key role in the adjustment, because it redistributes income from countries which have a low propensity to consume, the unconstrained countries, toward countries that have a high propensity to consume, the borrowing constrained countries. The result is that the asymmetry in the response of production of tradable goods between borrowing constrained and unconstrained countries mitigates the rise in the world propensity to save caused by the deleveraging shock, thus limiting the fall in the world interest rate.

To illustrate this point, I consider a counterfactual “fixed output” economy, in which countries do not adjust their pattern of production in response to the deleveraging shock.³⁴ Figure 6 compares the adjustment to deleveraging for the baseline economy, the solid lines, and the counterfactual economy with no output response, the dashed lines. The figure shows that the world interest rate falls by more in response to the deleveraging shock in the economy with fixed output compared to the baseline economy. Since in the economy with fixed production

³³Chari et al. (2005) provide a detailed discussion of this feature of the frictionless neoclassical model.

³⁴More precisely, in the counterfactual economy the pattern of production during period 0 is the same as in the initial steady state. From period 1 on countries adjust production optimally.

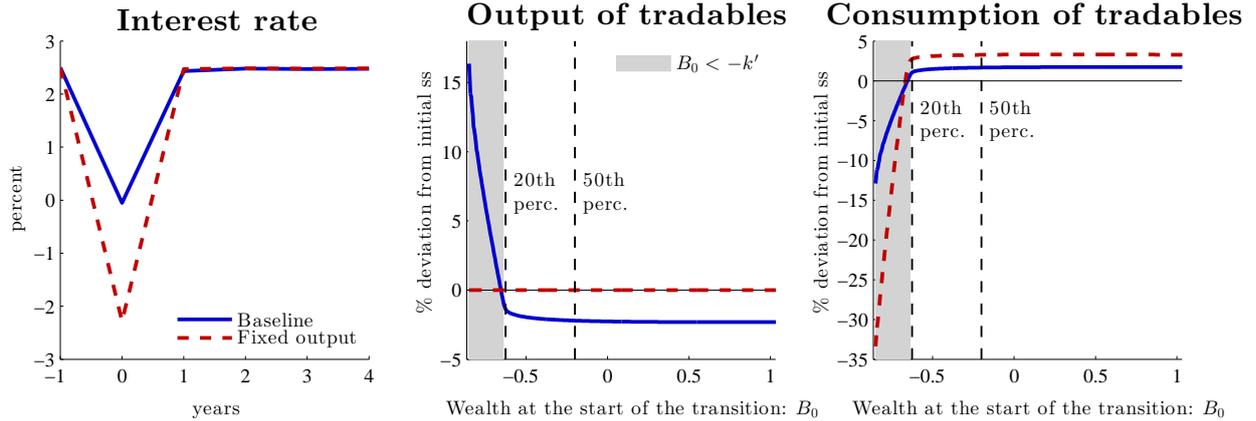


Figure 6: Comparison between baseline economy and fixed output.

all the adjustment takes place through changes in consumption, the interest rate has to fall by more in the fixed output economy to induce unconstrained countries to absorb a larger share of the world's production of the tradable good compared to the baseline economy. This result suggests that frictions that prevent the shift in production of the tradable good from unconstrained to constrained countries amplify the fall in the world interest rate in response to a deleveraging shock.³⁵

The real wage is the key price that has to adjust to allow production to respond to the deleveraging shock. This can be seen by rearranging the optimality condition for firms in the tradable sector to obtain

$$L_{i,t}^T = \left(\frac{\alpha_T A_{i,t}^T}{w_{i,t}} \right)^{\frac{1}{1-\alpha_T}}.$$

This expression implies that, given values for α_T and $A_{i,t}^T$, an increase in employment in the tradable sector in country i has to come with a decrease in the real wage $w_{i,t}$.³⁶ Hence, as shown by the bottom-right panel of figure 5, in the frictionless economy the adjustment to the deleveraging shock entails a decrease in real wages in high-debt constrained economies and an increase in real wages in the rest of the world.

Intuitively, following the deleveraging shock households in high-debt countries increase

³⁵Though in the rest of the paper I discuss the role of the exchange rate regime in facilitating or impeding the adjustment in the pattern of production, this result is by no mean restricted to open economies. In fact, one could imagine a variety of frictions operating in closed economies that might prevent constrained agents from increasing their income and amplify the adjustment in the interest rate.

³⁶More precisely, we can write the elasticity of real wages with respect to employment in the tradable sector as

$$\frac{\partial w_{i,t}}{\partial L_{i,t}^T} \frac{L_{i,t}^T}{w_{i,t}} = \alpha_T - 1.$$

Given that $\alpha_T = 0.65$, a one percent increase in employment in the tradable sector entails a 0.35 percent decrease in the real wage.

their labor supply to boost labor income and to repay debts without cutting consumption too severely. The increase in labor supply translates into a fall in real wages, which represent the cost of labor in terms of the tradable consumption good. In turn, the fall in real wages induces firms in the tradable sector to employ more labor. This is the mechanism through which the deleveraging shock leads to an increase in employment and output in the tradable sector in high-debt economies. Conversely, households in unconstrained countries decrease their labor supply in response to the fall in the interest rate and the subsequent rise in consumption, which leads to a rise in real wages.

The empirical evidence reviewed in the introduction suggests that nominal wages adjust sluggishly to shocks. In particular, a recurrent pattern in severe recessions is that nominal wages do not fall much, even in the face of large rises in unemployment. It is then difficult to imagine that the adjustment in real wages required by the deleveraging shock could come from an adjustment in nominal wages.

In a world in which exchange rates are allowed to float, nominal exchange rate flexibility may substitute for the lack of nominal wage flexibility. The intuition can be gained using a simple partial equilibrium approach. Suppose that there is an international currency in which the tradable good is priced. Let P^T denote the price of the tradable good expressed in units of the international currency. Given the absence of trade frictions, the law of one price holds and the price of the tradable good in terms of the domestic currency is given by

$$P_{i,t}^T = S_{i,t} P_t^T,$$

where $S_{i,t}$ denotes the nominal exchange rate of country i 's against the key currency, i.e. the units of country i currency needed to buy one unit of the key currency.

The real wage, that is the nominal wage divided by the price of the tradable good, is now given by

$$w_{i,t} = \frac{W_{i,t}}{P_{i,t}^T} = \frac{W_{i,t}}{S_{i,t} P_t^T},$$

where $W_{i,t}$ denotes the nominal wage in country i . This expression shows that, given P_t^T and $W_{i,t}$, a reduction in the real wage can come through a nominal exchange rate depreciation against the key currency, that is an increase in S_i . Assuming that P^T does not respond to the deleveraging shock, it follows that to mimic the response to the deleveraging shock under flexible wages, despite the presence of nominal wage rigidities, high-debt borrowing constrained countries should let their nominal exchange rate depreciate against the key currency, while unconstrained countries should let their nominal exchange rate appreciate.

From the point of view of a single country replicating the flexible wage equilibrium through movements in the nominal exchange rate corresponds to the constrained optimal policy.

Proposition 1 *From the perspective of a single country the flexible wage equilibrium corresponds to the constrained efficient allocation.*

Proof. See appendix C. ■

Hence, the results for the economy without nominal rigidities also apply to a world in which nominal wage rigidities are present, but in which countries optimally adjust their exchange rates.

Looking at the current events affecting the Euro area, many commentators have argued that the combination of rigidities in wage setting and fixed exchange rates has contributed to the severity of the crisis in deleveraging countries.³⁷ A point that is often overlooked is that in a financially integrated world all the countries are tied together by the world interest rate, and that the exchange rate regime can have an important role in shaping the behavior of the world interest rate during an episode of global debt deleveraging. The next section introduces a model of a monetary union to illustrate the insights that can be gained from adopting a general equilibrium approach and taking into account the interactions across countries inside a monetary union.

4 Deleveraging in a monetary union

This section focuses on the impact of deleveraging in a monetary union with nominal wage rigidities. To consider the case of a monetary union we have to modify the model introduced in the previous section in a few dimensions. In particular, the model presented in this section explicitly considers nominal, in addition to real, variables.

In a monetary union there is a single currency that is used for transactions in all the participating countries. For simplicity, I consider a world in which every country belongs to the monetary union. From now on I will then use the words monetary union and world interchangeably.

The household's budget constraint in units of currency is

$$P_t^T C_{i,t}^T + P_{i,t}^N C_{i,t}^N + \frac{B_{i,t+1}}{R_i^N} = W_{i,t} L_{i,t} + B_{i,t} + \Pi_{i,t}^T + \Pi_{i,t}^N.$$

In this expression, P^T denotes the price of a unit of tradable consumption good in terms of

³⁷For example, see Feldstein (2010) and Krugman (2010).

currency. Since the tradable good is homogenous and there are no trade frictions, its price is common across all the countries. P_i^N is the nominal price of a unit of non-tradable consumption good, and it is country specific. Realistically, bonds are denominated in units of currency and R^N denotes the gross nominal interest rate. W_i is the nominal wage in country i . Finally, Π_i^T and Π_i^N are now the profits of the firms expressed in nominal terms.

