# The Impact of Adverse Selection on Misallocation of Capital and Finance 

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## Motivation

- Anecdotally, asym info is important financial friction which leads to misallocation but hard to quantify
- This paper focuses on asym info about firm's persistent productivity between informed borrower (firm) and uninformed creditors (bondholders)
- How large welfare loss created by asym info in corporate bond markets?


## Two Ways to Alleviate Asym Info:

## Debt Structure: International comparison

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1. Reputation building in corporate bond markets
2. Debt substitution of costly monitored lending (e.g., bank loan)

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## Two Ways to Alleviate Asym Info:

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## Debt Structure:

- Corporate bonds (~70\%)
- reputation building (Diamond 91)
$\checkmark$ dynamic learning (Bayesian updating of assessment) about firm's productivity from public info (e.g., financial disclosure)
- Bank loans ( $\sim 30 \%$ )
- costly monitored lending (Diamond 84)
$\checkmark$ cost-advantage in collecting private info


## Research Question

How much asym info about firm's productivity affects financing, investment, aggregate productivity, and consumer welfare?

## Empirical Challenge:

## Approach:

## Research Question

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## Empirical Challenge:

1. Full info set and investor's assessment about firm's productivity are unobservable for researcher
2. Assessment and financing are endogenous

## Approach:

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## Approach:

- Estimates corporate financing model under dynamic adverse selection (screening + signaling problems) consistent with data facts Data Facts
- defaultable debts with heterogeneous firms (Hennessy and Whited 07)
- integrates screening + signaling problems about firm's productivity (Chatterjee, Corbae, Dempsey, and Rios-Rull 20 for unsecured consumer credit market)


## Summary

- Estimation: back out size of transitory "noise" to firm's choice from variance of leverage and probability of default
- Mechanism:
- Counterfactual:
- Future Application: debt maturity; stock issue and buyback; and relationship banking


## Summary

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- Mechanism:

1. Cross-subsidization low (high) productivity firm overissues (underissues) corporate bonds and overinvests (underinvests) in capital compared to full info $\rightarrow$ capital misallocation ( $\downarrow$ aggregate productivity)
2. Signaling leverage and equity send positive signal to uninformed lenders $\rightarrow$ good reputation lowers interest rates of corporate bonds

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- Counterfactual:

1. symmetric info about firm's productivity
$\checkmark$ info improves aggregate productivity (TFP) $\uparrow 29 \mathrm{bps}$ and increases consumption $\uparrow 1.4 \%$
$\checkmark$ bank debt / total debt $21 \% \xrightarrow{\downarrow .6 \% \text { points }} 15 \%$
2. taxation of debt forgiveness restores efficient allocation without changing info structure.

- Future Application: debt maturity; stock issue and buyback; and relationship banking


## Thank You

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## Selected Literature Review

1. Dynamic Adverse Selection in Unsecured Consumer Credit Markets

Chatterjee, Corbae, Dempsey, and Rios-Rull 20 (hereafter CCDR).
2. Defaultable Bank Loan Markets

Heterogeneous Firm: Cooley and Quadrini 01; Hennessy and Whited 07; Corbae and D'Erasmo 20.
3. Defaultable Corporate Bond and Bank Loan Markets

Theory: Diamond 91; Rajan 92. Macromodel: De Fiore and Uhlig 15. Heterogeneous Firm: Crouzet 17; Xiao 19. Borrowing Constraint: Lian and Ma 20.
4. Dynamic Corporate Financing Model Under Asym Info Discrete Time: Hennessy, Livdan, and Miranda 10. Continuous Time: Morellec and Schurhoff 11.
5. Capital Misallocation and Financial Friction

Gilchrist, Sim, and Zakrajšek 13; Whited and Zhao 20.

