# Pooling Multiple Case Studies using Synthetic Controls: An Application to Minimum Wage Policies

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#### Abstract

We assess the employment and wage effects minimum wage increases between 1979 and 2013 by pooling 29 synthetic control case studies. Using the mean percentile rank, a simple, distribution-free method, we find a sizable, positive and statistically significant effect on the average teen wage. We also test for heterogeneous treatment effects using the distribution of estimated ranks, which has a known form, and detect heterogeneity in the wage elasticities, consistent with differential bites in the policy. In contrast, the employment estimates suggest a small constant effect not distinguishable from zero.

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# **1** Introduction

The synthetic control offers a data driven method for choosing control groups that is valuable for individual case studies (Abadie, Diamond and Hainmueller, 2010). This increasingly popular technique generalizes the difference-in-difference estimator offering a factor-based approach to control for time-varying confounders. For a single state that receives a policy treatment, the synthetic control is the weighted average of untreated units that best predicts the treated state in the pre-treatment period, and the estimator is the post-treatment difference between the treated state and its synthetic control. Whereas conventional regression designs equally weight all units (conditional on covariates), units comprising the synthetic control typically receive unequal weights. Matching on pre-treatment outcomes allows the synthetic control approach to provide unbiased estimates for case studies even when there are multiple unobserved time factors, unlike the conventional difference-in-difference model which imposes a single factor assumption.

In this paper, we present a method for pooling synthetic control estimates to study the effect of state-level minimum wage changes on teen employment and wages. Because the intensity of the treatment varies across cases, we convert the estimates to elasticities by scaling them by the size of the minimum wage changes, and then aggregate these elasticities across events. One methodological contribution of the paper is to show how the mean of the percentile ranks of the effects in the treated states *vis-à-vis* donor (or potential control) states can be used to judge the statistical significance for the pooled Hodges Jr. and Lehmann (1963) point estimate. Pooling the estimates using their ranks is particularly useful since the exact distribution of the sum (or mean) of the ranks under the null is known, enabling us to perform exact inference that is valid for small samples. Additionally, we invert the mean rank statistic to construct the confidence interval for the pooled estimate. Our approach of pooling across treated units is closely related to the van Elteren (1960) stratified rank sum test. It is also a natural extension of the placebo-based inference used by Abadie et al. (2010) for a single case study, where the distribution of a test statistic under the null is constructed by randomly permuting the treatment status of the donor units. Our inferential procedure has some similarity to Conley and Taber (2011); operating under the classic difference-in-difference context,

they also use information from control units to form an empirical distribution under the null, and invert the test statistic to construct confidence intervals that are valid with a small number of treated cases. Finally, Dube et al. (2011) also use a average rank-based test that is valid for small samples in the context of financial market event studies.

Since percentile ranks of the estimates have a known distribution under the null hypothesis, exact inference is feasible not only for the mean but also distributional statistics as well. In this paper we use the Kolmogorov-Smirnov and Anderson-Darling tests to determine whether the distribution of ranked effects indicates heterogeneous treatment effects. One concern when pooling across events is that the quality of the match between the treated and synthetic control unit may be poor in some instances. We assess the role of match quality by trimming on pre-intervention goodness of fit as determined by the mean squared prediction error (*MSPE*). A final contribution of the paper concerns the choice of predictor variables, since there is little guidance on this issue in the existing literature. We use a cross-validation criterion of minimizing *MSPE* among donor units to choose between alternative sets of predictors.

The minimum wage offers an interesting setting for applying the synthetic control estimator, since states receiving treatment have important differences that appear to vary over time, thereby confounding the canonical two-way fixed effects panel estimator (Allegretto et al., 2015). Since the synthetic control method depends on isolated treatment events with well-defined pre- and post-treatment periods, the approach can only utilize a limited amount of minimum wage variation available to conventional regression techniques. We select those events with no minimum wage changes two years prior to treatment and with at least one year of post-treatment data, which we consider to be the minimal requirement for measuring the policy's impact. Of the 215 state minimum wage changes during our 1979-2013 study period, only 29 meet our minimal criteria; on average these events have a 19 quarters of data prior to the intervention and 10 quarters afterward. While this is a limited number of events, we show that pooling across these 29 cases provides us with sufficient statistical power to detect economically relevant effects posited in the literature.

Our results show that the minimum wage changes were binding: 25 out of the 19 cases have

positive effects on average teen wage, with a median elasticity of 0.24 and mean of 0.37. The pooled Hodges-Lehman elasticity of 0.266 is statistically significant at the one percent level using our mean rank test. Turning to teen employment, we find 12 positive elasticities and 17 negative ones. Both the median (-0.051) and mean (-0.058) estimates are small in magnitude. The mean percentile rank is 0.497 and the associated pooled Hodges-Lehman elasticity is -0.036. With a 95 percent confidence interval, we rule out a pooled employment elasticity more negative than -0.170. The distribution of the ranked wage estimates indicate a heterogeneity in the impact, consistent with some minimum wage increases having more "bite," affecting a larger share of the teen workforce. In contrast, the distribution of the ranked employment estimates is consistent with the sharp null of a small (possibly zero) effect everywhere, as opposed to an averaging of true positive and true negative effects across events. To address concerns about match quality, we show that our results are similar when we limit our case studies to those with better pre-treatment fit. We do note that the treated states are generally some of the highest wage areas, making it difficult to find a convex combination of donors to very closely match the average wage level in the pre-intervention period. However, this does not affect our ability to match their overall employment dynamics prior to the intervention.

Three papers in the minimum wage literature have particular relevance to the application of synthetic controls. An early precursor to synthetic controls is the study of California's 1988 minimum wage change by Card (1992). Card compares California with an aggregated control comprised of four southern states and one metro area that failed to raise their minimum wages during the 1987-1989 period. Similar to the synthetic control approach, the aggregated control in Card (1992) roughly matches California on several pre-treatment labor market and demographic characteristics. However, Card's selection of the donor states is heuristic and not based on a solution to the explicit optimization problem underlying the contemporary synthetic control approach.

The 1988 minimum wage increase in California studied by Card (1992) is one of our 29 events. We find a positive wage and employment point estimates for teens, which is broadly consistent with Card (1992)'s findings. However, both the employment and wage elasticities are highly imprecise, with wide confidence intervals containing positive and negative values. This highlights the difficulty in learning very much from an individual case study—a point also stressed by Dube et al. (2010) in the context of pooling across case studies using contiguous area controls. More recently, Sabia et al. (2012) uses the synthetic control approach to study the impact of the 2005 New York minimum wage increase. They ignore four other candidate treatment events that also began the same year in Florida, Minnesota, New Jersey, and Wisconsin. It is not clear what guided the authors' selection of New York as the sole case; in our results for these five states, we find that the New York event is associated with a negative and sizable employment estimate. Sabia et al. (2012) also crucially fail to use *any* pre-treatment outcomes as predictors. Although any characteristics unaffected by the policy treatment are valid predictors under the synthetic control approach, some combination of pre-intervention outcomes, it is able to account for any number of time-varying factors.<sup>1</sup> As a result of omitting pre-intervention outcomes, Sabia et al. (2012) obtain a likely unreliable counterfactual: specifically, employment paths for actual and synthetic New York *never* coincide during the entire 2000-2004 pre-treatment period.<sup>2</sup>

Neumark et al. (2014) use a panel estimator loosely based on the synthetic control method. Allegretto et al. (2015) discusses in detail the problems with this approach. First, they do not actually pool individual synthetic control estimates. Instead, they stack the treated units and the synthetic controls and estimate a two-way fixed effect model using the stacked data with log minimum wage as the main independent variable. Unlike a standard synthetic control study, their estimator does not limit identifying variation to be within a matched pair of treated state and its synthetic control. Rather, it also uses variation in the minimum wage between all treated and synthetic control units, which is difficult to justify within a synthetic control approach. Second,

<sup>&</sup>lt;sup>1</sup>Formally, the unbiasedness of the synthetic control estimator relies specifically on pre-treatment outcome balance between the treated unit and the weighted combination of donors (see Appendix B of Abadie et al. (2010)). The choice of exactly which pre-treatment outcomes and other characteristics to select as predictor variables is not obvious, *a priori*. We provide guidance for these decisions in section 3.2.

<sup>&</sup>lt;sup>2</sup>See Figure 3 of Sabia et al. (2012). Relatedly, the authors try to account for the poor pre-intervention fit by using a *difference-in-difference* with respect to the synthetic control. While this has a heuristic appeal, it is quite different from the synthetic control estimator, which requires the pre-intervention values in the treated and synthetic control units to be close.

in their setup both treatment and potential control units are experiencing minimum wage changes, making the distinction between treatment and control units somewhat meaningless. Moreover, they experience minimum wage changes both before and after "treatment," making the before/after distinction somewhat meaningless as well. Since the synthetic control approach requires a clean pre-intervention period and untreated donors to correctly estimate the donor weights, the violation of these assumptions makes the donor weights they estimate unreliable. Finally, they use a very short pre-intervention window (4 quarters) to calculate synthetic control matches, which makes finding a good match difficult. As shown in Allegretto et al. (2015), the treated and the synthetic control units constructed by Neumark et al. (2014) did not follow parallel trends prior to the treatment. Perhaps as a result of these problems with their sample construction and research design, Allegretto et al. (2015) also note that there is no reduction in employment for the subset of the events used by Neumark et al. (2014) with the most sizable relative minimum wage increases.

In contrast to these prior applications, we select 29 different events using clear and reasonable criteria for case selection, estimate synthetic controls for each treatment using a data-driven choice of predictors, and pool across these estimates using rigorous statistical procedures that are valid for small samples.

A growing number of papers have used the synthetic control approach to study topics as diverse as the impacts of anti-smoking legislation (Abadie et al., 2010), immigration laws (Bohn et al. 2014), and minimum wages (Sabia et al. 2012). However, to date the applications have largely been restricted to estimating the effect of individual treated cases or to presenting numerous such estimates separately. For example, Billmeier and Nannicini (2013) use synthetic controls to investigate the effects of 30 country-level episodes of trade liberalization on their GDP. While the authors helpfully organize their presentation of synthetic and actual GDP trends by region and time period, the presentation of 30 individual pictures obscures their argument that later episodes of liberalization failed to boost GDP. Some episodes appear to raise, lower, or have no effect on growth, and it becomes difficult for the reader to gauge the magnitude of estimates or to draw statistical inference. Using synthetic controls, Campos et al. (2014) estimate a mean effect of EU integration

on GDP, but the authors do not perform statistical inference on either the mean or individual case study estimates.

Two papers conduct statistical inference on the mean treatment effect of multiple synthetic control case studies using a permutation-based test. Cavallo et al. (2013) use synthetic controls to calculate the mean effect of multiple country-specific natural disasters on GDP per capita. With randomization inference on the mean effect, the authors show that there is a statistically significant fall in GDP for the group of the four most fatal disasters events in their data, although the authors find that this may be driven by two of the four events, which also experienced political revolutions near the time of their respective natural disasters. Gobillon and Magnac (2015) pools synthetic control estimates in a Monte Carlo simulation to evaluate several estimators and also uses randomization inference on the mean effect. In contrast, our rank-based inference is less susceptible to outliers, is exact using a known distribution, and also allows for easy assessment of heterogenous treatment effects. In the Appendix we compare our rank-based method of inference to randomization inference on the mean effect and also use rank-based methods to account for serial correlation and the overlap of donors across treatment events.

The synthetic control estimator assumes that the data generating process follows a factor model. Consequently, this paper also relates to a growing literature that use linear factor models to account for time-varying heterogeneity in program evaluation, e.g., Bai (2009). Gobillon and Magnac (2015) provide evidence comparing the performance of alternative estimators using Monte Carlo simulation. In work carried out contemporaneously with our own, a recent working paper by Totty (2015) applies linear factor models such as Bai (2009) to estimate minimum wage effects and finds results that are broadly similar to those we estimate here using a pooled synthetic control approach.

Focusing on the subset of events that have a longer post-treatment period, we are able to investigate the presence of lagged employment effects. Meer and West (2015) find significant lagged effects of state-level minimum wages on overall private-sector employment. In contrast, in our study of teens—a group of workers far more likely to have wages near the minimum than workers generally in the overall private sector—we are unable to detect significant lagged effects

three years after a minimum wage increase. Although the three year estimates are somewhat imprecise, they are consistent with the lack of medium-run employment effects for teens found in other work (Allegretto et al. 2015).

The rest of the paper is structured as follows. Section 2 reviews the synthetic control method and explains our proposed rank-based inference for the pooled estimate. Section 3 discuss our sample and the choice of predictor variables. Section 4 presents our findings, including the mean effect and the test of heterogeneity, as well as issues of match quality. Section 5 concludes.