For consistency with the model outlined in the previous section, the borrowing constraint limits the amount of tradable goods that a household can commit to repay during the following period. Formally, for every household the end-of-period bond position has to satisfy

$$\frac{B_{i,t+1}}{P_{t+1}^T} \geq -\kappa.$$

There is a single central bank that uses the nominal interest rate R^N as its policy instrument. The central bank targets inflation in the tradable sector. This policy captures in a simple way the objective of stabilizing prices across all the countries in the union, usually characterizing central banks in monetary unions.³⁸ Moreover, this policy allows for a clean comparison with the flexible wage economy described in the previous sections. In fact, as long as the central bank avoids unexpected movements in the price of the tradable good, nominal bonds and bonds denominated in units of tradables are perfect substitutes.³⁹ To simplify the exposition, in this section I focus on a central bank that targets zero inflation in the traded sector, and hence sets $P_t^T = P_{t-1}^T$ in every period t .

To capture the sluggish adjustment of nominal wages typical of deep recessions, while keeping the intuition underlying the main results of the paper transparent, in this section I consider a very simple form of nominal wage rigidities. I assume that wages are completely rigid

³⁸To be concrete, the European Central Bank targets euro area consumer price inflation. Euro area consumer price inflation is computed using a euro area consumer price index, calculated as an average of the national consumer price indexes for the euro area countries, weighted by the countries relative household consumption expenditure shares in the euro area total. In the model consumer price inflation of the monetary union does not necessarily correspond to inflation in the tradable sector, because of the presence of non-traded goods in the consumption basket. However, quantitatively the differences between consumer price inflation of the monetary union and inflation in the tradable sector are always very small, and in the simulations presented below they never exceed 0.05 percentage points.

³⁹To see this point, consider that the Euler equation for bonds denominated in units of currency is

$$\frac{U_{C_{i,t}^T}}{R_t^N P_t^T} = \beta E_t \left[\frac{1}{P_{t+1}^T} \left(U_{C_{i,t+1}^T} + \mu_{i,t} \right) \right],$$

while the Euler equation for bonds denominated in units of tradables is

$$\frac{U_{C_{i,t}^T}}{R_t} = \beta E_t \left[U_{C_{i,t+1}^T} \right] + \mu_{i,t}.$$

In absence of unexpected movements in the price of the tradable good we can write $R_t = R_t^N P_t^T / P_{t+1}^T$ and verify that the two Euler equations are identical and the two assets are perfect substitutes.

during the first period in which the unexpected shock to the borrowing limit hits the economy, period $t = 0$, while they become fully flexible thereafter.⁴⁰ Once wages are set, workers stand ready to supply the labor demanded by firms. Moreover, I assume that nominal wages in $t = 0$ are set after the uncertainty about the idiosyncratic productivity shocks is resolved, but before the shock to the borrowing limit hits the economy. These assumptions about wage setting isolate the novel contribution of the paper, which concerns the role of wage rigidities and of the exchange rate regime in shaping the adjustment to a deleveraging shock, abstracting from the well understood impact of wage rigidities and exchange rate policy on normal business cycle fluctuations, captured by the idiosyncratic productivity shocks.⁴¹

More precisely, the timing during period 0 is the following:

1. At the start of the period countries are hit by the idiosyncratic productivity shocks.
2. Nominal wages are set so that the pattern of production characterizing the flexible wage equilibrium is replicated as long as the central bank implements the inflation target, that is if $P_0^T = E_{-1} [P_0^T]$.
3. The shock to the borrowing limit is revealed to agents.

Afterward, in periods $t > 0$, wages become again fully flexible.

To understand the implications of this form of nominal wage rigidities, denote by $\hat{L}_{i,0}^T$ the notional equilibrium labor in the traded sector that would prevail in country i and period 0 in the absence of the shock to the borrowing limit, that is in the initial steady state. Wages are then set according to

$$W_{i,0} = \alpha_T A_{i,0}^T E_{-1} [P_0^T] \left(\hat{L}_{i,0}^T \right)^{\alpha_T - 1}.$$

Once wages are set, equilibrium labor is determined by firms' labor demand. Combining the expression for wages and firms' labor demand gives

$$L_{i,0}^T = \left(\frac{P_0^T}{E_{-1} [P_0^T]} \right)^{\frac{1}{1-\alpha_T}} \hat{L}_{i,0}^T.$$

Hence, the assumptions about wage setting imply that on impact the shock to the borrowing limit affects equilibrium labor in the tradable sector only if it induces unexpected movements in the nominal price of the traded good.

Figure 7 shows how the monetary union with nominal wage rigidities responds to a tightening of the borrowing limit. As in the previous section, in period $t = 0$ the union is subject to

⁴⁰Section 6 introduces a model in which wage rigidities last longer than a single period.

⁴¹There is a vast theoretical literature studying the role of exchange rate policy in stabilizing normal business cycle fluctuations. Two excellent recent surveys are Corsetti et al. (2010) and Engel (2013).

an unexpected permanent drop in the borrowing limit, such that the final borrowing limit is equal to 75 percent of the initial one. This shock triggers a process of deleveraging that leads to a progressive reduction in the world debt-to-GDP ratio, as shown by the top-right panel of figure 7.

The bottom-left panel of the figure shows the response of the interest rate.⁴² For ease of comparison, the figure shows both the path of the interest rate in the monetary union, the solid line, and in the economy with optimal exchange rate policy, the dashed line. In both cases deleveraging triggers a fall in the world interest rate. However, quantitatively the fall in the interest rate is much larger in the monetary union. In fact, when the exchange rate is adjusted optimally the interest rate falls on impact by around 2.5 percentage points. Instead, in a monetary union with nominal wage rigidities the fall in the interest rate is two times larger, since it goes from 2.5 percent to around -3 percent. Hence, in a monetary union the combination of nominal wage rigidities and fixed exchange rates amplifies the fall in the interest rate following a deleveraging shock.⁴³

To gain intuition about this effect, it is useful to look at the behavior of high-debt borrowing-constrained countries. Figure 8 displays the impact responses of the current account-to-GDP ratio, the output and consumption of the traded good and the output of the non-traded good across the initial distribution of net foreign assets. As it was the case under the optimal exchange rate policy, high-debt countries are forced to improve their current account by the tightening of the constraint. However, in a monetary union with nominal wage rigidities improving the current account through an increase in the production of the traded good is no longer an option. In fact, given that nominal wages are fixed, this would require a nominal exchange rate depreciation, which is ruled out by the participation in the monetary union. This is illustrated by the top-right panel of figure 8, which shows that the combination of nominal wage rigidities and fixed exchange rates shuts down the response of the output of tradable goods to the deleveraging shock.⁴⁴

Hence, the monetary union exhibits an adjustment pattern similar to the one of the “fixed

⁴²Notice that, since inflation in the tradable sector is zero, the interest rate displayed in figure 7 can be interpreted both as the nominal rate or as the real rate, defined as the nominal rate deflated by inflation in the tradable sector.

⁴³One might wonder how the world responds to a deleveraging shock when exchange rates are flexible, but not adjusted optimally. In appendix *D I* study an economy in which exchange rates are flexible and central banks target consumer price inflation. This monetary policy captures the floating cum inflation targeting regimes that have become increasingly popular since the early 1990s. To summarize the results, the response to the deleveraging shock under floating cum inflation targeting is qualitatively similar to the one under the optimal exchange rate policy. Moreover, the fall in the world interest rate caused by the deleveraging shock is milder under the floating cum inflation targeting regime compared to the monetary union.

⁴⁴Precisely, this happens because the central bank hits the inflation target, so $P_0^T = E_{-1} [P_0^T]$ and the pattern of production during period $t = 0$ is the same as the one in the initial steady state.

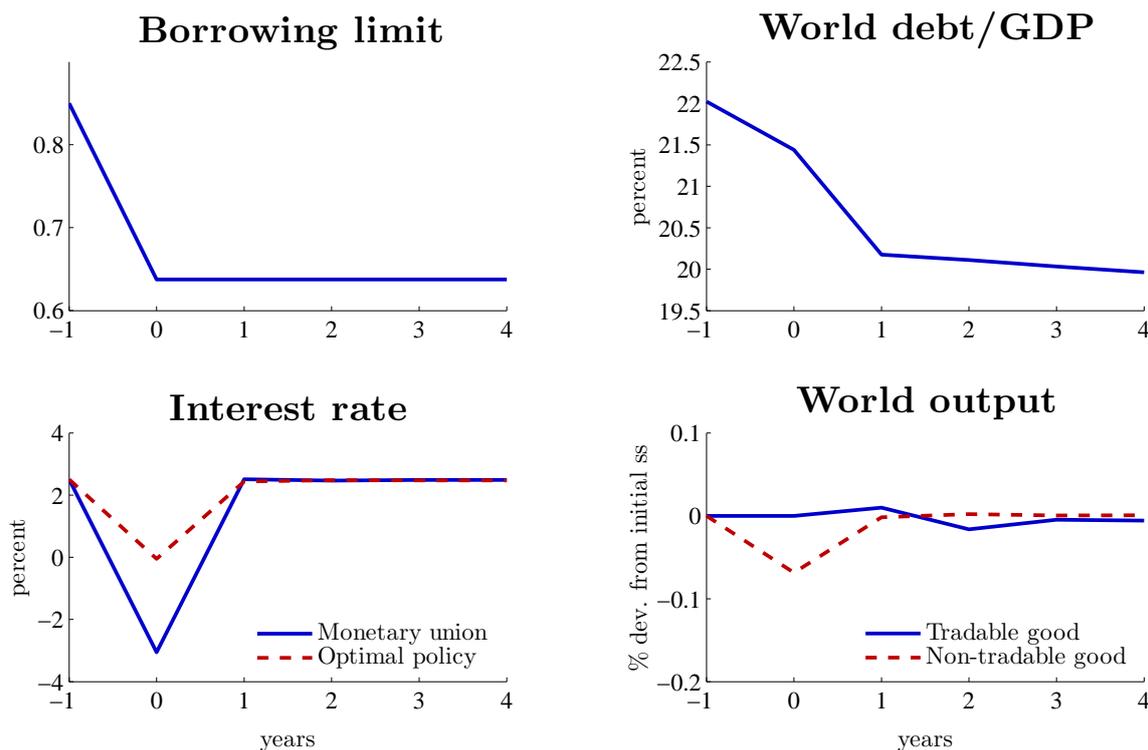


Figure 7: Response to deleveraging shock - monetary union with nominal wage rigidities. Note: Since inflation in the tradable sector is zero, the interest rate can be interpreted both as the nominal rate or as the real rate, defined as the nominal rate deflated by inflation in the tradable sector.