Contribution to Literature: this paper introduces dynamic learning in unmonitored corporate bonds and substitution for monitored bank loans in unified quantitative model

# Roadmap 

Introduction

Model

Equilibrium

## Estimation/Validation

Counterfactual

Conclusion

# Roadmap 

## Introduction

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## Environment

## Basics:

- Time is discrete, infinite horizon, annual frequency
- Agents: (i) firm managers; (ii) financial intermediaries; and (iii) representative household
- Discrete choice model: amounts of debt and equity on discrete grids of points


## Technology in Production:

- Production: $\exp (z) k^{\alpha_{k}}, \alpha_{k} \in(0,1)$ with fixed costs $f$, measured in units of output
- where firm specific productivity $z \in\left\{z_{L}, z_{H}\right\}$ follows symmetric 2-state Markov process
- and capital $k$
- Price of capital is 1
- Capital depreciates by rate $\delta$


## Environment (Cont'd)

## Preference:

- Manager and financial intermediaries are risk-neutral
- No aggregate shocks $\rightarrow$ households risk aversion does not affect pricing
- Manager effectively receives per-period utility from

```
\underbracec
    shareholdings
```

- Preference shocks are unobservable
- Two types of preference shocks $\left(\varepsilon, \varepsilon_{\Delta}\right)$ Timing: 2 Sub-periods Timing: Diagram

1. $\varepsilon$ adds noise to balance sheet choice (debt outstanding $b$, debt type $\phi$, next period equity $e^{\prime}$ ) where $\phi= \begin{cases}M & \text { for corporate bonds (Market debt) } \\ B & \text { for bank loans (Bank debt) }\end{cases}$
2. $\varepsilon_{\Delta}$ adds noise to bankruptcy choice

## Preference Shocks

capture unobserved factors affecting firm's choice

- Discrete choice + preference shocks drawn from GEV dist $\rightarrow$ closed form solution (McFadden 73; Rust 87) Recursive Problem Conditional Value Function Simple Model
- Preference shocks help

1. computation by smoothing value function
2. to eliminate off-the-equilibrium beliefs (=assessment of firm's productivity)
3. to slow down dynamic learning about firm's productivity $z$

- Transitory preference shocks $\left(\varepsilon, \varepsilon_{\Delta}\right)$ hinder inference of persistent productivity $z$
- Micro-foundation to shocks: rational inattention (Matejka and Mckay 15)
- info-processing to investigate payouts is costly (e.g., communication costs in board meeting)


## Agents, Firm's Choice, and Flow of Funds

State Variable
(productivity, equity, assessment of firm's productivity)

## Firm Manager

## Bondholders

Bank Lenders

Households (Shareholders)

## Agents, Firm's Choice, and Flow of Funds



## Bondholders

Bank Lenders

Households (Shareholders)

## Agents, Firm's Choice, and Flow of Funds

Equity Market Role of Bank Loan



## Agents, Firm's Choice, and Flow of Funds

Equity Market Role of Bank Loan



## Agents, Firm's Choice, and Flow of Funds

Equity Market<br>Role of Bank Loan



## Technologies in Bank Loans and Corporate Bonds

Creditors (i.e., banks and bondholders) offer debt contract contingent on publicly observable characteristics (e.g., size of debt, leverage, assessment about firm's productivity)

1. Asym info about persistent productivity $z$
2. Financial intermediation costs
3. Recovery at default (Ch. 11 reorganization)

Corporate bond recovery at default depends on privately informed productivity z

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## 1. Asym info about persistent productivity $z$

- monitoring is only available for banks
- banks can charge different interest rates among firm's productivity $z$

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2. Financial intermediation costs

- costs of banks $\mu_{B}>$ costs of bondholders $\mu_{M}$
$\checkmark$ e.g., monitoring costs, compliance costs, regulatory burdens

3. Recovery at default (Ch. 11 reorganization)

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3. Recovery at default (Ch. 11 reorganization)

- dispersed bondholders fail to coordinate Bankruptcy
- cash-flow based debt in corporate bonds
- asset based debt in bank loans
- Lian and Ma 20 and EBITDA-multiple approach in practice