## **2** Synthetic controls and multiple case studies

#### 2.1 Synthetic control estimator

Consider the case of a single treated state (i = 1) that raises its minimum wage at time t = t', where the outcome of interest  $Y_{it}$  is teen employment. Denoting the intervention as D, the synthetic control approach assumes a data generating process such that the observed outcome  $Y_{it}$  is a sum of the effect from the treatment,  $\alpha_{1t}D_{it}$ , and the counterfactual outcome,  $Y_{it}^N$ :

$$Y_{it} = \alpha_{it}D_{it} + Y_{it}^N = \alpha_{it}D_{it} + \theta_t \mathbf{Z}_i + \lambda_t \mu_i + \delta_t + \varepsilon_{it}$$

Here  $\delta_t$  is an unknown common factor with constant factor loadings across units,  $\mathbf{Z}_i$  is a  $(1 \times r)$  vector of observed covariates unaffected by the intervention, and  $\theta_t$  is a vector of unknown parameters. Like the standard fixed effects model, there is a common time factor  $\delta_t$ . However, there is an additional  $\lambda_t \mu_i$  term as well. Here  $\lambda_t$  is a vector of unobserved time-varying factors and  $\mu_i$  are the unknown factor loadings. Since the factor loadings can vary across states, treatment and control states need not follow parallel trends, conditional on observables. If we knew the true factor loadings  $\mu_1$  for the treated state, we could construct an unbiased control by taking untreated donor states whose factor loadings average to  $\mu_1$ . Since we do not observe the factor loadings, the synthetic control procedure constructs a vector of weights  $\mathbf{W}$  over J donor states such that the

weighted combination of donor states closely matches the treated state in pre-intervention outcomes. This weighted combination of donors is called the synthetic control; as shown in Abadie et al. (2010), the average factor loadings of the synthetic control thus constructed matches the loadings of the treated state.

Formally, for the treated state, define the  $(k \times 1)$  vector of pre-treatment characteristics as  $\mathbf{X}_1 = (\mathbf{Z}'_1, Y_i^{K_1}, \dots, Y_i^{K_L})$ , where k = r + L and  $Y_i^{K_l}$  are L linear combinations of pre-treatment outcomes. Analogously, define the  $k \times J$  matrix  $\mathbf{X}_0$  containing the same characteristics for the J donor states. The synthetic control procedure chooses donor weights W to minimize the distance between pre-treatment characteristics  $\mathbf{X}_1$  and  $\mathbf{X}_0$  of the treated state and untreated states. The distance equals the mean square prediction error (*MSPE*)

$$\sum_{m=1}^{k} v_m (X_{1m} - \mathbf{X}_{0m} \mathbf{W})^2$$

over *k* pre-treatment characteristics, and where  $v_m$  measures relative importance of the *m*-th predictor. Given the optimal weights  $w_j^*$  for each of the j = 2, ..., N donors, the synthetic control at any time *t* is simply the weighted combination of donor employment  $\sum_{j=2}^{N} w_j^* Y_{jt}$ . The estimate of the employment impact  $\alpha_{1t}$  is therefore the difference between employment in the treated state  $Y_{1t}$  and the synthetic state  $\sum_j w_j^* Y_{jt}$  at any post-treatment time  $t \ge t'$ :

$$\hat{\alpha}_{1t} = Y_{1t} - \sum_{j=2}^{N} w_j^* Y_{jt}.$$

When the intensity of treatment varies across events, elasticities offer a simple way of comparing across events. Moreover, the use of elasticities also connects our findings with other estimates in the minimum wage literature. For this reason, our key estimates of interest are the employment or wage elasticities of the minimum wage, defined as follows. For a single treatment event, we construct the synthetic control  $\sum_{j} w_{j}^{*} Y_{jt}$  for the treated outcome  $Y_{1t}$ . In the post-intervention period  $t = t', \ldots, T$ ,

the average percent difference between the treated and synthetic control outcomes is given by

$$\hat{\beta}_1 = \frac{\frac{1}{T}\sum_{t=t'}^T \left(Y_{1t} - \sum_j w_j^* Y_{jt}\right)}{\frac{1}{T}\sum_{t=t'}^T \sum_j w_j^* Y_{jt}}$$

Writing the percent minimum wage increase over the full post-treatment period as

$$\Delta MW = \frac{MW_T - MW_{t'-1}}{MW_{t'-1}}$$

we define the post-treatment elasticity  $\eta_1$  to be the ratio

$$\hat{\eta}_1 = rac{\hat{eta}_1}{\Delta M W}.$$

As we describe below, it will be useful for placebo-based inference to construct analogous elasticities  $\eta_j$  for each of the donor states. Specifically, for each of the donor states j = 2, ..., N we calculate the post-treatment difference  $\beta_j$ , this time using the remaining N - 2 donor states as donors for the synthetic control of state j. The placebo elasticity  $\eta_j$  is scaled by the actual minimum wage increase in treated state:  $\eta_j = \beta_j / \Delta M W$ .<sup>3</sup>

When there are multiple treatment events, we calculate separate event-specific elasticities  $\eta_{e1} = \beta_{ej} / \Delta M W_e$  for the events e = 1, ..., E. Note that this construction of elasticities allows us to incorporate the fact that treated states vary both in their outcome levels and in their minimum wage treatment intensities. To aggregate across events we calculate the mean or median of these estimated elasticities, or calculate the Hodges-Lehman pooled estimate as described in detail below. The mean treatment effect, for example, is equal to the mean elasticity

$$\overline{\eta} = \frac{\sum_e \hat{\eta}_{e1}}{E}$$

<sup>&</sup>lt;sup>3</sup>As we discuss in Section 3, since some states change their minimum wage multiple times during the post-treatment period, we simply define the minimum wage change to be the largest percent change between the post- and pre-treatment periods. We define the elasticity  $\eta_1$  using the ratio of means in  $\beta_1$  rather than the post-treatment mean of the percent changes  $\frac{1}{T} \sum_{t=t'}^{T} \left( \frac{Y_{1t} - \sum_{j} w_j^* Y_{jt}}{\sum_{j} w_j^* Y_{jt}} \right)$  to avoid the possibility that the resulting elasticity has a different sign than the post-treatment mean of level changes in the numerator of  $\beta_1$ .

#### 2.2 Inference using the rank test with single and multiple events

We follow Abadie et al. (2010) in using placebo-based inference from permuting the treatment status of donor states in order to assess the statistical significance of a single treated state's estimated elasticity. For each event, we estimate  $\eta_{ej}$  for every *donor* state *j* (excluding the actually treated state but using the same minimum wage change) and determine whether the elasticity  $\eta_{e1}$  for the treated state lies in the tails of the resulting placebo distribution formed by  $\hat{\eta}_{ej}$  for  $j = 2, ..., N_e$ . Like Abadie et al. (2010), we assume exchangeability of units for the purpose of conducting statistical inference throughout the paper.

Equivalently, we summarize the relative position of the treated state's elasticity among the placebo distribution by using the percentile rank statistic  $p_{e1} = \hat{F}_e(\eta_{e1})$ , where  $\hat{F}_e$  is the empirical CDF of the elasticities  $\hat{\eta}_{ej}$  from event e.<sup>4</sup> Since the percentile rank is (approximately) uniformly distributed on the unit interval, we determine whether the rank of the treated state  $p_{e1}$  lies in the tails of the uniform distribution. Using a statistical significance level of five percent, we reject the null of  $\eta_{e1} = 0$  precisely when  $p_{e1} < 0.025$  or  $p_{e1} > 0.975$ . We note that the number of available donors limits the range of confidence levels we can implement for a single treated event. For example, many of our events have only twenty donors; in these cases we can only assess a ten percent level of significance. Using multiple events allows us to assess stronger levels of statistical confidence.

The above approach suggests a natural way of conducting inference when pooling across cases by constructing a test statistic  $\overline{p}$  which is the the mean of the percentile ranks of individual events:

$$\overline{p} = \frac{\sum_{e=1}^{E} p_e}{E}.$$

The exact distribution of  $\overline{p}$  can be calculated using the Irwin-Hall distribution of the sum of *E* independent uniform random variables. The sum of the ranks,  $s = E \cdot \overline{p}$ , has the the CDF

<sup>&</sup>lt;sup>4</sup>To calculate the percentile  $p_{ei}$  of the ranked position  $r_{ei}$  of the estimated elasticity  $\eta_{ej}$  for state *i* in event *e*, we use the Weibull-Gumbel rule (see Hyndman and Fan, 1996):  $p_e = r_{e1}/(N_e + 1)$ , where  $N_e$  equals one plus the number of donor states, ensuring that the median effect within an event receives the rank 0.50 when the total number of states  $N_e$  is odd.

$$\Gamma(s;E) = \frac{1}{E!} \sum_{k=0}^{\lfloor s \rfloor} (-1)^k {\binom{E}{k}} (s-k)^{E-1}$$

where  $\lfloor . \rfloor$  is the floor function.<sup>5</sup> Under the sharp null hypothesis of zero effect everywhere, the average of *E* ranks,  $\overline{p}$ , is distributed with mean 0.5. If  $G(x; E) = \Gamma(x \cdot E; E)$  denotes the CDF of the mean of *E* uniformly distributed variables random variables, then for a statistical significance level of five percent, we reject the null hypothesis  $\overline{\eta} = 0$  precisely when  $G(\overline{p}; E) < 0.025$  or  $G(\overline{p}; E) > 0.975$ .

While the central limit theorem tells us that the distribution of the mean rank will converge to an appropriately scaled normal distribution, for small *E* we should prefer to use the exact distribution. Table A1 shows various percentiles of this distribution for E = 1, ..., 30. At 29 treatment events— the maximum number of case studies we will have in our study—a two-sided 5% significance test requires the mean rank to fall below 0.395 or above 0.605. We note that this method is closely related to the van Elteren (1960) stratified rank sum test, where the rank of each treatment is estimated using placebos associated with the stratum (i.e., event). The only substantive difference is that we use the percentile ranks of each treatment from each stratum,  $p_{e1}$ , instead of the ranked position  $r_{e1}$ , for transparency of the calculations; this choice potentially impacts the critical values when the number of observations (states) varies across strata (events) and the number of observations is also small. However, as we show in the Appendix, there is very little difference if we calculate the critical values taking into account the number of observations in each stratum used to calculate the ranks. For concision, in the rest of this paper we will often we refer to the percentile rank as simply the "rank."

While there are alternative ways of doing pooled inference, we note some advantages to our approach. First, the rank-based pooling is a natural generalization of the single-case study based inference in Abadie et al. (2010), who use the rank of the treatment effect for individual events. Second, the mean (or sum of) ranks has a known distribution under the sharp null, allowing for exact inference. This avoids reliance on large sample properties, and also avoids the empirical

<sup>&</sup>lt;sup>5</sup>See http://en.wikipedia.org/wiki/Irwin-Hall\_distribution.

estimation of distribution of the statistic under the null—as would be the case were we, for example, to conduct inference for the mean elasticity. Third, and relatedly, the use of the mean rank  $\overline{p}$  diminishes the impact of outliers as compared to the mean elasticity  $\overline{\eta}$ , which may be a particular concern given a small number of events. Fourth, within the class of rank sum tests, the ranks could be estimated without regard to strata, as in the case of the Wilcoxon (1945) rank sum test. However, stratification accounts for event-wise heteroscedasticity, which may be of particular concern given varying window lengths across events. One limitation of the rank-based pooling is that we are testing the sharp null that effect is zero everywhere, as opposed to the *average* effect being zero. However, we address this concern in Section 4.3 by testing for heterogeneous treatment effects.

In the Appendix, we relax the approximation that the event ranks are independently and uniformly distribution by accounting for the finite number of donors, some of which overlap across events. We show that in our case this makes little difference to the calculation of the critical values, or the resulting confidence intervals for the treatment effect. For comparison, we also calculate the confidence interval using randomization inference on the mean effect (elasticity), as opposed to using the mean rank. This too produces similar conclusions, though the confidence intervals are somewhat wider—consistent with the impact of outliers when evaluating the mean (as opposed to the ranked) effect.

#### **2.3** Inverting the rank test to form confidence intervals

We also invert the individual-event and mean rank statistic to estimate confidence sets.<sup>6</sup> These confidence sets show values of the elasticities which imposed as the null cannot be rejected as being equal to the estimated effect. For a single treatment event with estimated elasticity  $\hat{\eta}_{e1}$ , we use the percentile rank  $p_{e1} = \hat{F}_e(\hat{\eta}_{e1})$  as the test statistic to determine statistical significance: we cannot reject the null hypothesis  $\eta_{e1} = 0$  at the five percent level precisely when  $0.025 \leq \hat{F}_e(\eta_{e1}) \leq 0.975$ . Inverting this test, we ask for what values of  $\tau$  does the adjusted response  $\eta_{e1} - \tau$  appear free from

<sup>&</sup>lt;sup>6</sup>Although Abadie et al. (2010) do not explicitly construct these confidence sets in the case of their single treatment event, they follow directly from their inferential procedure.

treatment: when does  $0.025 \le \hat{F}_e(\hat{\eta}_{e1} - \tau) \le 0.975$ ? The 95 percent confidence interval is the set of  $\tau$  not rejected using the critical values 0.025 and 0.0975.

In the framework of multiple treatment events, we can apply a similar procedure to construct Hodges Jr. and Lehmann (1963) confidence intervals for the pooled effect, using the mean rank  $\overline{p}$ as the test statistic to be inverted. We first calculate the adjusted responses  $\eta_{e1} - \tau$  for all events e = 1, ..., E, and re-calculate event-specific ranks  $\hat{F}_e(\hat{\eta}_{e1} - \tau)$ . Define the mean adjusted rank

$$\overline{p}(\tau) = \frac{\sum_{e} \hat{F}_{e}(\eta_{e1} - \tau)}{E}.$$

The 95 percent confidence interval for the pooled effect is the set of  $\tau$  such the mean adjusted rank  $\overline{p}(\tau)$  lies within the critical values given by the mean of *E* uniform distributions. In other words, we find values  $\tau$  such that  $0.025 < G(\overline{p}(\tau); E) < 0.975$ . Figure 1 illustrates this procedure for the estimated mean elasticity  $\overline{\eta} = c$ . The confidence interval is (c - b, c + a) because  $G(\overline{p}(c - (c + a)); E) = 0.05$  and  $G(\overline{p}(c - (c - b)); E) = 0.95$ .

Collapsing these confidence intervals yields the Hodges-Lehman point estimate, which we also refer to as the pooled estimate in this paper. In the case of a single event, the mean, median, and Hodges-Lehman point estimates are trivially the same, and so are the confidence intervals. In the case of multiple events, the mean, median and Hodges-Lehman point estimate and confidence intervals need not correspond. This is especially the case when outlying estimates of individual treatment events heavily influence the mean estimate. The robustness to outliers is one reason we prefer using the Hodges-Lehman confidence interval, as it is ultimately based on ranked location. Throughout the paper, we report the mean percentile rank, the pooled Hodges-Lehman point estimate, and the Hodges-Lehman confidence intervals. We also report the median and mean estimates because of their natural interpretations.

Our inference assumes that the ranks of the treated states across events are independent draws. There are two potential concerns with this assumption, but overall we do not believe they represent major problems in our case. First, some events are from the same state, which may bring up a concern that the ranks of the events are not independent draws. However, while  $Y_{it}$  may be serially correlated, the same need not be true for  $\hat{\eta}_{eit}$  across two events e' and e'' from the same state i in time periods t' and t''. If the synthetic control estimator is unbiased, and it successfully matches pre-treatment outcomes of both events, the post-treatment gap would from the two events are (by construction) uncorrelated:  $E(\hat{\eta}_{e'1}, \hat{\eta}_{e''1}) = 0$ . Moreover, this can be verified empirically.

The second and more serious concern is that the because the minimum wage increases often occur around the same time, two states with minimum wage increases may share many of the same potential donors. As a result, the ranks determined by the placebo distributions are not truly independent across treatment events. For two events e' and e'', the set of placebo estimates  $\hat{\eta}_{e'qt'}$  and  $\hat{\eta}_{e'qt''}$  from donor q may be correlated, in particular when t' = t''. In the extreme case, the donors and hence the placebo estimates  $\hat{\alpha}_{e'qt'}$  may be identical. This may induce a correlation in the ranks  $\hat{F}_{e'}(\hat{\eta}_{e'1})$  and  $\hat{F}_{e''}(\hat{\eta}_{e''1})$  even though  $E(\hat{\eta}_{e'1}, \hat{\eta}_{e''1}) = 0$ . In reality the overlap in donor pool is only partial, which mitigates this problem. However, since this may be a concern in other applications, we provide a more computationally intensive (but more accurate) method of constructing the critical values for hypothesis testing in the Appendix. As described further in that section, we draw sets of 29 placebo-law interventions that match the timing and donor overlap has little impact on the estimated critical values, justifying our use of the mean of independent uniform distributions.

Relatedly, one reason to prefer conducting inference using the mean rank is that under the independence assumption, we know its exact distribution under the sharp null. This virtue cannot be claimed by the sample mean elasticity, whose distribution under the null is unknown. We must empirically estimate the mean elasticity under the null using the mean of donor elasticities. A second, and related, reason to prefer rank-based inference is that it allows for conceptually simple tests of heterogeneity in the treatment effects, as described in section 4.5.

## **3** Minimum wage treatment events and empirical specification

#### **3.1** Sample periods and timing of treatment

The synthetic control estimator requires a set of untreated or donor units for each treatment event. Since the vast majority of states were affected by the federal minimum wage increases, federal increases are not suitable for use with the synthetic control method: there are very few untreated donors that can be drawn from to construct a synthetic control for affected states. For example, 45 states changed their minimum wage at some point during the year of the 2007 federal minimum wage increase, leaving only 5 states as potential donors to form synthetic controls.

To maximize the number of treatment events, we consider the entire 1979-2013 period available using Current Population Survey (CPS) data. We focus on teen employment and wages, as many 16- to 19-year olds have wages near the minimum. During this period, almost 38 percent of teens received wages within 10% of the statutory minimum wage, compared with about 5 percent of workers aged 20 to 64. While there is considerable debate regarding the size of teen employment effects, we expect to find significantly positive effects on teen wages. The high incidence of minimum wage workers among teens makes them the most frequently studied group in the minimum wage literature (e.g., Neumark et al. 2014, Allegretto et al. 2015). For outcome variables we calculate quarterly state-level teen employment-to-population ratios and average wages using the CPS.<sup>7</sup> Although annual state means would contain less noise, they would correspondingly limit the number of pre- and post-treatment observations; moreover, not all minimum wage increases occur during the same part of the calendar year.

The top panel of Figure 2 shows all quarterly minimum wage changes during the study period. During this period the federal minimum wage increased nine times, indicated by the vertical lines in the Figure. Aside from federal minimum wage changes, 33 states in this period raised their

<sup>&</sup>lt;sup>7</sup>For employment outcomes we use the Unicon CPS extracts for the monthly Basic Survey (http://unicon.com). Wage data is only available in the outgoing rotation group subset of these data; for wage data, we use the NBER Merged Outgoing Rotation Group extracts (http://www.nber.org/morg/annual/). We calculate wages as hourly earnings or, if these are not reported, weekly earnings divided by usual weekly hours. State-quarter-level averages use the sampling weights.

minimum wage 215 times. Many states increase their minimum wage frequently, often on an annual basis. To utilize the synthetic control method, we limit the sample of usable treatment events to those with well-defined pre- and post-treatment periods. We select those events with no minimum wage changes two-to-eight years prior to treatment, and we require at least one year of post-treatment data (eliminating from consideration very recent minimum wage changes in Rhode Island and Missouri).We also limit the sample to minimum wage increases of at least 5 percent, which discards states with small increases indexed to inflation. Finally, we only consider treatment events with at least 5 untreated states so that there are a sufficient number of potential donor states to form synthetic controls. These restrictions reduce the pool of state-level minimum wage increases by more than 88 percent and yield the 29 treatment events in the top panel of Figure 2 labeled in dark text.

The eligible 29 events have valid pre- and post-treatment periods of varying length. West Virginia, for example, has many years of data prior to its minimum wage change in 2006q3 available but only one year of post-treatment data. By contrast, California's treatment in 2001q1 allows only two years of clean pre-treatment data but many years of post-treatment data. Also, California's post-treatment period includes an additional minimum wage increase in 2002q1. To simplify choices, for each event we select its "maximal" pre-treatment period available from 8-32 quarters; having done so, we then select each event's maximal post-treatment window from 4-12 quarters. The bottom panel of Figure 2 illustrates these pre- and post-treatment selections in blue and red, respectively, with red circles indicating the times of treatment. Two features stand out. First, while the pre-treatment period contains no minimum wage increases by definition, the post-treatment period includes multiple minimum wage changes-states that raise their minimum wage often do so again within the next year or two. Table 1, which lists all 29 treatment event configurations that form the basis for our primary specifications, shows that most events include multiple minimum wage increases. There are four events whose post-treatment period includes four minimum wage increases. For this reason our treatment intensity definition incorporates the maximum minimum wage in the post-treatment period.

Second, Figure 2 there are three states in the 2000s with recurring minimum wage changes where the post-treatment period of one minimum wage change overlaps with the pre-treatment period of a later minimum wage change: Hawaii, Rhode Island, and Vermont. For example, Hawaii's post-treatment period for its 2002q1 treatment overlaps with the pre-treatment period of Hawaii's 2006q1 treatment. Delayed effects from the former 2002q1 treatment could in principle violate the assumption that, for the latter 2006q1 event, Hawaii's pre-treatment period is absent from treatment. On the other hand, the pre-treatment period of Hawaii's 2006q1 is absent from treatment using our original definition that it contains no minimum wage changes. For our primary specifications we will include all 29 events, but we will also describe results excluding the three events of Hawaii 2006q1, Rhode Island 2006q1, and Vermont 2004q1.

There is a trade-off between window length and the number of events and donors. Allowing relatively short pre- and post-treatment periods maximizes the number of treatment events but, at the same time, may reduce the quality of the estimated counterfactual, as there is less pre-treatment data informing the selection of synthetic controls. On the other hand, lengthy pre-treatment periods limit both the number of events and potential donors, thereby reducing the credibility the resulting estimates. When we limit our treatment events to those with more restrictive pre- and post-treatment window lengths, we sharply reduce the number of case studies, as Table 2 illustrates. The first line in Table 2 is our primary configuration: 29 events with at least 8 and 4 quarters of respective preand post-treatment data. Requiring pre-treatment and post-treatment windows of at least 16 and 8 quarters, respectively, curtails the number of case studies to 14, and there is only a single treatment event with the most restrictive window configuration of 32 pre-treatment quarters. In terms of the potential for alternative window configurations to affect donor availability, the configurations in Table 2 show only a small amount of variation. As we limit the pool of case studies to the most restrictive window configurations, the mean minimum wage treatment rises a small amount, from about a 19 percent increase to an increase of about 24 percent when we require 6 years and 2 years of pre- and post-treatment data, respectively. Our primary results use the maximal window configuration with 29 events, but we explore how the alternate window configurations affect our

results in Section 4.3.

#### **3.2** Specifying predictor variables

Any characteristics unaffected by the policy intervention are valid predictors under the synthetic control approach, including demographic and industrial compositions or other economic attributes of the region. However, the unbiasedness of the estimator relies on the predictors including some linear combination of the pre-treatment values of the outcome of interest. There are two related questions when it comes to these predictors. First, exactly which variables should one include in the set of predictors? Second, what weight should one place on each of those predictor variables when estimating the donor weights? Abadie et al. (2010) provides a simple answer to the second question of how best to determine the weights on specific predictors within a set, which we describe first. Then we tackle the more challenging question of what predictors—and specifically what pre-treatment outcomes—one should include in this set.

For a given event *e*, the optimal donor weights are defined as

$$\mathbf{W}_{e}^{*}(\mathbf{V}_{e}) = \underset{\mathbf{W}_{e}}{\operatorname{argmin}} \sum_{m}^{k} v_{m} \left( X_{e1m} - \mathbf{X}_{e0m} \mathbf{W}_{e} \right)^{2}.$$
(1)

The optimal weights depend on the predictor importance matrix  $\mathbf{V}_e = \{v_{em}\}$  selected by the researcher. For example, **V** might weight each predictor equally. Instead we follow the suggestion in Abadie et al. (2010) to select  $\mathbf{V}_e^*$  such that the resulting synthetic control best fits pre-treatment outcomes. We therefore solve the joint (nested) optimization problem given by equation 1 and the equation

$$\mathbf{V}_{e}^{*} = \underset{\mathbf{V}_{e}}{\operatorname{argmin}} \sum_{t < t'_{e}} (Y_{e1t} - Y_{e0t} \mathbf{W}(\mathbf{V}_{e}))^{2}$$

which minimizes pre-treatment fit. Our results use the "optimal" choice of weights  $\mathbf{W}_{e}^{*}(\mathbf{V}_{e}^{*})$  instead of alternatives such as manually specifying weights for predictors, or using the computationally less intensive methods available to users.<sup>8</sup>

<sup>&</sup>lt;sup>8</sup>We implement the synthetic control approach in Stata using the synth package with nested optimization and

But exactly which sets of pre-treatment outcomes and other characteristics should the researcher choose as predictors? When computationally feasible, perhaps the simplest strategy is to include every pre-treatment outcome in the predictor set X. In their study of the effects of Arizona's 2007 Legal Arizona Workers Act, Bohn et al. (2014) employ this strategy with annual CPS data, using every pre-treatment value of the 1998-2006 non-citizen Hispanic share of the population, in addition to other industrial and demographic shares.