output” economy considered in section 3. In particular, the improvement in the current account in high-debt countries comes solely through a cut in the consumption of the tradable good, as displayed by the bottom-left panel of figure 8. The fact that constrained countries have to adjust exclusively through a cut in consumption implies a bigger fall in the demand for consumption compared to the economy with optimal exchange rate policy. In turn, the interest rate has to fall by more to induce unconstrained countries to increase consumption and pick up the slack left by borrowing constrained economies. Hence, the chances that a deleveraging shock pushes the world into a liquidity trap, that is a situation in which the nominal interest rate hits the zero lower bound, are higher if countries are part of a monetary union.

Moreover, while the deleveraging shock had an expansionary effect on output in high-debt countries in the absence of nominal rigidities, this is no longer the case when wages are rigid and the nominal exchange rates cannot adjust. Indeed, on impact the deleveraging shock generates a drop in the production of non-traded goods in high-debt countries, as highlighted by the bottom-right panel of figure 8. To understand this result, consider that labor demand from

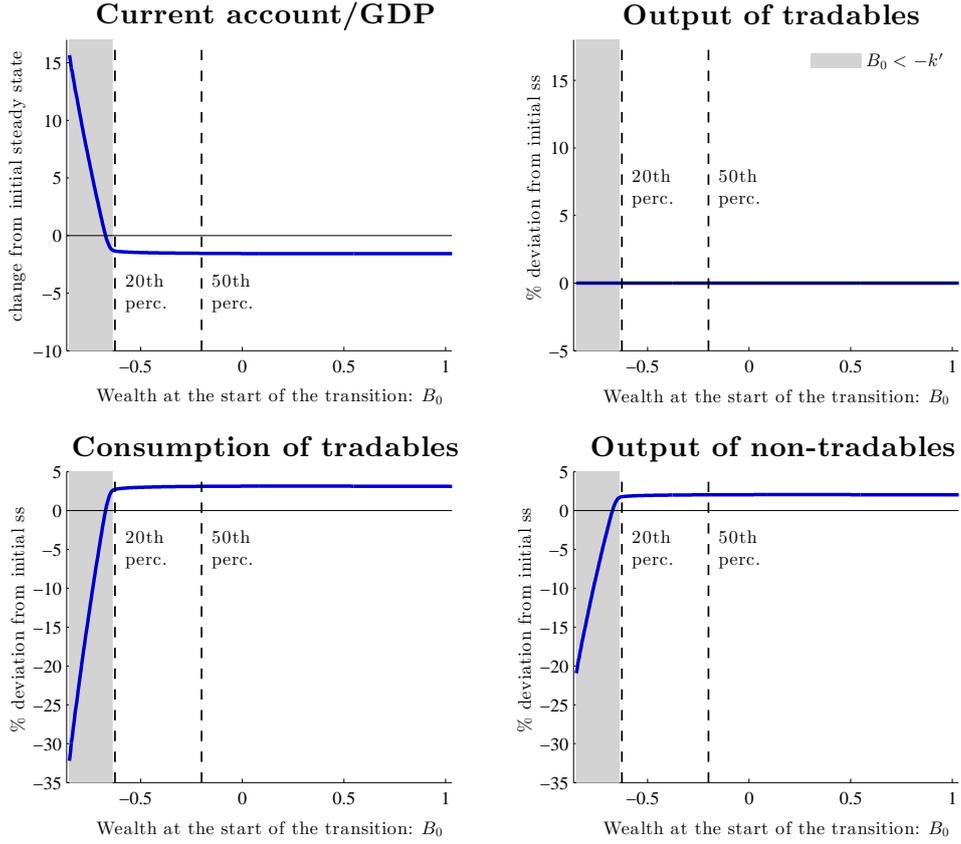


Figure 8: Impact responses to deleveraging shock across the NFA distribution - monetary union with nominal wage rigidities.

firms in the non-traded sector is given by

$$L_{i,t}^N = \left(\alpha_N A^N \frac{P_{i,t}^N}{W_{i,t}} \right)^{\frac{1}{1-\alpha_N}},$$

while households' optimality conditions give an expression for the nominal price of the non-tradable good

$$P_{i,t}^N = \frac{1 - \omega}{\omega} \frac{C_{i,t}^T}{C_{i,t}^N} P_t^T. \quad (8)$$

The drop in the consumption of the traded good experienced by high-debt countries generates a real exchange rate depreciation, that is a fall in the relative price of non-tradables. Since the central bank strictly targets inflation in the traded sector and nominal exchange rates are fixed, the real exchange rate depreciation translates into a fall in the nominal price of the non-tradable good. Given the fixed nominal wages, this implies that employing labor in the non-traded sector becomes less profitable and firms in the non-traded sector of high-debt countries reduce employment and production.

The interaction between nominal wage rigidities and fixed exchange rates generates a recession in the countries that end up being financially constrained following the deleveraging shock. The next section shows how the recession can spread to unconstrained countries if the deleveraging shock pushes the union into a liquidity trap.

5 The role of the zero lower bound

The previous section considered a central bank freely able to set the nominal interest rate in order to hit the inflation target. In reality, nominal interest rates cannot fall below zero. This section considers explicitly the role of the zero lower bound on the nominal interest rate and shows that deleveraging can generate a union-wide recession if the zero lower bound on the interest rate becomes binding.

Define \hat{R}_t^N as the nominal interest rate consistent with the central bank's inflation target. In this section the focus is on a central bank that sets the interest rate according to $R_t^N = \max(\hat{R}_t^N, 1)$. This rule implies that the central bank implements the inflation target as long as this does not imply a negative nominal rate, otherwise it sets the nominal interest rate to zero.⁴⁵

From the analysis in the previous section we know that in $t = 0$, the first period in which the borrowing limit gets tighter, the nominal interest rate consistent with zero inflation in the price of the tradable good is negative. Hence, the central bank sets $R_0^N = 1$. However, at this interest rate the market for consumption of the traded good does not clear, since demand for consumption is too weak to absorb the whole production of tradables. Excess supply induces firms to cut the nominal price of the traded good until equilibrium on the traded good market is restored. We then have that the unexpected deleveraging shock triggers an unexpected fall in the nominal price of the traded good, so that $P_0^T < E_{-1}[P_0^T]$.

The unexpected fall in the nominal price of the traded good has two distinct effects. On the one hand, the fall in the price of the traded good reduces the profitability of employing labor in the traded sector, leading to a fall in the world production of tradables. Indeed, this is the mechanism through which deflation in the traded sector restores equality between demand and supply of the traded good.

On the other hand, since bonds are denominated in units of currency, the unexpected fall in the nominal price of the traded good increases the debt burden of debtor countries in terms of the tradable consumption good, giving rise to an effect akin to Fisher's debt deflation. The

⁴⁵Remember that R^N denotes the gross nominal interest rate.

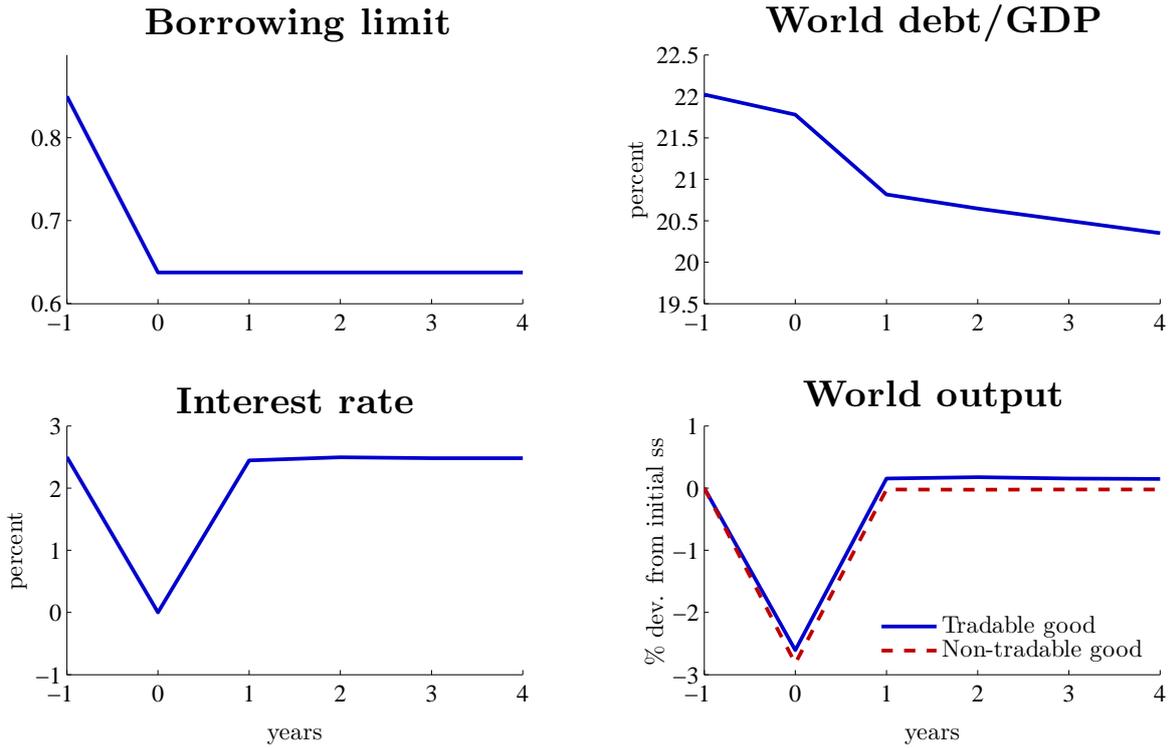


Figure 9: Response to deleveraging shock - liquidity trap in a monetary union.