Corporate bond recovery at default depends on privately informed productivity z

# Roadmap 

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## Evolution of Assessment of Firm's Productivity

follows Bayesian updating

1. Bondholders observe firm's state (equity (e), and assessment of firm's productivity (s)) and choice (size of borrowing (b), equity ( $e^{\prime}$ ), debt type $(\phi)$, and bankruptcy $(\Delta)$ )
2. Bondholders Bayesian updates assessment of firm's productivity in next period ( $s^{\prime}$ ) given (i) public info $\left\{e, s, b, \phi, e^{\prime}, \Delta\right\}$ and (ii) equilibrium policy functions How Firm Uses Reputation?

Corporate bond credit spreads depend on expectation of probability of default and recovery using probability weights ( $\sim$ assessment of firm's productivity) Corporate Eond Pricing

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## Data and Parameters

- Data for estimation: Compustat
- 12 parameters are selected outside model More
- intermediation costs $\mu_{B}-\mu_{M}=170$ bps (Schwert 20)
- Estimated 5 parameters $\left\{\alpha, \alpha_{\Delta}, f, f_{c 11}, \lambda_{1}\right\}$ to U.S. data via Simulated Method of Moments

More

- $\operatorname{var}($ debt to assets) and overall bankruptcy rates are informative to estimate variance of preference shocks $\left\{\alpha, \alpha_{\Delta}\right\}$
- $f_{c 11}$ targets fraction of Ch. 11
- Linear external financing costs $\lambda_{1}=0.09$ is close to estimate in Hennessy and Whited 07
- Model is consistent with bank debt ratio, debt-to-EBITDA, spreads, PD, recovery rates, credit ratings in data Targeted and Untargeted (Credit Losses) Other Validations


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## Info about Productivity Improves Efficiency

- Productivity z: private info (benchmark) $\rightarrow$ public info (counterfactual) - i.e., $q_{M}\left(\omega_{M}\right) \rightarrow q_{M}\left(\omega_{M}, z\right)$ where $\omega_{M}$ is observable firm characteristics - preference, technology, and parameters are unchanged

|  | Consumption | TFP | Aggregate <br> bank debt ratio |
| :--- | ---: | ---: | ---: |
| Change (\%) | 1.35 | 0.29 | -26.52 |

- Measured TFP and consumption increase, and less demand for bank loans in counterfactual Olley and Pakes Decomposition and $\operatorname{Var}(\mathrm{mpk})$
- Private info induces low (high) type to overinvest (underinvest) $\rightarrow$ misallocation of capital

- Simpler model delivers different quantitative results Atterative Model


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## Taxation of Cancellation of Debt (COD) Income

## Policy Recommendation:

- Taxation of debt forgiveness improves welfare without changing info structure
- Current US law exempts tax of COD in bankruptcy
- COD=debt outstanding (b) - reduced debt repayment at default $\geq 0$
- other things being equal, $\operatorname{COD}\left(z_{L}\right)>\operatorname{COD}\left(z_{H}\right)$ since $z_{L}<z_{H}$



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## Takeaways

## What I Do:

- I develop quantitative model of reputation building


## Main Mechanism:



Policy Recommendation:
Taxation of Debt Forgiveness

## Debt Structure: International Comparison



Reference: Becker and Josephson (2016). Debt outstanding of publicly traded debt in 37 countries (including US, UK, and Japan) by region in 2010.

## Data Facts

1. Corporate bonds consist for $70 \%$ of non-financial corporate debt in US
2. Average firm issues corporate bonds is highly levered
3. Annual bankruptcy rates is $0.9 \%$

- Ch. 11 reorganization is $0.7 \%$ and Ch .7 liquidation is $0.1 \%$

4. Corporate bond recovery rates at default are highly dispersed
5. CFOs think credit ratings - expected Probability of Default (PD) - is one of most important determinant of debt financing

Source: Compustat, