

# A Structural Approach to Dynamic Energy Pricing and Consumer Welfare

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# Motivation

## Dynamic Pricing

- Increasing availability in US over past 5 years
- Well studied: many RCTs estimate average treatment response
- Few studies of welfare effects

## Identification Problems:

- Low price variation during off-peak hours
  - Hausman, Kinnucan, McFadden (1979) - A Two-Level Electricity Demand Model
- Average Welfare with unobserved heterogeneity
  - Hausman and Newey (2016) - Individual Heterogeneity and Average Welfare

# Motivation

## Contribution

- High Frequency Household consumption data from RCT
- Methodology for causal analysis using ML to generate counterfactuals, matches
- Policy analysis of specific dynamic rate that was adopted by Utility

## Findings

- High variation in price elasticity of demand throughout day
- In this experiment, consumer welfare gain during off-peak hours exceeds consumer welfare loss for all but the highest peak prices

## Rate Structure

### **Dynamic Price** - Treated Group

- Price per KW during off-peak hours is constant: \$0.045
  - Off-Peak Hours: 12 a.m. - 2 p.m., 7 p.m. - 12 a.m.
- Price per KW during peak hours for all treated households is chosen by Utility each day:  
\$0.045, \$0.113, \$0.23, \$0.46
  - Peak Hours: 2 - 7 p.m.

### **Standard Block Rate** - Control Group

- Constant price per KW each day
  - Price per KW: \$0.083 for the first 1400 KW used in a month
  - \$0.096 per KW for additional usage

# Experiment

## Consumption Data

- Consumption observed in 15 minute increments for 2010, 2011
- Household Behavior observed in 2010 was before households enrolled in Experiment
  - Control Households experience no change in technology or price
  - Treated Households exposed to new technology and new price
  - Treated Households' behavior observed under both policies

	2010		2011
Control	Standard Rate	→	Standard Rate
Treatment	Standard Rate	→	Dynamic Rate

**2,146,464 observations of hourly household consumption**

# Identification Strategy

## Difference in Difference

- Ideally we could regress quantity on observed price, controlling for weather to account for endogenous price setting decision
- Identification problem: only one price observed during off-peak hours (\$0.045/KWH)
- Can simulate behavior of treated households in 2011 using pretreatment data from 2010

$$\left[ \begin{array}{l|l} W_0^{10} : 2010 \text{ Control Households} & W_0^{11} : 2011 \text{ Control Households} \\ \hline Y_0^{10} : 2011 \text{ Treated Households} & Y_1^{11} : 2011 \text{ Treated Households} \end{array} \right]$$

**Identification strategy follows from simulating  $\widehat{Y}_0^{11}$**

# Counterfactuals - Lasso Prediction

see Burlig, Knittle, Rapson, Reguant, and Wolfram 2018

- 1 Model consumption in 2010 as a function of observed variables in 2010
- 2 Use penalized regression (Lasso, Ridge, Elastic Net) to select model with best fit for 2010 data
- 3 Predict consumption in 2011 by using observations of variables in 2011 in function with parameters chosen in (2)

## Variable Pool

- Temperature
- Humidity
- Dewpoint
- Previous Day Cooling Degrees
- Average consumption among similar households
- Month and Day-of-week fixed effects

# Counterfactuals - Vertical Regression + Lasso

see Athey, Bayati, Doudchenko, Imbens, and Khosravi 2018

- 1 Consider  $J$  control units and  $K = 2$  treated units  $Y_{N-1}, Y_N$ :

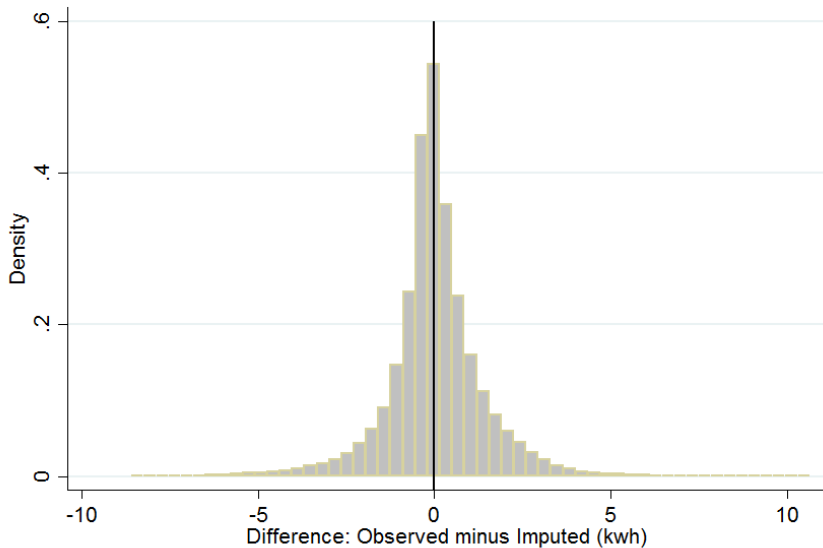
Pre Treatment		Post Treatment	
$Y_{1,1}$	$Y_{1,2}$	$Y_{1,3}$	$Y_{1,4}$
$\dots$	$\dots$	$\dots$	$\dots$
$Y_{J,1}$	$Y_{J,2}$	$Y_{J,3}$	$Y_{J,4}$
$Y_{N-1,1}$	$Y_{N-1,2}$	?	?
$Y_{N,1}$	$Y_{N,2}$	?	?