wealth redistribution from debtor to creditor countries further depresses aggregate demand inside the monetary union. The result is that once the zero lower bound on the nominal interest rate is taken into account, deleveraging in part of the monetary union can push the whole union into a recession.

Figure 9 displays the response of the union to the deleveraging shock in the case in which the central bank is constrained by the zero bound on the interest rate. The tightening of the borrowing limit has a depressive effect on the interest rate, which on impact hits the zero lower bound. Firms respond to the excess supply of tradable consumption good by cutting prices, generating a fall in the nominal price of the tradable good. In turn, the combination of nominal wage rigidities and deflation reduces the profitability of employing labor in the tradable sector. There is thus a union-wide drop in the output of traded goods, which falls by almost 3 percentage points below its value in the initial steady state. Moreover, deflation in the price of the tradable sector puts downward pressure on the nominal prices of the non-traded goods, as shown by equation (8). Deflation in the price of the non-traded good pushes firms in the non-traded sector to cut employment and production. Because of this effect also the aggregate production of non-traded goods falls.

To see how the recession affects differently the countries depending on their initial debt

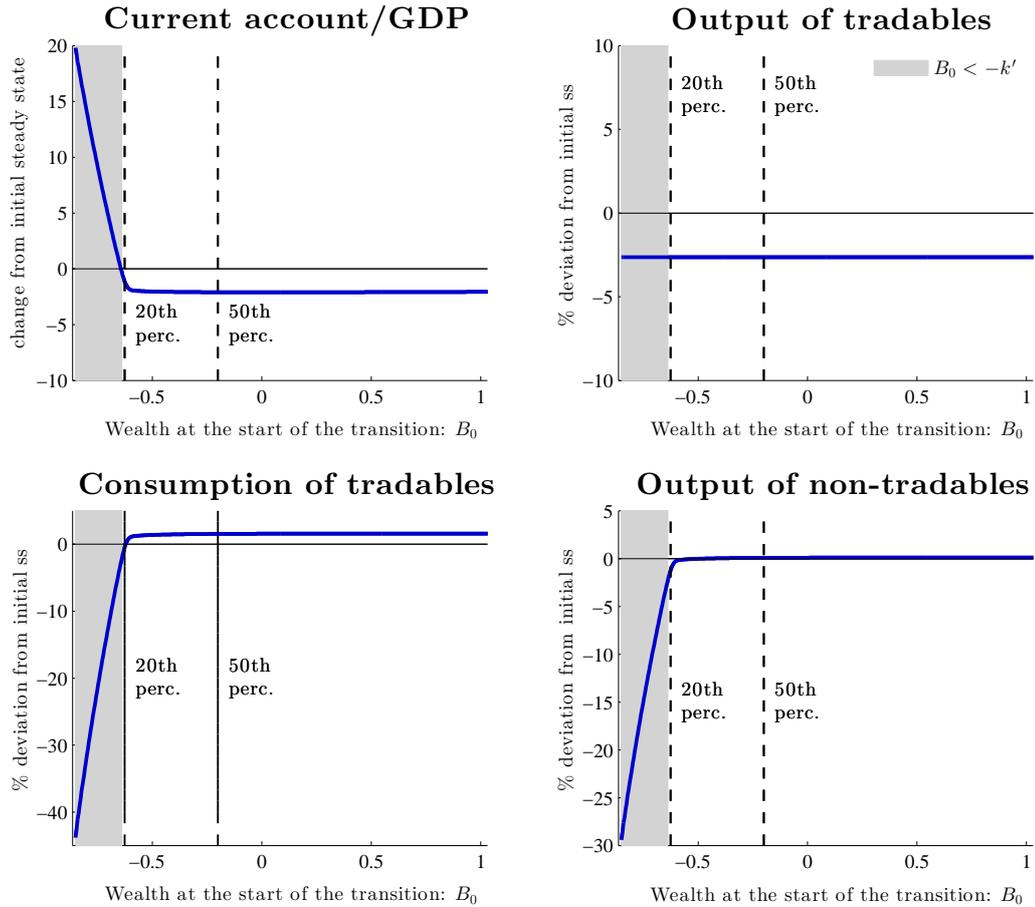


Figure 10: Impact responses to deleveraging shock across the NFA distribution - liquidity trap in a monetary union.

positions, it is useful to look at figure 10. Both high-debt and low-debt countries experience the same fall in the output of the tradable good, because production of the traded good depends on the demand from all the countries in the union.

The consumption of the traded good exhibits a different pattern. In fact, the countries featuring a high initial debt experience deep falls in the consumption of the traded good, much larger than the one experienced in the absence of the zero lower bound. The large drop in consumption is explained by the fact that constrained countries have a high propensity to consume out of current income. Hence, the fall in the production of tradables directly translates into a fall in consumption. In addition, deflation increases the initial debt position of debtor countries, the Fisher's debt deflation effect, further depressing their consumption of tradable goods.

Concerning the production of non-tradables, figure 10 shows that high-debt countries exhibit deep falls in employment and output in the non-traded sector. As before, the drop in production of non-tradable goods in high debt countries happens because the fall in the con-

sumption of the traded good generates a real exchange rate depreciation. Since the nominal exchange rate cannot adjust, the real depreciation results in a fall in the nominal price of non-tradables. Given the fixed wages, deflation in the non-traded sector induces a fall in employment. The result is that the whole monetary union enters a recession, but the recession is particularly severe in the non-traded sectors in high-debt countries.

6 Dynamic deleveraging

This section considers a version of the model parameterized at quarterly frequency in which the adjustment to the deleveraging shock lasts more than one period and dynamic effects take the center stage. Indeed, whenever a liquidity trap lasts more than one period dynamic amplification effects are set in motion, so a quarterly parameterization is better suited to capture the quantitative implications of the model and to perform policy analysis. To be clear, the objective of this section is not to reproduce a specific event, but rather to show that the effects captured by the model are quantitatively relevant for reasonable calibrations of the deleveraging shock.

As a first step, I introduce a dynamic process of wage adjustment in which nominal rigidities last more than a single period. As in the previous section, I assume that in the first period in which the borrowing limit gets tighter, $t = 0$, nominal wages are fully rigid, in the sense that they do not respond to the deleveraging shock. The difference is that now in $t > 0$ wages are no longer fully flexible, but evolve according to

$$W_{i,t} = (W_{i,0}\pi^t)^{\phi_t} (W_{i,t}^{flex})^{1-\phi_t}.$$

This expression implies that the nominal wage in period t in country i is a weighted average of the nominal wage in country i in period $t = 0$, $W_{i,0}$, and of the wage that would clear the market for labor, $W_{i,t}^{flex}$.⁴⁶ This reduced form captures in a simple way a case in which every period only part of the wages respond to the deleveraging shock. The fraction of the wages that do not adjust are indexed on the inflation target in the tradable sector, π . The weights

⁴⁶Formally, $W_{i,t}^{flex}$ is defined as the wage that equates the marginal disutility of labor to the marginal benefit that the household gets from working more

$$W_{i,t}^{flex} = -\frac{U_{L_{i,t}}}{U_{C_{i,t}^T}} P_t^T.$$

Table 2: Parameters (quarterly)

	Value	Source/Target
Discount factor	$\beta = 0.9938$	$R = 1.025$ (annualized)
TFP process	$\sigma_{A^T} = 0.0106, \rho = 0.9573$	Benigno and Thoenissen (2008)
Target for trad. inflation	$\pi = 2\%$	Standard value (annualized)
Initial borrowing limit	$\kappa = 3.24$	World debt/GDP = 88%
Final borrowing limit	$\kappa' = 2.57$	Forced savings/world GDP = 1%

given to rigid wages, ϕ_t , declines linearly over time

$$\phi_t = \max\{0, \phi_0 - \Delta t\},$$

so that in the long run wages become fully flexible.⁴⁷ The parameter Δ is set so that complete wage flexibility is reached after two years, or eight quarters.⁴⁸

Table 2 displays the value of the parameters that change with respect to the annual parametrization used in the previous sections. The discount factor β is adjusted so as to target an annualized real interest rate in the initial steady state of 2.5 percent. The parameters governing the TFP process are adjusted so that TFP in the tradable sector exhibits the same persistence and standard deviation as in the annual parametrization, once it is aggregated annually.⁴⁹ The inflation target in the tradable sector is set to 2 percent per year, in line with the definition of price stability given by the Federal Reserve and the European Central Bank. The borrowing limit in the initial steady state is set to $\kappa = 3.24$ to target a world gross debt-to-GDP ratio of 88 percent. This is the same target as in the annual calibration, taking into account the fact that now GDP in each period corresponds to quarterly GDP in the data.

To set the borrowing limit in the final steady state, and hence the size of the deleveraging

⁴⁷The assumption of long run wage flexibility is made to abstract from the impact of wage rigidities on normal business cycles, driven by the productivity shocks, in order to fully concentrate on their interaction with the deleveraging shock.

Midrigan and Philippon (2011) study a similar, though not identical, process of wage adjustment. Alternatively, nominal wage rigidities could be introduced by assuming that each period only a fraction of agents can reset their wages, as in the Calvo model, or by assuming some costs from wage adjustment. However, these alternative formulations of nominal wage rigidities would make the model computationally intractable.

⁴⁸This process for ϕ implies that each quarter between periods 1 and 8 a fraction of wages equal to 0.125 adjusts to the deleveraging shock. A possible interpretation is that it takes 4.3 quarters on average for a wage to adjust to the deleveraging shock. This is in line with the evidence discussed by Olivei and Tenreyro (2010), which points toward an average wage duration of one year in Japan, France, the United Kingdom and the United States. They also report that wages in Germany tend to last between one and three years.

⁴⁹To convert the parameters from annual to quarterly frequency I use the following formulas

$$\rho = \rho_a^{\frac{1}{4}}$$

$$\sigma_{A^T}^2 = \frac{8(1 - \rho^2)}{2 + 3\rho + 2\rho^2 + \rho^3} \frac{\sigma_{A^T,a}^2}{1 - \rho_a^2},$$

where the a subscript denotes annual parameters.

shock, I use the following strategy. In 2009 the euro area countries that were running a current account deficit experienced an abrupt improvement in their current accounts, equal to 1 percent of 2008 euro area GDP.⁵⁰ Accordingly, I set $\kappa' = 2.57$ so that the deleveraging shock generates an amount of forced savings from high-debt countries equal to 1 percent of world GDP in the initial steady state.⁵¹ In particular, I assume that from period $t = 0$ on the borrowing limit follows the linear adjustment path

$$\kappa = \max\{\kappa', \kappa - \Delta_\kappa t\}.$$

The parameter Δ_κ is chosen so that it takes four quarters, or one year, for the borrowing limit to reach its new steady state value. This process for the borrowing limit ensures that the increase in the current account in high-debt countries takes place over one year.⁵² As before, the initial fall in the borrowing limit happening in $t = 0$ is not anticipated by agents, while from period 0 on agents correctly anticipate the path of adjustment of the borrowing limit.

Figure 11 illustrates the transitional dynamics after a shock to the borrowing limit for the model with multi-period wage rigidities. In period 0, the monetary union is hit by an unexpected tightening of the borrowing limit that reaches its new steady state value in four quarters. The deleveraging shock induces agents to increase savings and reduce the demand for consumption, driving down the interest rate. In response, the central bank lowers the nominal interest rate to zero in an attempt to hit the inflation target and the economy enters a liquidity trap that starts in period 0 and lasts four quarters. Since the nominal interest rate cannot go low enough to guarantee market clearing, prices fall to restore equality between demand

⁵⁰The sum of the current account deficits of euro area deficit countries expressed as a fraction of 2008 euro area GDP passed from 2.8 percent in 2008 to 1.8 percent in 2009. To compute these statistics I used data provided by Lane and Milesi-Ferretti (2007).

Another possibility would be to target the behavior of the net foreign asset position of euro area debtor countries. I do not follow this strategy because short run movements in net foreign assets tend to be dominated by valuation effects, which are absent from the model.

⁵¹Formally, define forced savings as the reduction in world debt needed to satisfy the new borrowing limit $\int_{-\kappa}^{-\kappa'} (-\kappa' - B_j) \hat{\Psi}_{ss}(B) dj$, where the subscript ss denotes the initial steady state and $\hat{\Psi}_t(B)$ denotes the distribution of bond holdings. I set $\kappa' = 2.57$ so that

$$\frac{\int_{-\kappa}^{-\kappa'} (-\kappa' - B_j) \hat{\Psi}_{ss}(B) dj}{4GDP_{ss}} = 0.01,$$

where $GDP_{ss} = \int_0^1 P_{ss}^T Y_{i,ss}^T + P_{i,ss}^N Y_{i,ss}^N di$ and steady state GDP is multiplied by 4 to convert it to its annual value. In words, the above expression means that the group of countries that have a debt position in the initial steady state higher than the borrowing limit in the final steady state is forced by the deleveraging shock to reduce debt by an amount equal to 1 percent of world GDP in the initial steady state.

⁵²Another reason to consider a gradual adjustment of the borrowing limit is the fact that the model features only debt contracts that last one period, that is one quarter. In reality, debt can take maturities that are longer than one quarter. Considering a gradual adjustment in the borrowing limit is a simple way of capturing the fact that long term debt allows agents to adjust gradually to the new, tighter, credit conditions.

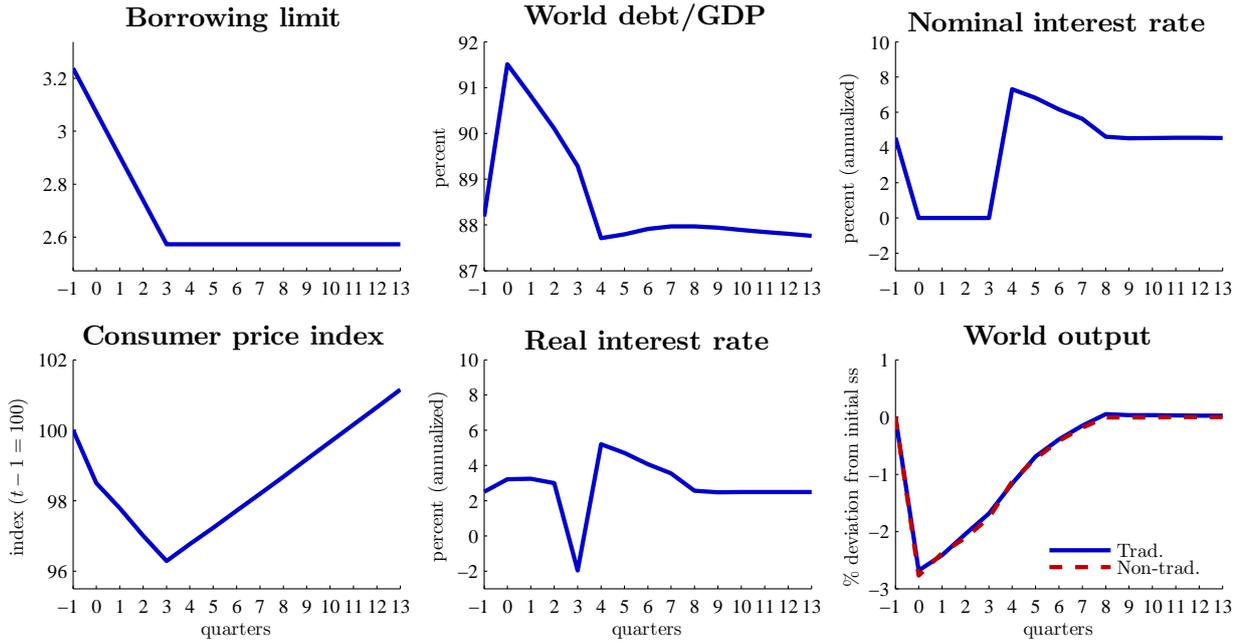


Figure 11: Response to deleveraging shock - multi-period liquidity trap. Note: Consumer price index denotes the monetary union aggregate consumer price index. The real interest rate is the nominal interest rate deflated by inflation in the tradable sector.

and supply. This is illustrated by the bottom-left panel of figure 11, which shows the path of the monetary union aggregate consumer price index (CPI).⁵³ During a liquidity trap the real interest rate is equal to the inverse of expected inflation, hence deflation leads to an increase in the world real interest rate that further depresses consumption demand leading to even more deflation.⁵⁴ This amplification effect, which is not present when the liquidity trap lasts just one period, further depresses aggregate demand and sharpens the recession. Equilibrium is reached through a rise in real wages. In fact, the fall in nominal prices is not matched by an equivalent fall in nominal wages. This reduces profits and induces firms to cut employment and production both in the tradable and in the non-tradable sector.

The result is a prolonged recession that affects all the countries belonging to the monetary union. On impact world output, both of the traded and the non-traded good, falls by almost 3 percentage points below its value in the initial steady state. The recession lasts two years and leads to a cumulative output loss equal to 11 percent of output in the initial steady state. The deleveraging process does not follow a monotonic pattern. Instead, initially the debt-to-GDP

⁵³Formally, the CPI in a generic country i is defined as the minimum price of a unit of the consumption basket C_i

$$CPI_{i,t} = \omega^{-\omega} (1 - \omega)^{\omega-1} (P_t^T)^\omega (P_{i,t}^N)^{1-\omega}.$$

The aggregate CPI of the monetary union is defined as $CPI_t = \int_0^1 CPI_{i,t} di$.