Within the pre-intervention sample, one cannot do any better in terms of pre-intervention MSPE than to include every pre-intervention outcome. However, this will not be true when predicting out of the pre-intervention sample, which is ultimately the object of interest. Matching on higher frequency pre-intervention data may actually produce less reliable synthetic controls. For example, our study uses quarterly CPS data, we risk matching on noise when using as predictors every quarterly pre-treatment value of teen employment-to-population ratios or average wages. As a result, we also consider the predictor set **X** consisting of annualized averages of the pre-treatment outcome.<sup>9</sup>

Different sets of predictors may result in different synthetic controls, and there is little explicit guidance in the synthetic control literature to assess predictor choice. We consider four different predictor sets  $\mathbf{X}$ , which vary according to whether we include every quarterly or annualized pre-treatment outcome, and whether we include other pre-treatment average demographic, labor market, industry shares.<sup>10</sup> These predictor sets are summarized at the bottom of Table 3. Using teen employment as an example outcome, predictor set 1 is composed of all quarterly pre-treatment values of teen employment-to-population ratios. Predictor set 2 is composed of all annualized pre-treatment

allopt starting point checks for robustness: http://www.mit.edu/~jhainm/synthpage.html. There is a option for using a less computationally intensive but less reliable "regression-based" predictor weights. In our experience, the regression-based weights can produce worse fit, and the nested optimization uses regression-based weights as an initial set of values for optimization.

<sup>&</sup>lt;sup>9</sup>Here, annualized averages refer to the mean of the first through fourth quarter before treatment, the mean of the fifth through the eighth quarter before treatment, *etc*. For Minnesota's 2005q3 treatment, say, these refer to the 2004q3-2005q2 mean, the 2003q3-2004q2 mean, *etc*.

<sup>&</sup>lt;sup>10</sup>The demographic and labor market variables are the pre-treatment means of white, black, female, and married shares of the teen population, the teen population share, the share of the overall population with a college degree, and the overall unemployment rate. Industry variables are the employment shares in agriculture & mining, construction, manufacturing, wholesale & retail trade, transportation & utilities, information/finance/professional/business services, education & health services, leisure/hospitality/personal services, and public administration.

employment-to-population ratios. Predictor set 3 includes all annualized pre-treatment employment *and* wage outcomes. Predictor set 4 adds to predictor set 3 the pre-treatment demographic, labor market, and industry shares described above. We note that when every quarterly pre-intervention outcome is included in the predictor set, inclusion of other predictor variables is redundant when weights on those predictors are calculated optimally using nested optimization. For this reason, it only makes sense to include variables such as industry or demographic shares when using annualized and not quarterly pre-treatment outcomes.

To identify the "best" choice for  $\mathbf{X}$ , we use a cross-validation procedure to choose from different sets of predictors. Recall that in creating synthetic controls for each event, the pre-intervention observations form a "training sample" used to estimate synthetic control donor weights as well as predictor weights for a given set of predictors. Here, when choosing the most reliable set of predictors, we use the post-intervention observations of the donors as our "validation" sample to evaluate prediction error associated with a given set of predictors. For a given predictor set  $\mathbf{X}$ , we calculate the post-treatment mean-squared prediction error (*MSPE*) for each donor *j* given by

$$MSPE_{ej} = \frac{1}{T_e} \sum_{t=t'_e}^{T_e} \left( Y_{jte} - \sum_q w_{eq}^* Y_{eqt} \right)^2$$

where  $t'_e$  begins the post-treatment period in event *e*, and where *q* indexes the available N - 2 donors for (untreated) state *j*. We define the average *RMSPE* to be the square root of the mean of this quantity across all donors for all 29 events. The optimal model will yield the smallest post-treatment *RMSPE*, so predictor sets **X** with higher average *RMSPE* in the post-treatment period indicate models with worse performance in the sample of untreated donors.<sup>11</sup>

Table 3 reports the average donor *RMSPE* for both the post-treatment (validation) and pretreatment (training) samples across four candidate specifications for predictors. Predictor set 1, which uses quarterly pre-treatment outcomes, naturally obtains the best pre-treatment fit to quarterly employment or wages when compared to predictor sets 2 through 4, which try to fit quarterly

<sup>&</sup>lt;sup>11</sup>We do not use the treated states for this cross-validation exercise because use of the post-treatment period in these states would require us to also have a valid estimate of the treatment effect.

frequency data using annualized pre-treatment outcomes. Incorporating both annualized outcomes and additional controls improves pre-treatment fit relative to using only one annualized outcome: for employment, pre-treatment *RMSPE* falls from about 0.040 in specification 2 to about 0.035 in specifications 3 and 4.

While using every pre-treatment outcome by definition maximizes goodness-of-fit in the preintervention sample, the same need not hold out of sample. In terms of post-treatment fit, the specification 4 is actually mildly preferable to specification 1. Using both annualized outcomes and demographic, labor market, and industry shares in specification 4, the post-treatment *RMSPE* for teen employment is about 0.0472, compared to the *RMSPE* of about 0.0478 for quarterly predictors. For wages, post-treatment *RMSPE* falls more—from 0.7911, when using quarterly outcomes in specification 1, to about 0.7758 in specification 4. The observed reduction in *RMSPE*—although admittedly small—is consistent with our *a priori* concerns about noise in the aggregations of quarterly CPS data, leading us to select specification 4 as the preferred one. Yet because the small measured reduction in *RMSPE* makes our preference for this model somewhat weak, we explore the robustness of estimates across all sets of predictors in section 4.3.

## **4** Synthetic control estimates of minimum wage effects

#### 4.1 Donors selected by synthetic control

Conditional on other covariates, conventional regression effectively assigns equal weights to the states the researcher selects as potential controls. By contrast, the synthetic control approach selects a convex combination of donor states based on that combination's pre-intervention fit to the treated state. For our sample of treatment events, we observe that the synthetic control procedure on average assigns greater weights for nearby donors, suggesting that nearby states generally form better counterfactuals than do distant states. To illustrate this, Table 4 compares average per donor weights for those donors near to and further away from the treated state. For each treated state, some donors reside within the same Census region as the treatment, whereas other donors lie

outside that region. We first calculate the sum, across events, of all weights for these within-region donors, and then we divide this sum by the total number of within-region donors. The first entry in Table 4 is the resulting within-region per donor weight, 0.050, when the outcome of interest is the teen employment-to-population ratio. For outside-region donors, the per donor weight is 0.027. Calculating per donor weights in this way adjusts for the fact that the number of potential donors within or outside a given area varies across treatments.

The primary statistic of interest in Table 5 is the ratio of within-area to outside-area per donor weights. For the employment-to-population ratio, the relative weight is 1.836, indicating that donors within the same Census region as the treated state are, on average, assigned weights almost twice as high as donors from outside the the same Census region. Relative weights tend to increase as we restrict the relative distance band. Same-Census-division donors—a finer aggregation level—receive even more weight, with relative weights of about 3.0 and 2.5, for teen employment and wages, respectively.<sup>12</sup> Donors within 1000 miles receive 1.3 to 1.5 times as much weight, and donors within 500 miles receive about 2.0 times as much weight. On the whole, the evidence suggests that nearby donors are more likely to be included in a synthetic control, consistent with spatial correlation in the factor loadings underlying the data generating process.

## 4.2 Primary results

We begin with reporting the estimates for each of the 29 treatment events in Table 5. First, the results appear to indicate a positive impact of minimum wage increases on average teen wages. While the wage elasticity estimates range from -0.188 to 1.969, we find that 25 out of the 29 estimates are positive and more than half (16) are strictly greater than 0.20. As described earlier, the reported rank is the percentile rank of the treated state's elasticity relative to the placebo distribution. Seven of the 29 estimated wage effects are statistically significant at the 10 percent level.

Turning to teen employment, the estimated elasticities range between -1.199 and 0.769, although

<sup>&</sup>lt;sup>12</sup>The US Census Bureau partitions the country into four Census regions and nine Census divisions: https://www.census.gov/geo/www/us\_regdiv.pdf.

14 of the 29 events have elasticities no greater than than 0.2 in magnitude. Consistent with a small treatment effect, 12 out of the 29 employment estimates are positive. Only a single event, Massachusetts in 2000q1, has an elasticity (-0.456) that is statistically significant at the 10 percent level. Highlighting the imprecision of individual case studies, we find that the confidence intervals are wide, with an average spread of 1.474 (1.762) for employment (wage) elasticities.

The presence of occasionally very large estimates is partly due to the non-normality of the distribution of synthetic control estimates. To show this, Figure 5 compares probability densities of the *donor* employment and wage elasticities to normal probability densities. For both employment and wage outcomes, the placebo distribution formed by the donors is clearly non-normal: although centered close to zero (about -0.01 and 0.01 in employment and wages, respectively), extreme values give the placebo distribution fatter tails. The estimated kurtosis is 5.82 for donor employment elasticities and 58.37 for wage elasticities, compared to the value of 3.0 for any normally distributed sample. The especially severe departure from normality in wage estimates is partly due to extreme estimates in this space with poor *pre*-intervention fit, as discussed in Section 4.3. Shapiro-Wilk tests clearly reject the null of normality in both cases, with p-values close to zero. In the presence of such fatter tails, the placebo-based confidence intervals are more appropriate than those formed under large sample assumptions.

The imprecision of individual estimates highlights the gains from pooling case studies. Table 6 presents our preferred aggregated results as both the mean elasticity and median elasticity across events. As discussed earlier, we also present the mean ranks, and the associated Hodges-Lehmann confidence intervals; both the median estimate and the Hodges-Lehman interval are less swayed by potential outliers, a concern that is highlighted by the presence of fatter tails. The median and mean employment elasticities for the 29 treatment events are relatively small: -0.051 and -0.058, respectively. Across treatment events, the mean employment rank is 0.470, close to would be expected under the null of a zero treatment effect. The pooled Hodges-Lehman effect is small at -0.036 and is statistically insignificant, as the mean rank falls between the cutoffs (0.395, 0.605) derived from the 2.5th and 97.5th percentiles of the mean of 29 uniformly distributed variables. The

associated 95 percent confidence interval is (-0.170, 0.087). Although somewhat wide, pooling across the 29 events nonetheless allows us to draw economically meaningful inference, and rules out a substantial portion of the old "consensus" estimate range of -0.1 to -0.3. (Brown 1999).

These small aggregated employment effects contrast sharply with those for wages, where the median and mean elasticity are 0.237 and 0.368, respectively. The pooled wage elasticity of 0.266 is statistically significant at the 1 percent level, as the mean rank is 0.758. The associated 95 percent confidence interval rules out wage effects smaller than 0.169 and larger than 0.414.

Figure 3 illustrates these aggregate effects by showing the time path of the mean annualized employment and wage elasticities, both before and after the minimum wage increase.<sup>13</sup> The top panel shows the mean annualized employment elasticities ranging from 7 years prior to the minimum wage increase (i.e., quarters -28 through -25) to 3 years afterward (i.e., quarters 8 through 11). The middle panel shows the analogous estimates for wages. The bottom panel shows the number of treated states used for the estimation of the elasticity of each 4-quarter bin, as well as the associated proportionate change in the minimum wage.

For employment, all pre-treatment point estimates are small in magnitude hovering around zero, adding validity to our research design. After the minimum wage increase, employment nominally falls, but the elasticity remains less than 0.1 in magnitude. There is no indication of a more negative effect further out in time: the impact during the third year after treatment (quarters 8 through 11) is close to zero, albeit less precise. For wages, pre-treatment elasticities are centered around zero until about the first two years prior to treatment (quarters -8 through -5), at which point we detect a statistically significant elasticity of about 0.1 on employment. Positive pre-treatment elasticities for wages suggest that the synthetic control research design may not be as reliable for wage impacts—partly because wages for minimum wage increasing states are generally higher than

<sup>&</sup>lt;sup>13</sup>Specifically, we annualize actual treated state and synthetic control outcomes by taking the event-specific mean of these values at every pre- and post-treatment four-quarter interval. The percent difference between these values, divided by the actual minimum wage increase, forms the event-specific elasticity at each time interval. The figure displays the mean elasticity across events at each time interval. Performing the analogous calculation for the donors, we then construct event-time-specific percentile ranks, which we invert to calculate Hodges-Lehmann point estimates and 95% confidence intervals, where the latter use mean uniform cutoffs from Appendix Table A1 with the appropriate number events.

potential donor states, making it difficult to find a convex combination of donors to very closely match the treated units.<sup>14</sup> At the same time, we do find a sharp increase in teen wages at the time of and after the minimum wage increase. The Hodges-Lehmann point estimate for the teen wage elasticity lies between 0.2 and 0.4 in the post-treatment period. Approaching 0.40, the pooled wage elasticity is high after three years of treatment, but this is not inconsistent with the fact that nearly 38 percent of teens during the 1979-2013 period earned within 10 percent of the minimum wage.