- 2 Use shrinkage estimator to select from among many possible control households  $J$  as covariates
- 3 Impute counterfactual untreated behavior behavior of  $Y_{N-1}, Y_N$  during treated periods:

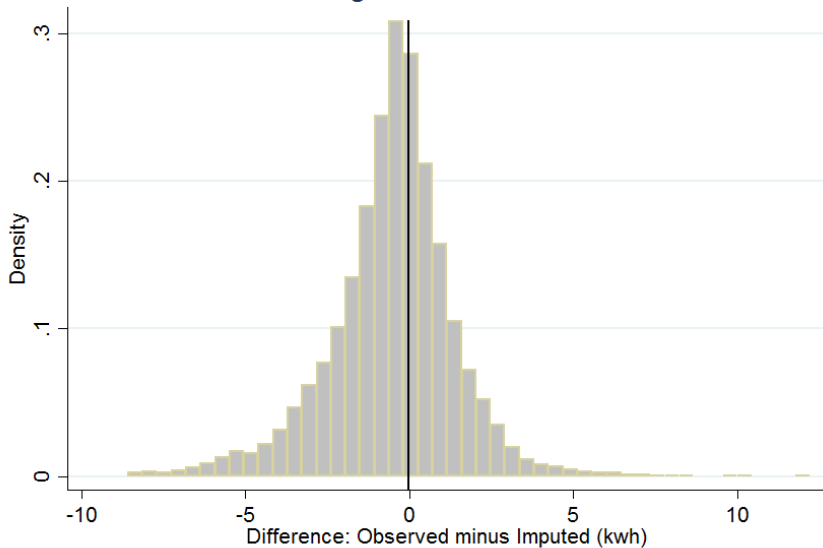
$$\hat{Y}_{N,t} = \hat{\beta}_0 + \sum_{i=1}^N \hat{\beta}_i Y_{i,t}$$



## Low Price Periods



## High Price Periods



## Constant Elasticity Specification

$$\ln(Q_{i,h}^{2011}) = \ln(a) + \gamma \ln(p_h) + \sum_{j=-1}^{j=+1} \delta_j \ln(T_j) + \varepsilon_{i,h} \quad (1)$$

- Constant Elasticity specification allows one-step estimation of price elasticity conditional on temperature
- Temperature Control accounts for omitted variable bias stemming from correlation between high price and high consumption on hottest days of summer.

# Computing Consumer Surplus

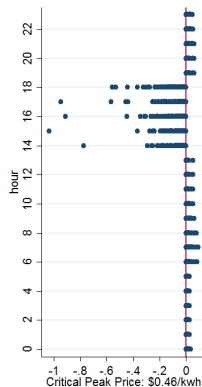
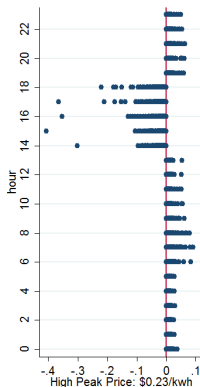
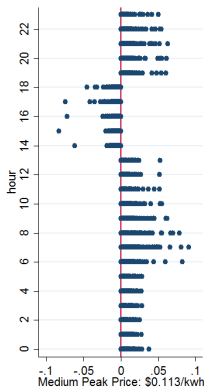
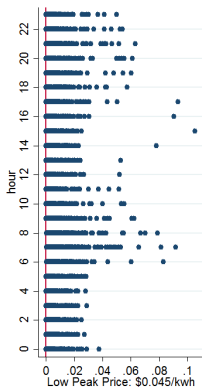
## Analytic Solution

$$\Delta CS_h = a * T_{h-1}^{\hat{\delta}_{1,h}} * T_h^{\hat{\delta}_{2,h}} * T_{h+1}^{\hat{\delta}_{3,h}} * \frac{[p_2^{1+\hat{\gamma}_h} - p_1^{1+\hat{\gamma}_h}]}{1 + \hat{\gamma}_h} \quad (2)$$

- Consumer Surplus increases in off-peak hours where price falls from control rate \$0.083 to off-peak price \$0.045
- Consumer Surplus decreases in on-peak hours where price rises to either \$0.113, \$0.23, or \$0.46

# Estimation: Consumer Surplus

## Hourly Change in Consumer Surplus



# Estimation: Consumer Surplus

## Average Household Effects

- Off-peak price more than compensates for consumer surplus loss on days with medium and high peak prices
- Critical price days are net reductions in consumer surplus
- In 2011, with 23 low, 30 medium, 22 high, and 12 critical price days, average change in consumer surplus is \$4.63 per household

	Daily Change in Consumer Surplus	Peak Hours Only	Off-Peak Hours Only	Average Ratio Peak:Off-Peak
Low Peak Price	\$0.15	0.0269	0.1234	-
Medium Peak Price	\$0.10	-0.0218	0.1239	-0.1759
High Peak Price	\$0.01	-0.1106	0.1240	-0.9064
Critical Peak Price	-\$0.17	-0.2964	0.1241	-2.4844

# Conclusions

## Methodology

- ML forecasts trained on pretreatment data forecast counterfactual (untreated) behavior
- Counterfactual predictions identify household specific price elasticity of demand
- Identification strategy evades problems with unobserved individual heterogeneity

## Policy

- Household consumer surplus effects are small but positive
- Utility could have offered a less drastic discount without reducing consumer welfare