⁵⁴For consistency with the previous sections, the real rate is defined as the nominal rate deflated by inflation in the traded sector. However, quantitatively the difference between inflation in the traded sector and CPI inflation are negligible.

ratio rises due to the sharp fall in GDP. Only starting from the second quarter the ratio of gross world debt-to-GDP starts declining.⁵⁵

Once the liquidity trap is over, in period 4, the central bank raises the nominal interest rate above its value in the new steady state. This happens because the fall in prices coupled with nominally rigid wages keeps labor costs high and supply subdued. Instead, after four quarters of deleveraging the debt overhang is reduced and aggregate demand recovers. The combination of low supply and high demand puts upward pressure on prices, so the central bank has to raise nominal rates in order to dampen the rise in consumption demand to prevent inflation from exceeding the 2 percent target. This explains the slow recovery that takes two years to complete.

Overall, this exercise shows that a reasonably calibrated deleveraging shock, leading to an adjustment in the current accounts of high-debt countries similar to the one observed in the euro area in 2009, leads to a significant recession. In the next sections I discuss some examples of policies that can mitigate the negative impact of deleveraging on output, in order to illustrate how the model can be used to evaluate policy interventions.

6.1 Raising the inflation target

One policy that can mitigate the recession during debt deleveraging consists in adopting a higher inflation target. Figure 12 compares two monetary unions with different steady state inflation targets.⁵⁶ The solid lines refer to the baseline economy, in which the inflation target is 2 percent a year, while the dashed lines refer to an economy with a higher inflation target, of 3 percent per year.

Even with a 3 percent inflation target the deleveraging shock pushes the monetary union into a liquidity trap that lasts four quarters. However, the adjustment is much less traumatic in the economy with higher inflation target. In fact, a higher inflation target guarantees a smaller drop in output, as well as less deflation and lower real rates throughout the liquidity trap. The reason is the following. In the last period of the liquidity trap, period $t = 3$, the real interest rate, defined as the nominal interest rate deflated by inflation in the tradable sector, is equal to the inverse of the inflation target. This happens because the nominal interest rate

⁵⁵This is consistent with the path of the private debt-to-GDP ratio observed during several deleveraging episodes. See McKinsey (2010, 2012).

⁵⁶This section looks at two economies whose steady state inflation target is different. An alternative would be to consider a change in the inflation target in response to the tightening of the borrowing limit. However credibility issues are likely to prevent a central bank from changing the inflation target in the middle of a deleveraging episode. This point is discussed by Eggertsson (2008), who considers credibility issues faced by the FED during the Great Depression.

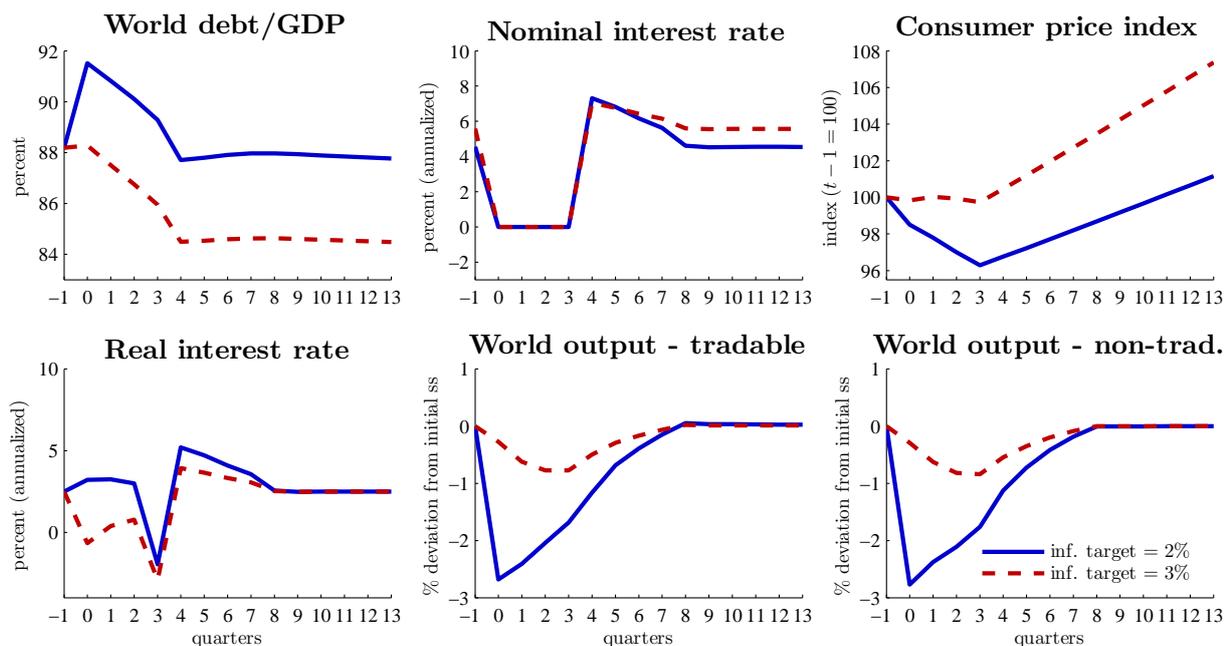


Figure 12: Response to deleveraging shock - higher inflation target. Note: Consumer price index denotes the monetary union aggregate consumer price index. The real interest rate is the nominal interest rate deflated by inflation in the tradable sector.

is equal to zero, so the real rate is equal to the inverse of the inflation rate. Since the central bank hits the inflation target once the liquidity trap is over, the expected inflation in period $t = 3$ is equal to the inflation target. This means that the real interest rate in the last period of the liquidity trap is lower the higher the inflation target.

A lower real rate stimulates demand for consumption in the last period of the trap, limiting the fall in prices and the contraction in output. Moreover, the lower real rate in the last period of the trap has also a positive effect on demand during the previous periods, since aggregate demand depends on the path of all the future interest rates. It follows that during the previous periods too deflation is lower and the drop in output is smaller. The effect is quantitatively important. In fact, raising the inflation target from 2 to 3 percent reduces the cumulative output loss due to the deleveraging shock from 11 to 3.5 percent of steady state output. This experiment suggests that a higher inflation target may be helpful in limiting the recession during a deleveraging episode in a monetary union.

6.2 Transfers within members of the monetary union

One policy that has been much discussed in the context of the ongoing eurozone crisis concerns transfers among members of a monetary union. In this section I consider a simple experiment to evaluate the macroeconomic impact of transfers from creditor to debtor countries. I consider

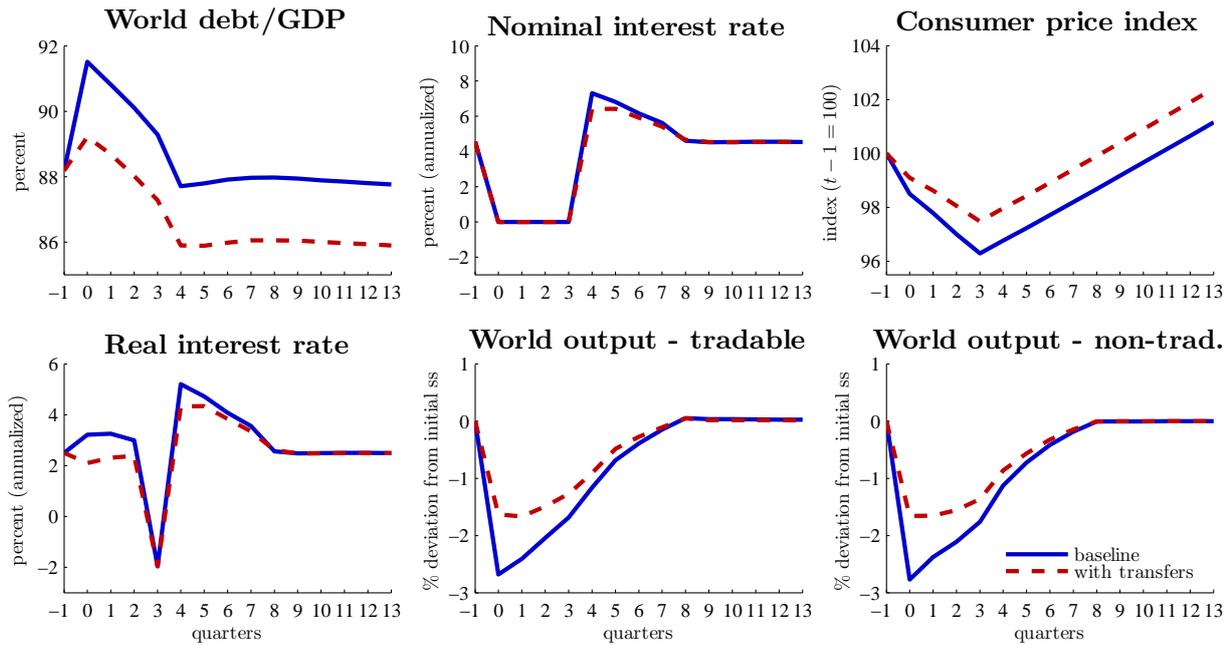


Figure 13: Response to deleveraging shock - transfers. Note: Consumer price index denotes the monetary union aggregate consumer price index.

a scenario in which at the start of period 0 every debtor country receives a transfer equal to 1 percent of its external debt. This transfer is financed by creditor countries, and each creditor country contributes with a sum equal to 1 percent of its stock of assets.⁵⁷ Hence, on aggregate creditor countries transfer to debtor countries a sum equal to 0.2 percent of the annual GDP of the monetary union in the initial steady state.