Before exploring match quality and robustness issues, we take stock of our baseline estimates in Figure 4. The Figure shows all 29 individual employment elasticities (vertical axis) and wage elasticities, along with the mean and pooled effects. Overall, while the estimates appear noisy, there is very little relation between the magnitude of the wage elasticity and employment elasticity. In particular, the dotted line shows the locus of unitary elastic labor demand ( $\eta^{emp}/\eta^{wage} = -1$ ), where the wage effects of the minimum are completely offset by the employment effects, ignoring any changes in hours. Of the 29 treatment events, 19 lie clearly above this locus, as do the mean and pooled effects. The point estimates in the Figure seem inconsistent with the idea that negative employment effects are more likely when there is a more binding minimum wage: of the 10 events where the employment elasticity lies below the unit-elastic demand locus, in only one case (Oregon in 2003q1) do we see the wage estimates (or equivalently with wage estimate ranks below 0.5), the average employment elasticity moves from -0.058 to 0.031. This suggests sampling error and not more binding minimum wages underlie the spread in the employment elasticity—a conclusion confirmed in section **4.5** where we test for heterogeneous treatment effects.

## 4.3 Accounting for match quality

The extent to which a synthetic control matches the treatment unit in the pre-treatment period indicates how well it accounts for time-varying confounders. For a single case study, the pre-

<sup>&</sup>lt;sup>14</sup>The possibility that a treated unit characteristic might not belong to the convex hull of the donor characteristics is also discussed in Gobillon and Magnac (2015). The wage findings here are an empirical illustration of that possibility.

treatment match quality is usually apparent: for example, the synthetic control for New York in in Sabia et al. (2012) never coincides with the actual treated state. However, when pooling across many cases, it may be difficult to evaluate and account for match quality merely by inspection. Some of the the synthetic controls for the 29 treatment events in this paper also suffer from poor pre-treatment fit, but our pooling of estimates does not account for differences in match quality.

To assess this issue more systematically, we progressively exclude events with particularly poor pre-treatment fit and examine how this affects our post-treatment elasticities. For each treatment event, we calculate a pre-treatment *RMSPE* between the synthetic and actual treatment outcomes this is our measure of pre-treatment fit. We also calculate an estimated pre-treatment elasticity, defined just as our conventional treatment effect  $\eta_1$  except calculated over the pre-treatment period (and scaled by the actual minimum wage increase). Next, we trim our sample of case studies on pre-treatment fit and examine how the trimming affects the pooled pre-treatment and post-treatment elasticities.<sup>15</sup>

Figure 7 shows how pre- and post-treatment elasticities vary after trimming up to 11 events (about one-third of our sample). The top panel shows that the post-treatment Hodges-Lehmann point estimate remains relatively for both employment and wages as we progressively drop the worst matches. The same is true for the mean employment effect. One exception is the mean wage effect, which rises to 0.43 after removing 11 events with the worst match quality. We discuss how the mean wage effect is susceptible to three large elasticities (greater than 1.0) in the next section. In the bottom panel, pre-treatment elasticities for employment remain close to zero. For wages, as we eliminate events with the worst match quality, pre-treatment elasticities fall slightly toward zero, reducing the extent of bias. The pooled pre-treatment wage elasticity is always statistically significant at the 5 percent level, indicating that our research design has a detectable positive bias when it comes to wages. The size of pre-treatment elasticity, however, is very small, always less than 0.05.

<sup>&</sup>lt;sup>15</sup>Note that a reduction in the pre-treatment *RMSPE* can occur either from a reduced pre-treatment variance or a pre treatment bias. Therefore, an improved pre-treatment fit does not automatically guarantee a smaller pre-treatment elasticity, which is the measure of bias.

While the trimming of treatment events aims to improve the identification of the pooled treatment effect, there is also a concern that poor match quality for donor-based (placebo) synthetic controls biases our inference. In particular, donors whose synthetic controls have poor pre-treatment fit are not as informative for assessing the post-treatment rank of the treated state. In the context of a single treatment event, Abadie et al. (2010) address this concern by limiting inference to the subset of donors with better pre-treatment synthetic control fit relative to the treated state. Specifically, using the ratio  $\gamma_j = MSPE_j/MSPE_1$  of donor-to-treated synthetic control fit during the pre-treatment period, they limit randomization inference to subsets of donors with lower values of this ratio. Following this guidance, we explore how mean ranks and the associated confidence intervals change when we limit donors to those with event specific ratios  $\gamma_{ej} = MSPE_{ej}/MSPE_{e1}$  less than 20, 10, 5, and 2.

Table 7 presents the pooled effects from this exercise. Restricting donors has almost no effect on the mean rank or Hodges-Lehmann confidence intervals for the pooled employment elasticity, even when we limit the number of donors to those with *MSPE* ratios of less than 2, removing nearly one-quarter of donor states from the full sample. For wages, removing donors with the worst relative pre-treatment fit has removes some extreme donor elasticities: moving from the full sample to the subset of donors with a *MSPE* ratio of less than 20, the maximum donor of elasticity of 6.817 and kurtosis of 41.036 fall to 3.361 and 15.282, respectively. But as with employment, inference for wages remains relatively unchanged.

## 4.4 Robustness to window configuration length and predictor sets

Researchers using synthetic controls face choices about the exact length of pre- and post-treatment windows: more lengthy pre-treatment windows provide more pre-treatment predictor information but may also reduce the number of available treatment events. Similarly, synthetic control-based research designs require decisions about the exact set of predictor variables. In this section, we consider how the aggregated results change when modifying window configuration length and the predictor variable set.

We explore two issues using alternative configuration lengths. First, what happens to our estimates when we consider longer lagged effects? Second, we examine how our estimates vary when we only consider events with a longer pre-intervention period to fit the model. To consider lagged effects, Table 8 begins by showing employment effect estimates for the subsets of events with longer post-treatment periods. When we restrict the sample to those with at least 3 years of post-treatment data (12 quarters), the mean and Hodges-Lehmann point estimates are very close to zero (-0.001 and -0.019, respectively). While the estimate is somewhat less precise, we can still reject employment elasticities greater than -0.21 in magnitude at the five percent level. In short, although we cannot statistically rule out moderate sized estimates, the point estimates do not point to lagged effects through the third year of treatment. Table 8 also shows that our employment effect estimates are similar for events with longer pre-intervention periods. After requiring events to have longer pre-intervention windows, pooled employment elasticities are positive in sign, small in magnitude, and range from 0.007 to 0.040.

Table 8 reports suggestive evidence of lagged wage effects, as the pooled elasticity rises monotonically from 0.266, to 0.288, and then to 0.428, moving from the full sample to events to those with at least two and then at least three years of post-treatment data, respectively. Mean elasticities for these subsets seem rather high, and sometimes come close to the upper bound of the Hodges-Lehmann confidence intervals. These large elasticities are substantially influenced by three events with wage elasticities greater than 1.0 (MA 1986q3, ME 1985q1, NH 1987q1). The mean and pooled wage elasticity estimates are fairly stable up to requiring at least five or more years (20 quarters) of pre-intervention data. Then the wage estimates fall sharply to about 0.158 when requiring at least six years of pre-treatment data; and to 0.108 when requiring at least seven years of data. These requirements drop the aforementioned extreme elasticities and mechanically lower our pooled estimates. While the magnitude of the wage effect shifts depending on window configuration requirements, we find statistically significant teen wage effects of the minimum in all configurations except the most restrictive pre-treatment configuration of seven years, which reduces our sample to only eight events.

We additionally consider how alternative predictor sets affect pooled estimates of the teen employment and wage effects. Testing four candidate models, we found in Section 3.2 a weak preference for the most saturated model with annualized outcomes, including both annualized wage and employment outcomes and other labor market controls. This set of predictors provided all of the above estimates in this paper. Table 9 shows pooled estimates for all of these candidate models in columns 1 through 4. For both teen employment and teen wages, mean elasticities, ranks, and pooled elasticities change little across predictor sets. Hodges-Lehmann estimates for employment range from -0.003 to 0.073; for wages, the pooled elasticities lie between 0.265 and 0.294, all of which are statistically significant at the one percent level. With predictor set 4 (our preferred specification), confidence intervals are somewhat tighter in the case of employment.

#### 4.5 Heterogeneity

Thus far we have focused on the average effects of the treatment, and found employment estimates that are close to zero. However, it is possible that such an average effect is composed of causal effects of differing signs. For example, if the low wage labor market is characterized by monopsonistic competition, employment effects there could be positive in some cases and negative in others (Card and Krueger 1995, Burdett and Mortensen 1989, Manning 2003). Conversely, the spread in the estimated elasticities could simply be due to sampling error, with a true effect that is constant everywhere.

Here we take advantage of the fact that the distribution of the percentile ranks is of a known form under the sharp null hypothesis of a zero effect—it is uniformly distributed over the unit interval. If the distribution of empirically estimated percentile ranks differs sufficiently from the theoretical distribution, this constitutes evidence against the sharp null. This possibility can arise either from a non-zero constant effect everywhere, or heterogeneous effects across events.

We use the Kolmogorov-Smirnov test of equality of distributions to determine both the presence of any minimum wage effect and heterogeneous minimum wage effects. Under the sharp null of zero effects everywhere,  $\eta_e = 0$ , the percentile ranks of the nineteen treatment effects should be uniformly distributed. The empirical CDF of the actual percentile ranks is given by

$$\hat{H}(x) = \frac{1}{E} \sum_{e} I(p_{e1} \le x)$$

where *I* is the indicator function. The one-sample Kolmogorov-Smirnov test of the null hypothesis  $\hat{H}(x) = x$  has as its test statistic the maximum distance between the empirical CDF and the uniform CDF (see Gibbons and Chakraborti 2003):

$$D = \sup_{x} \left| \hat{H}(x) - x \right|.$$

The top panel of Figure 6 shows the uniform CDF and the empirical CDF for employment and wages. Visually, the percentile ranks of the employment effects are very similar to what would be expected under the sharp null, whereas the wage effects have a different percentile rank distribution. The Kolmogorov-Smirnov test p-values confirm this impression with p = 0.911 for employment and p = 0.000 for wage elasticity percentile ranks, leading us to reject the sharp null of zero effect only in case of wages.

The above test is against a sharp null of zero effect. To detect heterogeneous effects that average to something other than zero, we extend the procedure above to test for a constant effect equal to the mean effect:  $\eta_e = \overline{\eta}$ . This is particularly relevant for wage elasticities whose average is positive and substantial in magnitude. Under this sharp null, after centering the 29 elasticities around the mean effect, the adjusted percentile ranks  $\widetilde{p}_{e1} = \hat{F}_e(\eta_{e1} - \overline{\eta})$  should be uniformly distributed. The new Kolmogorov-Smirnov test statistic is

$$\widetilde{D} = \sup_{x} \left| \frac{1}{E} \sum_{e=1}^{E} I(\widetilde{p}_{e1} \le x) - x \right|.$$

The bottom panel of Figure 6 shows the distribution of adjusted percentile ranks for employment and wage elasticities after centering the effects around their means of -0.039 and 0.317, respectively. For employment, the Kolmogorov-Smirnov p-value is 0.5852; the re-calculated ranks appear to be

uniformly distributed, revealing no evidence of heterogeneous effects in our sample of treatment events. In contrast, we find evidence of some heterogeneity in the wage elasticities: the adjusted percentile ranks have more mass at the bottom of the distribution than would be expected from a uniform distribution. The Kolmogorov-Smirnov p-value is 0.055, meaning we can reject the null of a constant effect at the 10 percent level. This heterogeneity in the wage elasticities is consistent with there being variation in the bite of the minimum wage across different events.

The Kolmogorov-Smirnov test can be relatively insensitive to distributional differences near the tails, because there, by construction, the distributional deviations converge to zero (as the empirical distributions converge to 0 and 1). We may expect precisely this kind of heterogeneity if most minimum wage increases have small employment impacts, but a few sufficiently binding increases lead to large employment effects. As an alternative test of uniformly distributed ranks  $\tilde{p}_{e1}$ , we use the Anderson-Darling test statistic  $A^2$ , which places relatively more weight on the tails of the distribution (see Conover 1999):

$$A^{2} = -n - \sum_{e=1}^{E} \frac{2e-1}{E} \left( \log(\tilde{p}_{e1}) + \log(1 - \tilde{p}_{(E+1-e)1}) \right).$$

For completeness we perform this test both for heterogeneous effects (using the de-meaned percentile ranks  $\tilde{p}_{e1}$ ) and for a constant zero effect (using the original percentile ranks  $p_{e1}$ ). As shown in Figure 6, the resulting Anderson-Darling tests p-values are very similar to our previous tests, indicating no heterogeneity in the employment effect while providing some evidence for such heterogeneity in the case of wages.

In summary, we find that the minimum wage affects average teen wages somewhat heterogeneously across events, which is to be expected if the bite in the minimum wage differs across places. However, there is no indication of heterogeneous treatment effects for teen employment. For the events analyzed in this paper, the synthetic control-based estimates are consistent with sizable, positive and somewhat heterogeneous wage elasticities coupled with a small employment elasticity of the minimum wage that is not very different from zero.