The results are shown in figure 13. The solid lines refer to the baseline economy, while the dashed lines refer to the economy with transfers. Figure 13 makes clear that transfers from creditor to debtors countries reduce deflation and the output contraction. This happens because debtor countries have a higher propensity to consume out of income than creditor countries. Hence, transfers toward debtor countries stimulate aggregate demand. In turn, the increase in aggregate demand has a positive impact on output, because the recession during the liquidity trap is due to weak aggregate demand. Quantitatively, even a relatively modest transfer such as the one considered in this section can have a significant impact on output. For instance, the transfer scheme considered in this experiment reduces the cumulative loss in output during deleveraging from 11 to 8 percent of steady state output.

This experiment suggests that transfers from creditor to debtor countries of a monetary union can play a role in mitigating the recession associated with an episode of debt deleveraging.

⁵⁷This transfer scheme captures a variety of policies, such as fiscal transfers inside a monetary union or debt relief policies. This experiment also captures some of the aspects of the public flows passing via the ECB which played a major role in cushioning the fall in foreign credit in the countries at the eurozone periphery in the first phase of the 2008/2009 recession, as shown by Lane and Milesi-Ferretti (2012).

7 Conclusion

I propose a multi-country model for understanding deleveraging among a group of financially integrated countries. The model highlights a novel economic mechanism that makes episodes of debt deleveraging particularly painful for monetary unions. Deleveraging leads to a drop in the world interest rate, both because high-debt countries are forced to save more in order to reduce their debt and because the rest of the world experiences an increase in the desire to accumulate precautionary savings. In the absence of nominal rigidities, deleveraging also triggers a rise in production in high-debt countries. If wages are nominally rigid but nominal exchange rates are allowed to float, the rise in production involves a nominal depreciation in high-debt countries. In a monetary union, the combination of nominal wage rigidities and fixed exchange rates prevents any increase in production in indebted countries. This amplifies the fall in the world consumption demand and the drop in the world interest rate. Hence, monetary unions are particularly prone to enter a liquidity trap during an episode of deleveraging. In a liquidity trap deleveraging generates a deflationary union-wide recession, hitting high-debt countries especially hard.

The analysis presented in this paper can be extended in a number of directions. First, the model could be used to investigate a richer menu of policies. In particular, the recent experience of the eurozone has sparked a lively debate on the role of fiscal transfers and mutual insurance inside monetary unions, and the model has the potential to shed light on this key policy issue. In addition, it would be interesting to consider collateral constraints in which asset prices, for instance house prices, play a role in determining access to credit. Mendoza (2010) uses a small open economy model to show how economies in which borrowing depends on the price of capital can endogenously enter deleveraging episodes. An open research question concerns the interactions between these types of constraints and the zero lower bound in a model of the world economy.⁵⁸

⁵⁸See Fornaro (2012) for a small open economy model in which nominal wage rigidities and exchange rate policies interact with occasionally binding collateral constraints.

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Appendix

A Numerical solution method

To solve the model numerically I employ the method proposed by Guerrieri and Lorenzoni (2011).

Computing the steady state of the model involves finding the interest rate that clears the bond market at the world level. The first step consists in deriving the optimal policy functions $C^T(B, A^T)$, $C^N(B, A^T)$ and $L(B, A^T)$ for a given interest rate R . To compute the optimal policy functions I discretize the endogenous state variable B using a grid with 600 points, and then iterate on the Euler equation and on the intratemporal optimality conditions using the endogenous gridpoints method of Carroll (2006). Using the optimal policies, it is possible to derive the inverse of the bond accumulation policy $g(B, A^T)$. This is used to update the conditional bond distribution $\Psi(B, A^T)$ according to the formula $\Psi_\tau(B, A^T) = \sum_{\tilde{A}^T} \Psi_{\tau-1}(g(B, \tilde{A}^T), \tilde{A}^T) P(A^T | \tilde{A}^T)$ for all $B \leq -\kappa$, where τ is the τ -th iteration and $P(A^T | \tilde{A}^T)$ is the probability that $A_{t+1}^T = A^T$ if $A_t^T = \tilde{A}^T$. The bond accumulation function is not invertible at $B = -\kappa$, but the formula above holds if $g(-\kappa, A^T)$ is defined as the largest B such that $B' = -\kappa$ is optimal. Once the bond distribution has converged to the stationary distribution, I check whether the market for bonds clears. If not, I update the guess for the interest rate.

To compute the transitional dynamics, I first derive the initial and final steady states. I then choose a T large enough so that the economy has approximately converged to the final steady state at $t = T$ (I use $T = 200$, increasing T does not affect the results reported). The next step consists in guessing a path for the interest rate, with $R_T = R'$. I then set the policy functions for consumption in period T equal to the ones in the final steady state and iterate backward on the Euler equation and on the intratemporal optimality conditions to find the sequence of optimal policies $\{C_t^T(B, A^T), C_t^N(B, A^T), L_t(B, A^T)\}$. Next, I use the optimal policies to compute the sequence of bond distributions $\Psi_t(B, A^T)$ going forward from $t = 0$ to $t = T$, starting with the distribution in the initial steady state. Finally, I compute the world demand for bonds in every period and update the path for the interest rate until the market clears in every period.

To compute the transitional dynamics with wage rigidities I follow a similar method. The only difference is that the equilibrium in period $t = 0$ has to be modified to take into account the presence of pre-set wages.

Also the numerical solution to the model with multi-period wage rigidities is derived using the method described above. However, the presence of another endogenous state variable, the period 0 nominal wage, for the periods in which wages are partly rigid increases significantly the time needed to obtain a numerical solution.

B A model with interest rate spreads

In the model presented in the main text all the agents, and countries, are subject to the same interest rate. However, in many cases tight credit conditions manifest themselves with high interest rates. In fact, often countries whose access to the international credit markets is restricted are charged a spread over the interest rate paid by unconstrained countries. This appendix shows how it is possible to reconcile this fact with the model without changing any of the results. In particular, in this appendix I present a model in which the borrowing limit is enforced through interest rate spreads and show that this model is isomorphic to the framework studied in the main text. The discussion draws on Uribe (2006).

For simplicity I focus on the economy without nominal rigidities described in section 2, but the results can be extended to the case of a monetary union with nominal wage rigidities. Suppose that the representative household in country i is charged the country-specific interest rate $R_{i,t}$, potentially different from the world interest rate R_t . Suppose also that there is no limit to how much the household can borrow at the interest rate $R_{i,t}$. The Euler equation then writes

$$U_{C_{i,t}^T} = R_{i,t} \beta E_t \left[U_{C_{i,t+1}^T} \right].$$

In the model in the main text, in which the household is constrained by the borrowing limit (3) and it is charged the world interest rate R_t , the Euler equation can instead be written as

$$U_{C_{i,t}^T} = \frac{R_t}{1 - \frac{\mu_{i,t} R_t}{U_{C_{i,t}^T}}} \beta E_t \left[U_{C_{i,t+1}^T} \right],$$

where $\mu_{i,t}$ is the Lagrange multiplier on the borrowing constraint.

Notice that if the household is charged the interest rate

$$R_{i,t} = \frac{R_t}{1 - \frac{\mu_{i,t} R_t}{U_{C_{i,t}^T}}},$$

the two Euler equations coincide. Moreover, we have that $R_{i,t} = R_t$ when $\mu_{i,t} = 0$, while

$R_{i,t} > R_t$ when $\mu_{i,t} > 0$.⁵⁹ Intuitively, investors can make sure that a household respects the borrowing limit by charging a positive spread over the world interest rate anytime the household would violate the constraint if charged the world interest rate. In equilibrium, we would thus observe that high-debt constrained countries are charged a positive spread over the world interest rate.

To obtain a version of the model with interest rate spreads isomorphic to the model in the main text, we must make sure that the resource constraint of the household is not affected by the interest rate spreads. Indeed, whenever the constraint is binding there is a financial rent given by the difference between the cost of funds for the investor and the interest rate that the borrower would like to pay. In the model in the main text this rent accrues to the borrower, since constrained borrowers are charged the world interest rate, that is the cost of funds for investors. We must then ensure that financial rents go fully to the borrower also in the version of the model with interest rate spreads. Following Uribe (2006), this can be done by assuming the existence of domestic financial intermediaries that borrow at the world interest rate R_t and lend to households at the interest rate $R_{i,t}$. Assuming that the profits of the domestic financial intermediaries are fully rebated to households in a lump sum fashion, we obtain that the economy with the borrowing constraint described in the main text is isomorphic to the economy with spreads described in this appendix.

C Proof of proposition 1

To prove that from the perspective of a single country the equilibrium with flexible wages attains the constrained efficient allocation I characterize the solution to the social planner problem for a single country. Importantly, the social planner in a single country takes the world interest rate as given, since a single country is too small to influence the world interest rate.

The social planner in a generic country i chooses $C_{i,t}^T$, $C_{i,t}^N$, $L_{i,t}$, $L_{i,t}^T$, $L_{i,t}^N$ and $B_{i,t+1}$, taking the path for the interest rate $\{R_t\}_{t=0}^{\infty}$ and the initial bond position $B_{i,0}$ as given, to maximize expected utility

$$E_0 \left[\sum_{t=0}^{\infty} \beta^t U(C_{i,t}^T, C_{i,t}^N, L_{i,t}) \right],$$

⁵⁹Using the fact that $\mu_{i,t} \geq 0$ and rearranging the Euler equation in the main text, it is easy to check that $\mu_{i,t} R_t / U_{C_{i,t}^T} < 1$.

subject to the resource constraints

$$C_{i,t}^T = A_{i,t}^T (L_{i,t}^T)^{\alpha_T} + B_{i,t} - \frac{B_{i,t+1}}{R_t} \quad (C.1)$$

$$C_{i,t}^N = A^N (L_{i,t}^N)^{\alpha_N} \quad (C.2)$$

$$L_{i,t}^T + L_{i,t}^N = L_{i,t}, \quad (C.3)$$

and the borrowing constraint

$$B_{i,t+1} \geq -\kappa. \quad (C.4)$$

The first order conditions are

$$U_{C_{i,t}^T} = \lambda_{i,t}^T$$

$$U_{C_{i,t}^N} = \lambda_{i,t}^N$$

$$-U_{L_{i,t}} = \lambda_{i,t}^L$$

$$\lambda_{i,t}^T \alpha_T A_{i,t}^T (L_{i,t}^T)^{\alpha_T - 1} = \lambda_{i,t}^L$$

$$\lambda_{i,t}^N \alpha_N A^N (L_{i,t}^N)^{\alpha_N - 1} = \lambda_{i,t}^L$$

$$\frac{U_{C_{i,t}^T}}{R_t} = \beta E_t [U_{C_{i,t+1}^T}] + \mu_{i,t}$$

$$B_{i,t+1} \geq -\kappa, \quad \text{with equality if } \mu_{i,t} > 0,$$

where U_x denotes the first derivative of the utility function with respect to x and λ_i^T , λ_i^N , λ_i^L and μ_i are the Lagrange multiplier associated respectively with constraint (C.1), (C.2), (C.3) and (C.4) .

Defining

$$w_{i,t} = \frac{\lambda_{i,t}^L}{\lambda_{i,t}^T}$$

$$p_{i,t}^N = \frac{\lambda_{i,t}^N}{\lambda_{i,t}^T},$$

it is easy to verify that the social planner allocation coincide with the equilibrium conditions of the flexible wage version of the model presented in section 2. ■

D Inflation targeting with flexible exchange rates

This appendix explores the adjustment to a deleveraging shock in a world in which exchange rates are flexible and central banks target inflation. The key result is that the combination of floating exchange rates and inflation targeting produces an adjustment pattern qualitatively similar to the one under optimal exchange rate policy.

I start by modifying some aspects of the baseline model to allow for multiple currencies. The household's budget constraint is now specified in units of domestic currency and given by

$$P_{i,t}^T C_{i,t}^T + P_{i,t}^N C_{i,t}^N + P_{i,t}^T \frac{B_{i,t+1}}{R_t} = W_{i,t} L_{i,t} + P_{i,t}^T B_{i,t} + \Pi_{i,t}^T + \Pi_{i,t}^N.$$

In this expression, P_i^T and P_i^N denote respectively the price of a unit of tradable and non-tradable consumption good in terms of the currency of country i , W_i is the nominal wage, and Π_i^T and Π_i^N are now the profits of the firms expressed in nominal terms. Notice that bonds are denominated in units of the traded good.⁶⁰ Households are still subject to the borrowing limit specified in equation (3).

Since the tradable good is homogenous and there are no trade frictions, the law of one price holds

$$P_{i,t}^T = S_{ij,t} P_{j,t}^T. \quad (\text{D.1})$$

In this expression $S_{ij,t}$ denotes the nominal exchange rate of country i against the currency of country j , i.e. the units of country i 's currency needed to buy one unit of the country j 's currency.

In each country the consumer price index (CPI), defined as the minimum price for a unit of the consumption basket C_i , is

$$CPI_{i,t} = \left(\frac{P_{i,t}^T}{\omega} \right)^\omega \left(\frac{P_{i,t}^N}{1-\omega} \right)^{1-\omega}. \quad (\text{D.2})$$

Consistent with the practice of central banks that follow an inflation targeting regime, I consider central banks that target CPI inflation. For simplicity, I focus on central banks that follow a policy of zero inflation targeting, so that $CPI_{i,t} = CPI_i$ for every i and t .

Again for simplicity, I consider the simple form of short-run wage rigidities introduced in section 4. Hence, wages in period 0 are set after the realization of the productivity shock is known, but before the deleveraging shock is revealed to agents. From period 1 on wages are

⁶⁰Allowing for nominal bonds in a world with multiple currency would require a theory of currency denomination of gross financial positions, which is beyond the scope of the paper.

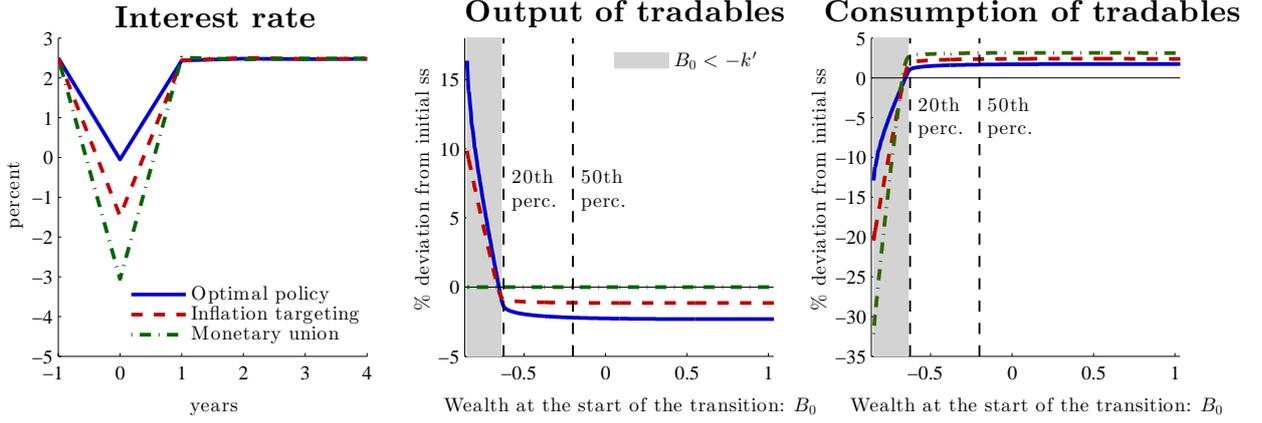


Figure 14: Comparison between optimal policy, inflation targeting and monetary union.

fully flexible.

Figure 14 compares the response of the world interest rate and the country-level responses of the production and consumption of the traded good to the deleveraging shock, for the economy with optimal exchange rate policy, solid lines, the economy with flexible exchange rates and inflation targeting, dashed lines, and the monetary union, dash-dotted lines. As shown by the left panel, the fall in the world interest rate under the floating cum inflation targeting regime stands in the middle between those of the economy with optimal policy and the monetary union. In terms of country-level responses, the adjustment is qualitatively similar to the one under optimal exchange rate policy, with constrained countries increasing their production and decreasing their consumption of the tradable good, while unconstrained countries decrease production and increase consumption of the traded good. Quantitatively, the response of the production of the traded good is milder than under the optimal exchange rate policy, which explains why the world interest rate falls by more under floating exchange rates with inflation targeting than under the optimal exchange rate policy.

To understand the economics behind this adjustment, we can use the fact that under inflation targeting $CPI_{0,t} = CPI_i$ and rearrange equation (D.2) as

$$P_{i,0}^T = \omega \left(CPI_i \left(\frac{1 - \omega}{P_{i,0}^N} \right)^{1-\omega} \right)^{\frac{1}{\omega}} .$$

This expression implies that under inflation targeting the response of $P_{i,0}^T$ and $P_{i,0}^N$ to the deleveraging shock must go in opposite directions so as to keep $CPI_{i,0}$ fixed.

Now consider what happens in a high-debt constrained country if $P_{i,0}^T$ does not respond to the deleveraging shock. In this case production of tradable goods does not respond to the

shock, and households adjust by cutting their consumption of tradable goods. The fall in the consumption of the tradable good also reduces the demand for the non-traded good, leading to, by equation (8), a fall in the price of the non-traded good $P_{i,0}^N$. Hence, to stabilize the consumer price index the central bank must engineer an increase in the domestic price of the traded good $P_{i,0}^T$. The rise in $P_{i,0}^T$ increases the profitability of employing labor in the traded sector, leading to an expansion in the production of the tradable good. This adjustment mechanism explains the increase in the production of traded good in high-debt constrained countries, while an opposite adjustment pattern explains the fall in the production of the traded goods in the rest of the world. The result is that in a world in which exchange rates are flexible and central banks target CPI inflation deleveraging produces a shift in the production of traded goods from unconstrained to constrained economies, qualitatively similar to the one that takes place when exchange rate policy is run optimally.

What does this adjustment imply for the exchange rate? Consider two countries, one that ends up being borrowing constrained following the deleveraging shock, and one that has sufficient wealth so that its borrowing constraint does not bind following the deleveraging shock. The constrained country reduces consumption and experiences an increase in the nominal price of the tradable good, while the unconstrained country increases consumption and experiences a decrease in the nominal price of the tradable good. Since the law of one price holds, equation (D.1) implies that the currency of the constrained country depreciates against the currency of the unconstrained country. More broadly, constrained countries experience a nominal exchange rate depreciation, while unconstrained countries experience an appreciation.