# 5 Conclusion

The appeal of using a data-driven method to choose control groups has led to the increased popularity of the synthetic control method. Since there may be a multitude of case studies one can investigate, the ability to pool across events is useful in many contexts. In this paper we propose and implement and way to pool across synthetic control case studies. We use a variant of the rank sum test to conduct exact inference appropriate for small samples. We also invert the mean rank to provide the Hodges-Lehman confidence interval for the pooled effect.

Although constructing confidence intervals of estimates using permutation-based inference is relatively straightforward in the case of a single treatment event, estimates from individual case studies are often imprecise. Pooling across them allows one to draw economically meaningful inference with, in our case, 29 events. Our mean employment elasticity is -0.036, and with a 95 percent level of confidence, we reject teen employment elasticities more negative than -0.170. The Hodges-Lehmann pooled wage elasticity of 0.266 is statistically significant at the 1 percent level. Consistent with differential bite of the minimum wage in different areas, we find heterogeneity in the minimum wage elasticities for the average teen wage. However, such differences in bite do not explain a small employment effect. The employment effects do not covary with the wage effects, and the distribution of employment estimate ranks is consistent with a small (possibly zero) constant effect across events. We also do not find evidence of a more negative employment effect when considering outcomes up to three years after the implementation of the policy.

Within the minimum wage literature, our estimates are similar to those from border discontinuity designs and estimates controlling for time-varying heterogeneity. Dube et al. (2014) compare contiguous counties across state borders. Using QWI data between 2000 and 2011, they find a minimum wage elasticity of 0.26 for teen earnings and and elasticity of -0.06 for teen employment—which are very close to the estimates in this paper. Using state-level CPS data on teens for 1979-2014, Allegretto et al. (2015) find an elasticity of 0.253 for the average teen wage, and a small employment elasticities once spatial controls are included (0.006). While our confidence sets do not rule out a moderate negative employment effect of the minimum wage (e.g., an elasticity around -0.1), our

pooled estimates point to small teen employment effects and substantially larger effects on teen wages. Our results are broadly similar to those of Totty (2015), who contrasts the conventional two-way fixed effects estimates of minimum wage effects with estimates from the factor models proposed by Pesaran (2006) and Bai (2009). With CPS-ORG data for 1990-2013, Totty (2015) finds that three factor models produce small and statistically insignificant employment elasticities for teens, ranging from -0.065 to -0.036, but with statistically significant earnings elasticities ranging from 0.097 to 0.158.

Our estimates of the employment effects for teens do differ sharply from large, negative elasticities from the synthetic control-based analysis in Neumark et al. (2014). As discussed in section 1, their preferred employment elasticities for teens (about -0.14) are nevertheless based on a sample where there is a short, four-quarter pre-treatment period, where the potential donors receive treatment, and where the treated units receive additional minimum wage increases prior to the assigned treatment date. Allegretto et al. (2015) show that some of the treated events in the Neumark et al. (2014) sample experience sizable minimum wage increases, and some experience employment reductions—but typically they are not the same events.

A limitation of pooled synthetic control-based case studies concerns window length. Due to the nature of minimum wage variation in the United States, increasing the post-treatment window requirements limits the number of available case studies and potential donors. On average, we find no lagged employment effects even when we consider up to twelve quarters after the treatment, though focusing on these events cuts our sample in half. This result contrasts sharply with the significant and negative lagged effects of the minimum found by Meer and West (2015) for the overall private-sector workforce. To the extent that there are lagged effects, it is natural to expect them to be concentrated on groups who are more likely to be earning near the minimum wage, but we do not find such lagged effects for teens. During our study period of 1979-2013, teens were at least seven times more likely to earn within 10% of the minimum compared to workers aged 20 to 64. A similar conclusion is reached in Allegretto et al. (2015), who use parametric trends and geographic area controls, and find small employment effects for teens up to three years following a

minimum wage increase.

Finally, the method we propose for rank-based inference need not be applied only to synthetic control studies, but instead can be used in canonical or matched difference-in-difference settings more generally. Using rank-based exact inference is useful for assessing both mean effects, as well as heterogeneity in the treatment effects in such contexts, and is especially useful when the researcher is analyzing a small number of events.

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# Figures

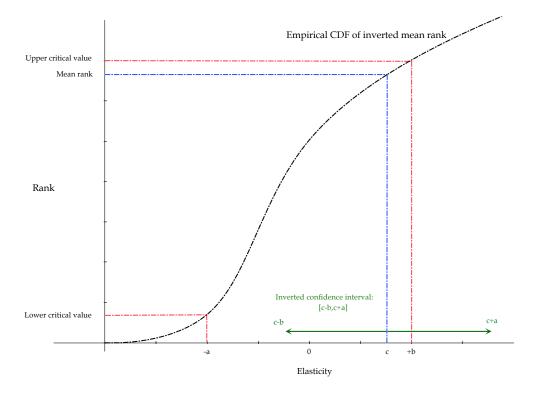


Figure 1: Forming confidence intervals by inverting the mean rank statistic

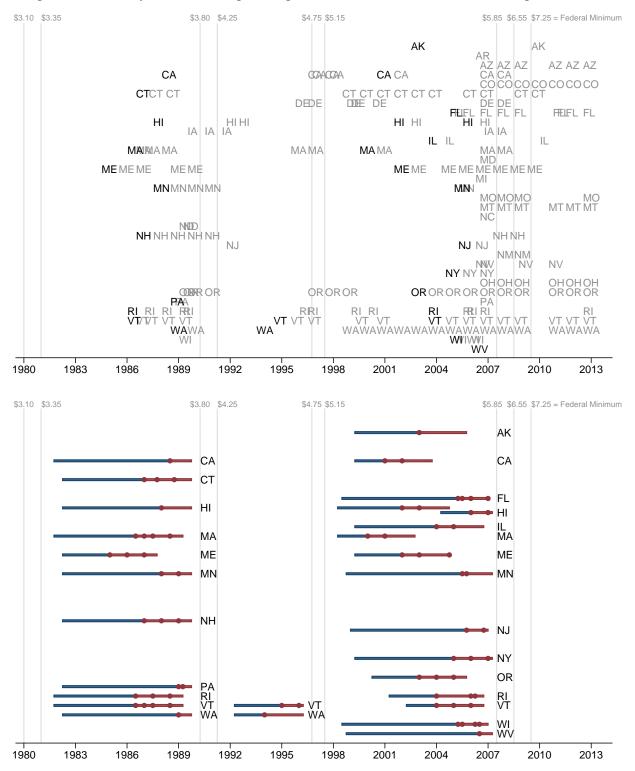


Figure 2: Quarterly minimum wage changes and usable treatment events during 1979-2013

*Notes:* The top panel displays all quarterly state-level minimum wage changes during the 1979-2013 period, with vertical lines representing the federal minimum wage changes, where bolded states indicate the first minimum wage rise of the 29 usable treatment events. The bottom panel shows the pre-treatment (blue) and post-treatment (red) windows of the 29 treatment events, with red circles showing the minimum wage increases during the post-treatment periods.

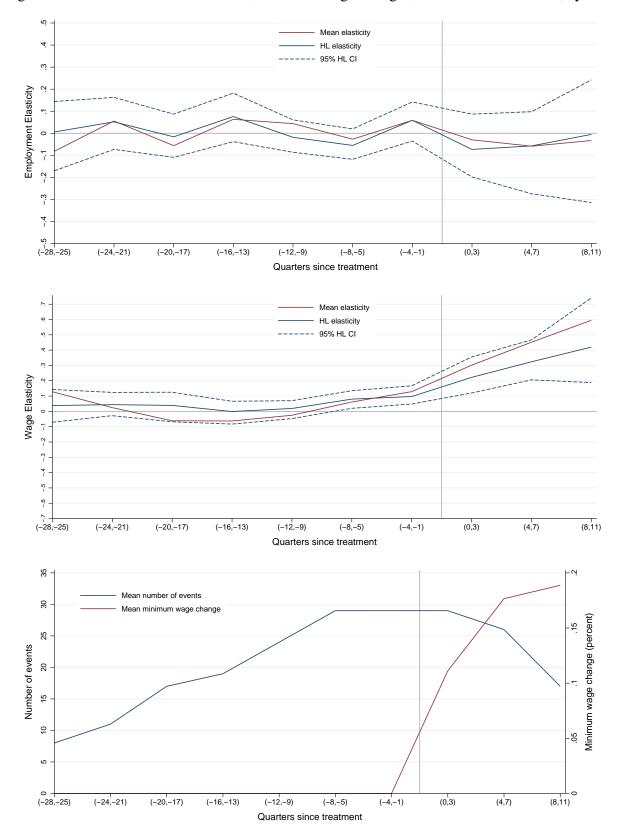


Figure 3: Mean annualized elasticities, minimum wage changes, and number of donors, by time

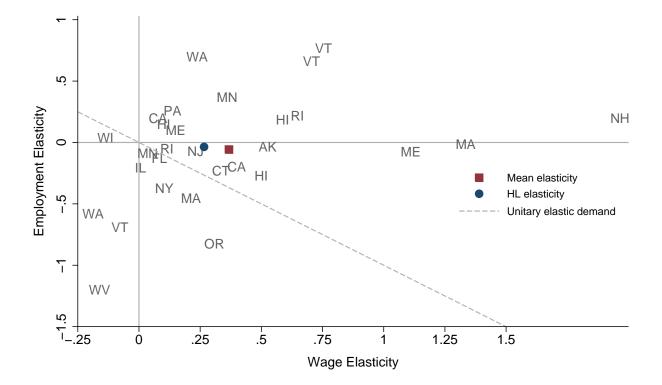


Figure 4: Event-specific and aggregated elasticities

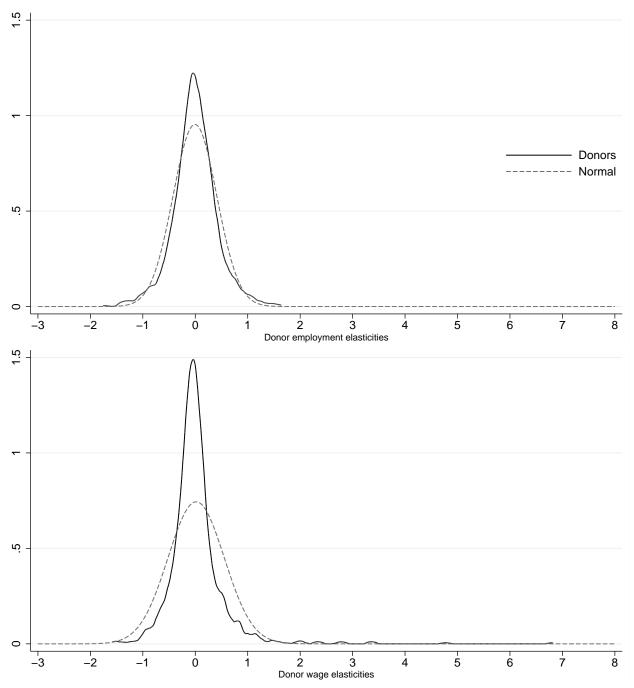


Figure 5: Probability density functions for the employment and wage elasticities of donors

*Notes:* The donor employment (wage) elasticity distributions have mean -0.012 (0.012), standard deviation 0.452 (0.565), and kurtosis 5.82 (58.37). For each outcome, the illustrated normal distributions have the same mean and variance. Shapiro-Wilk normality test p-values are 0.000 for both outcomes.

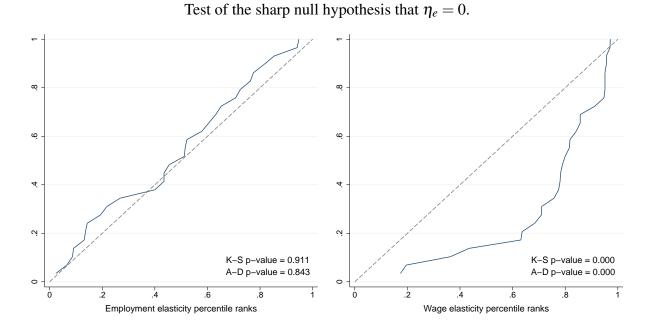
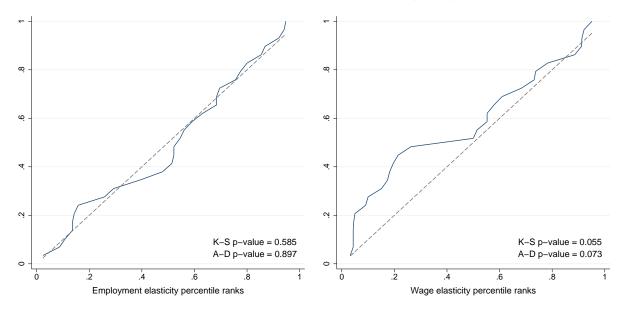


Figure 6: Cumulative distribution of estimated percentile ranks

Test of the sharp null hypothesis that  $\eta_e = \bar{\eta}$ .



*Notes:* The solid line is the cumulative distribution of percentile ranks of the 29 treatment effects, and the dashed line is the uniform CDF. P-values are for the Kolmogorov-Smirnov and Anderson-Darling tests of equality of these two distributions.

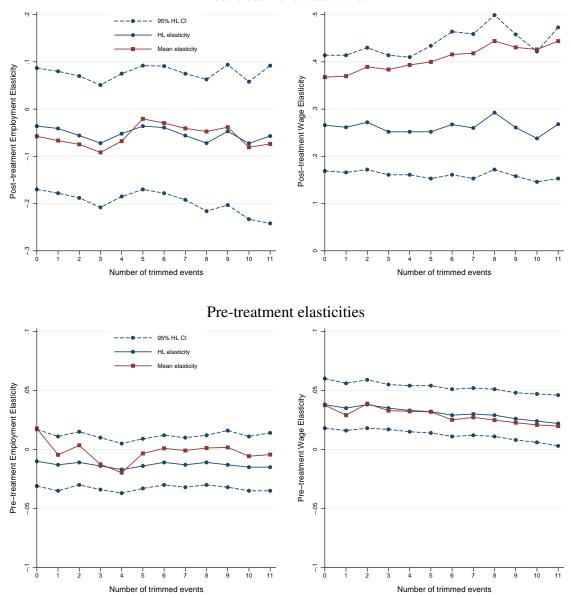


Figure 7: Employment and wage elasticities, trimming events on pre-treatment match quality Post-treatment elasticities

*Notes:* Mean and HL elasticities and confidence intervals re-calculated after successive trimming of N = 0, ..., 11 events with the highest pre-treatment RMSPE for the actually treated state.

### **Tables**

		Window	w length		MW in	creases
I	Event	Pre	Post	Donors	Number	Percent
AK	2003q1	16	12	33	1	0.265
CA	1988q3	28	6	36	1	0.269
CA	2001q1	8	12	39	2	0.174
CT	1987q1	20	12	36	3	0.269
FL	2005q2	28	8	21	4	0.295
HI	1988q1	24	8	36	1	0.149
HI	2002q1	16	12	38	2	0.190
HI	2006q1	8	6	21	2	0.160
IL	2004q1	20	12	29	2	0.262
MA	1986q3	20	12	39	4	0.119
MA	2000q1	8	12	40	2	0.286
ME	1985q1	12	12	44	3	0.090
ME	2002q1	12	12	38	3	0.233
MN	1988q1	24	8	36	2	0.149
MN	2005q3	28	8	20	2	0.194
NH	1987q1	20	12	36	3	0.090
NJ	2005q4	28	6	21	2	0.388
NY	2005q1	24	10	20	3	0.388
OR	2003q1	12	12	33	3	0.115
PA	1989q1	28	4	36	2	0.104
RI	1986q3	20	12	39	3	0.194
RI	2004q1	12	12	31	3	0.154
VT	1986q3	20	12	39	4	0.090
VT	1995q1	12	6	44	2	0.118
VT	2004q1	8	12	32	3	0.160
WA	1989q1	28	4	36	1	0.149
WA	1994q1	8	10	44	1	0.153
WI	2005q2	28	8	21	4	0.262
WV	2006q3	32	4	20	1	0.136

Table 1: Event description: window lengths, number of donors, and minimum wage increase

*Notes:* "Pre" and "Post" are the respective pre-treatment and post-treatment window lengths. Percent minimum wage increase is the percent increase from the pre-treatment minimum to the maximum post-treatment minimum wage.

Minimu	m Window			Num	ber of d	onors	Perce	nt MW c	hange
Pre-	Post-	Events	Treated states	Min.	Mean	Max.	Min.	Mean	Max.
8	4	29	19	20	33.0	44	0.090	0.193	0.388
8	8	22	16	20	33.8	44	0.090	0.195	0.388
8	12	15	11	29	36.4	44	0.090	0.179	0.286
16	4	19	17	20	31.2	39	0.090	0.209	0.388
16	8	14	12	20	31.6	39	0.090	0.208	0.388
16	12	8	8	29	36.1	39	0.090	0.185	0.269
24	4	11	10	20	27.5	36	0.104	0.226	0.388
24	8	6	5	20	25.7	36	0.149	0.240	0.388
32	4	1	1	20	20.0	20	0.136	0.136	0.136

Table 2: Summary of treatment events for more restrictive window configurations

*Notes:* Each row describes the subset of all 29 events in Table 1 with at least the specified number of preand post-treatment quarters.

	(1)	(2)	(3)	(4)
		Emplo	oyment	
Pre-treatment	0.0311	0.0401	0.0372	0.0342
Post-treatment	0.0477	0.0510	0.0493	0.0466
		Wa	age	
Pre-treatment	0.7022	0.7743	0.7563	0.7336
Post-treatment	0.7973	0.7872	0.7878	0.7735
Predictors				
Quarterly outcomes	Y			
Annualized outcomes		Y	Y	Y
Both annualized outcomes			Y	Y
Industry & Other controls				Y

Table 3: Average pre- and post-treatment RMSPE for donors, by model specification

*Notes:* The average RMSPE is the square root of the mean of all donors' MSPEs across all treatment events, for either the pre- or post-treatment period. Predictor categories are either all quarterly pre-treatment outcomes (Quarterly), annualized pre-treatment outcomes, both annualized employment and wage pre-treatment outcomes, or pre-treatment means of industry shares and demographic/labor market variables.

	Weights	per donor	
Donor relation to treatment	Inside	Outside	Relative weight
		Employment	
Same region	0.052	0.026	1.993
Same division	0.087	0.028	3.127
Within 0 - 500 miles	0.054	0.027	2.004
Within 0 - 1000 miles	0.037	0.026	1.393
		Wage	
Same region	0.048	0.027	1.788
Same division	0.068	0.029	2.375
Within 0 - 500 miles	0.048	0.028	1.739
Within 0 - 1000 miles	0.037	0.026	1.399

#### Table 4: Donor weights and distance to treated states

*Notes:* The inside (outside) weight per donor is equal to the sum across all treatment events of the weights assigned to donors inside (outside) the specified area, divided by the total number of inside (outside) donors. Relative weight is the ratio of inside-to-outside weights per donor. Distance in miles is the distance between population-weighted state centroids.

			Employn	nent		Wage	S
E	Event	Elasticity	Rank	90% CI	Elasticity	Rank	90% CI
AK	2003q1	-0.035	0.400	(-0.387, 0.319)	0.533	0.971*	( 0.339, 0.882)
CA	1988q3	0.198	0.763	(-0.355, 0.526)	0.083	0.711	(-1.615, 0.594)
CA	2001q1	-0.200	0.268	(-0.768, 0.398)	0.405	0.951*	( 0.053, 0.678)
СТ	1987q1	-0.229	0.132	(-0.695, 0.211)	0.342	0.816	(-0.576, 0.871)
FL	2005q2	-0.129	0.435	(-0.637, 0.381)	0.095	0.783	(-0.119, 0.310)
HI	1988q1	0.185	0.579	(-0.811, 0.758)	0.602	0.842	(-1.736, 1.172)
HI	2002q1	0.149	0.775	(-0.415, 0.705)	0.117	0.775	(-0.305, 0.395)
HI	2006q1	-0.272	0.217	(-1.107, 0.715)	0.515	0.913	(-0.595, 0.991)
IL	2004q1	-0.208	0.194	(-0.522, 0.271)	0.027	0.710	(-0.406, 0.312)
MA	1986q3	-0.015	0.512	(-1.149, 0.998)	1.337	0.951*	( 0.394, 2.060)
MA	2000q1	-0.456	0.024*	(-0.834,-0.157)	0.215	0.857	(-0.164, 0.505)
ME	1985q1	-0.078	0.522	(-1.230, 1.044)	1.113	0.957*	( 0.184, 2.062)
ME	2002q1	0.097	0.725	(-0.271, 0.544)	0.152	0.800	(-0.119, 0.355)
MN	1988q1	0.369	0.816	(-0.627, 0.942)	0.361	0.789	(-1.978, 0.930)
MN	2005q3	-0.089	0.455	(-0.762, 0.750)	0.036	0.636	(-0.328, 0.577)
NH	1987q1	0.197	0.605	(-1.198, 1.517)	1.969	0.947	(-0.784, 3.555)
NJ	2005q4	-0.071	0.435	(-0.414, 0.315)	0.241	0.957*	( 0.101, 0.444)
NY	2005q1	-0.375	0.136	(-0.781, 0.057)	0.109	0.818	(-0.055, 0.252)
OR	2003q1	-0.827	0.143	(-1.544, 0.200)	0.310	0.857	(-0.227, 1.189)
PA	1989q1	0.257	0.632	(-1.113, 1.368)	0.144	0.632	(-6.674, 1.578)
RI	1986q3	0.218	0.707	(-0.479, 0.842)	0.663	0.951*	( 0.083, 1.108)
RI	2004q1	-0.051	0.515	(-0.727, 0.679)	0.130	0.758	(-0.399, 0.777)
VT	1986q3	0.769	0.854	(-0.742, 2.120)	0.762	0.780	(-0.496, 1.726)
VT	1995q1	-0.689	0.087	(-1.310, 0.216)	-0.070	0.435	(-1.262, 0.693)
VT	2004q1	0.661	0.941	(-0.105, 1.363)	0.713	0.971*	( 0.221, 1.433)
WA	1989q1	0.698	0.947	(-0.261, 1.476)	0.237	0.684	(-4.536, 1.241)
WA	1994q1	-0.580	0.065	(-1.393, 0.022)	-0.188	0.196	(-0.792, 0.211)
WI	2005q2	0.038	0.652	(-0.533, 0.613)	-0.127	0.174	(-0.367, 0.116)
WV	2006q3	-1.199	0.091	(-2.207, 0.166)	-0.162	0.364	(-1.118, 0.811)

Table 5: Employment and wage elasticities, by event

*Notes:* \* indicates significance at the 10% level using the percentile rank of the elasticity within the event-specific donor-based placebo distribution. Inverting this rank obtains 90% CIs.

				Hodge	s-Lehmann
	Median elasticity	Mean elasticity	Mean rank	Elasticity	95% CI
Employment	-0.051	-0.058	0.470	-0.036	(-0.170, 0.087)
Wages	0.237	0.368	0.758***	0.266	( 0.169, 0.414)

#### Table 6: Employment and wage elasticities, pooled

*Notes:* Critical values for the mean percentile rank are derived from the mean of 29 uniform distributions. \* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01.

	Donor	states	D	onor sta	te elastic	cities	Treated st	tate elasticities
MSPE Ratio	Number	Fraction	Min	Max	SD	Kurtosis	Mean rank	95% CI
				Employ	vment			
	958	1.000	-1.756	1.640	0.418	4.613	0.470	(-0.170, 0.087)
20	958	1.000	-1.756	1.640	0.418	4.613	0.470	(-0.170, 0.087)
10	950	0.992	-1.756	1.640	0.419	4.608	0.469	(-0.172, 0.087)
5	893	0.932	-1.756	1.640	0.418	4.643	0.470	(-0.175, 0.088)
2	727	0.759	-1.756	1.640	0.428	4.729	0.489	(-0.170, 0.104)
				Wag	es			
	958	1.000	-1.586	6.817	0.536	41.036	0.758***	( 0.169, 0.414)
20	904	0.944	-1.586	3.351	0.408	12.102	0.770***	( 0.176, 0.428)
10	879	0.918	-1.586	3.351	0.406	12.433	0.773***	( 0.174, 0.430)
5	835	0.872	-1.586	3.351	0.398	13.530	0.771***	( 0.172, 0.425)
2	677	0.707	-1.522	3.351	0.398	15.282	0.752***	( 0.162, 0.426)

Table 7: Employment and wage confidence intervals, by pre-treatment donor MSPE ratios

*Notes:* Rows show results for samples where donors limited to those with donor-to-treated MSPE ratios less than X, where X=. indicates the full sample.

\* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01.

Windo	ow length				Hodges	s-Lehmann
Pre-	Post-	Events	Mean elasticity	Mean rank	Elasticity	95% CI
			Ei	nployment		
	4	29	-0.058	0.470	-0.036	(-0.170, 0.087)
	6	26	-0.055	0.460	-0.046	(-0.179, 0.070)
	8	22	-0.027	0.475	-0.039	(-0.182, 0.105)
	10	17	-0.057	0.442	-0.099	(-0.261, 0.105)
	12	15	-0.001	0.488	-0.019	(-0.205, 0.160)
8		29	-0.058	0.470	-0.036	(-0.170, 0.087)
12		24	-0.034	0.505	0.007	(-0.134, 0.122)
16		19	0.038	0.533	0.035	(-0.109, 0.172)
20		17	0.036	0.526	0.032	(-0.128, 0.184)
24		11	-0.011	0.540	0.035	(-0.140, 0.221)
28		8	-0.037	0.551	0.040	(-0.161, 0.280)
				Wages		
	4	29	0.368	0.758***	0.266	( 0.169, 0.414)
	6	26	0.402	0.781***	0.272	( 0.174, 0.430)
	8	22	0.440	0.786***	0.288	( 0.170, 0.489)
	10	17	0.512	0.827***	0.354	( 0.198, 0.554)
	12	15	0.586	0.870***	0.428	( 0.252, 0.633)
8		29	0.368	0.758***	0.266	( 0.169, 0.414)
12		24	0.375	0.754***	0.240	( 0.142, 0.408)
16		19	0.388	0.752***	0.252	( 0.125, 0.458)
20		17	0.395	0.738***	0.227	( 0.104, 0.473)
24		11	0.147	0.672**	0.158	( 0.001, 0.310)
28		8	0.068	0.617	0.108	(-0.091, 0.271)

Table 8: Employment and wage elasticities, by minimal window length

*Notes:* Window length of X restricts the events to the subset with a pre- or post-period greater than X quarters, where X = . is eight pre-treatment or four post-treatment quarters. Critical values for the mean percentile rank are derived from the mean of appropriate number of uniform distributions.

\* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01.

	(1)	(2)	(3)	(4)
		Emple	oyment	
Mean elasticity	-0.019	0.001	0.037	-0.058
Mean rank	0.499	0.506	0.537	0.470
HL elasticity	-0.001	0.011	0.053	-0.036
HL 95% CI	(-0.148, 0.143)	(-0.163, 0.157)	(-0.096, 0.191)	(-0.170, 0.087)
		Wa	ige	
Mean elasticity	0.358	0.448	0.434	0.368
Mean rank	0.760***	0.781***	0.790***	0.758***
HL elasticity	0.280	0.297	0.314	0.266
HL 95% CI	( 0.183, 0.413)	( 0.199, 0.446)	( 0.213, 0.471)	( 0.169, 0.414)
Predictors				
Quarterly outcomes	Y			
Annualized outcomes		Y	Y	Y
Both annualized outcomes			Y	Y
Industry & Other controls				Y

Table 9: Employment and wage elasticities, by alternative predictor sets

*Notes:* Predictor categories are either all quarterly pre-treatment outcomes (Quarterly), annualized pre-treatment outcomes, both annualized employment and wage pre-treatment outcomes, or pre-treatment means of industry shares and demographic/labor market variables.

\* p < 0.1, \*\* p < 0.05, \*\*\* p < 0.01.

### **Appendix: alternative methods of inference**

The results presented thus far assume that under the sharp null of zero treatment effects, the mean percentile rank is distributed as the mean of independent uniform distributions. There are two potential problems with this assumption. First, because some of our events contain as few as 20 donors, the mean percentile rank might be too discrete to be assumed to be distributed uniformly. The second and potentially more serious problem is that because some of our events occur at the same calendar time, they may share some of the same donor observations. This overlap in donors means that the estimated ranks from two events may be correlated, violating the assumption that the ranks are independent across events. Moreover, recurring treatments within the same state may also lead to serial correlation in the ranks across time.

In this section, we compare our primary rank-based inferential procedure with two alternative rank-based methods of conducting inference on the pooled Hodges-Lehmann employment elasticity that address the two issues raised above. For each of these three methods, we estimate the Hodges-Lehman confidence interval. We then consider a fourth method of inference: instead of using rank-based methods to estimate the Hodges-Lehmann confidence interval, we construct a randomization inference based confidence interval for the mean effect using means of donor elasticities. These four methods provide researchers a toolkit of possibilities for conducting inference with synthetic controls with multiple events. First we describe how we construct three rank-based counterfactual distributions used to test the sharp null  $\eta_{e1} = 0$  for all *N* events, along with randomization inference using the mean elasticity. Then we discuss the results using these four methods.

The first approach is the baseline one used throughout this paper, which assumes that the percentile ranks  $p_{e1}$  of these elasticities *vis-à-vis* the donor states are distributed continuously as independent uniform variables on [0,1]. We use one million simulations of the mean of *N* uniforms to calculate the 95% critical values for this Irwin-Hall distribution. Table A1 lists these critical values for N = 1...30. These are the preferred critical values for the mean percentile rank used throughout the paper. For the full sample of 29 events, the 5% critical values of this distribution are 0.395 and 0.605.

The second method recognizes that in practice the percentile ranks are calculated for a finite, event-specific number  $N_e$  of donor states. For this second method, we relax the assumption of continuous approximation, and calculate percentile ranks with the Weibull-Gumbel rule  $p_e = r_e/(N_e + 1)$  by simulating the uniform integer ranks  $r_e \in [1, N_e]$  with the appropriate number of donor states present in our data. The distribution of the mean of these percentile ranks across 29 treatment events forms the counterfactual of the mean percentile rank.

The third method further relaxes the assumption that the ranks are independently distributed. The set of placebo elasticities is not independently distributed because some treatments occur around the same time period. For example, the five states that raise their minimum wages during 2005 share many of the same donors. Therefore, these treatments are associated with similar donor elasticities, inducing a correlation in donor ranks across this set of events. To form the distribution of mean percentile ranks under the null hypothesis accounting for donor overlap, we use a computationally intensive randomization inference procedure. We permute state identifiers across the sample of 50 states and merge the treatment events to the shuffled sample of states. In this merged dataset, the "treatment" status is a randomly generated placebo with a mean zero effect on outcomes. However, the resulting dataset shares the exact timing and structure of donor overlap in our actual sample of 29 events, as well as the actual sample's event-specific pre- and post-treatment window configurations. The dataset also retains the same structure of recurring treatments, and hence accounts for serial correlation in the synthetic control estimates over time within a state. For each event, and for each "treated" and donor state, we calculate the percentile ranks of the placebo-treatment effects, defined as the post-treatment percent difference of employment-to-population ratios between the state and its synthetic control. Finally, we calculate the mean percentile rank of the 29 "treated" states. We iterate these one million times to estimate the distribution of average ranks under the null using this rank-based randomization inference. Note that although the placebo-law sample contains actually treated states, the resulting distribution remains a valid counterfactual because all states have the same probability of treatment assignment, before permuting state identifiers.

Table A2 describes all three methods of rank-based inference associated with our sample's 29

treatment events. The first column of results lists the 2.5 and 97.5 percentiles of each counterfactual distribution. These 95% critical values are very similar across methods. For example, with the third method which uses randomization inference on the rank to fully account for donor overlap, the cutoffs are (0.388,0.611). These are very close to the cutoffs using the first (baseline) method of (0.395, 0.605) from the Irwin-Hall distribution. In the second column, we calculate the 5% rejection rates for each counterfactual distribution using the 95% critical values of Irwin-Hall distribution. By construction, this is exactly 5.0% for the first method using Irwin-Hall distribution. For the second method, the rejection rate is similar but slightly lower, at about 4.3%. Finally, for the third method accounting for overlap using rank-based randomization inference, the rejection rate (when using the Irwin-Hall cutoffs) rises to about 6.6%, suggesting that donor overlap leads to a slight tendency to over-reject the null when using method 1, although the bias in the size of the test is very small.

To see how these methods affect estimates of the confidence intervals of the aggregate effects, columns 3-5 show the Hodges-Lehmann point estimate and associated confidence intervals. Here, we form confidence intervals as described in Section 2.3 by inverting the mean rank, but we use the critical values from the respective distributions for each method. The 95% Hodges-Lehman elasticity confidence of (-0.170, 0.087) with the first method remains essentially unchanged when using the critical values accounting for the discreteness of the ranks. Using the critical values based on the rank-based randomization inference accounting for donor overlap, the 95% confidence interval slightly widens to (-0.178, 0.094). The over-statement in precision due to ignoring overlap therefore appears to be very small in terms of Hodges-Lehmann confidence intervals: about 0.01 in elasticity space. These results validate the choice of using the simpler and computationally less costly Irwin-Hall distribution for conducting statistical inference.

In the fourth row of Table A2 we compare the above results using the Hodges-Lehmann pooled effect and rank-based inference to randomization inference for the mean effect. To form randomization-based confidence intervals around the mean employment elasticity estimate of -0.058, we first construct the counterfactual distribution of the mean of 29 donor elasticities: we select, at random, one donor from each of the treatment events, and calculate the mean of the synthetic

control-based elasticities. Repeating this process one million times, we use the resulting 2.5 and 97.5 percentiles of this distribution to calculate the 95% randomization inference confidence interval. For the mean effect of -0.058, the 95% randomization confidence interval is (-0.197, 0.100). This is somewhat wider than than our preferred Hodges-Lehman confidence interval (-0.170, 0.087). This is likely because the randomization inference confidence interval for the mean, based on means of donor elasticities, is somewhat more influenced by large outlier elasticities among donors.

## **Appendix Tables**

			Perce	entile		
Ν	0.5	2.5	5.0	95.0	97.5	99.5
1	0.005	0.025	0.050	0.950	0.975	0.995
2	0.050	0.111	0.158	0.842	0.888	0.950
3	0.103	0.176	0.223	0.777	0.823	0.896
4	0.147	0.220	0.261	0.738	0.780	0.852
5	0.182	0.249	0.287	0.713	0.751	0.819
6	0.206	0.271	0.305	0.694	0.729	0.793
7	0.227	0.288	0.320	0.680	0.712	0.774
8	0.244	0.301	0.332	0.668	0.699	0.757
9	0.258	0.312	0.341	0.658	0.687	0.743
10	0.269	0.322	0.350	0.650	0.678	0.731
11	0.280	0.330	0.357	0.643	0.670	0.720
12	0.289	0.337	0.363	0.637	0.663	0.711
13	0.297	0.344	0.368	0.632	0.656	0.703
14	0.304	0.349	0.373	0.627	0.651	0.696
15	0.311	0.354	0.377	0.623	0.646	0.689
16	0.317	0.359	0.381	0.619	0.641	0.683
17	0.322	0.363	0.385	0.615	0.637	0.679
18	0.327	0.367	0.388	0.612	0.633	0.673
19	0.331	0.370	0.391	0.609	0.630	0.669
20	0.335	0.374	0.394	0.606	0.626	0.665
21	0.339	0.377	0.396	0.604	0.623	0.660
22	0.343	0.379	0.398	0.601	0.620	0.657
23	0.346	0.382	0.401	0.599	0.618	0.654
24	0.349	0.384	0.403	0.597	0.615	0.650
25	0.352	0.387	0.405	0.595	0.613	0.647
26	0.355	0.389	0.407	0.593	0.611	0.645
27	0.358	0.391	0.408	0.591	0.609	0.642
28	0.360	0.393	0.410	0.590	0.607	0.639
29	0.363	0.395	0.412	0.588	0.605	0.637
30	0.365	0.397	0.413	0.587	0.603	0.635

Table A1: Extrema of the distribution of mean of N uniformly distributed random variables

*Notes:* Simulated using one million iterations of the mean of N uniformly distributed variables on [0, 1].

	Rank-based inference	inference	Aggregat	Aggregated employment elasticity	lasticity
	95% crit. values 5% rej. rate	5% rej. rate	Type	Point estimate	95% CI
Method 1: Rank, uniform iid.	(0.395, 0.605)	0.050	Hodges-Lehmann	-0.036	(-0.170, 0.087)
Method 2: Rank, discrete iid.	(0.398, 0.601)	0.043	Hodges-Lehmann	-0.036	(-0.164, 0.080)
Method 3: Rank, rand. inference	(0.388, 0.611)	0.066	Hodges-Lehmann	-0.036	(-0.178, 0.094)
Method 4: Elasticity, rand. inference	I	ı	Mean	-0.058	(-0.197, 0.100)
<i>Notes:</i> The baseline method 1 assumes mean rank is distributed as the mean of 29 uniform variables on [0,1]. Method 2 calculates the rank as the mean of 29 percentile ranks using the Weibull-Gumbel percentile rank calculation with the appropriate number of donor states for each event. Method 3 further relaxes the assumption that the ranks are independent across events by accounting for the donor overlap across events. In particular, method 3 uses a randomization inference procedure that permutes state identifiers randomly, and then estimates the distribution of	an rank is distributed /eibull-Gumbel percer hat the ranks are indo inference procedure of	l as the mean of ntile rank calcula ependent across that permutes str	assumes mean rank is distributed as the mean of 29 uniform variables on [0,1]. Method 2 calculates the rank as using the Weibull-Gumbel percentile rank calculation with the appropriate number of donor states for each event. ssumption that the ranks are independent across events by accounting for the donor overlap across events. In domization inference procedure that permutes state identifiers randomly, and then estimates the distribution of	n [0,1]. Method 2 c te number of donor for the donor over y, and then estimat	alculates the rank as states for each event. In across events. In es the distribution of

Table A2: Alternative methods of inference for employment elasticity

mean ranks or the effect of the placebo laws. The details for the simulation are described in the text. Method 4 conducts randomization interence using the mean effect (elasticity) as opposed to the mean rank; this method uses the mean of 29 donor employment elasticities, choosing one donor per event, for 1 million iterations. Rejection rates for each method are shown when using the critical values from method 1.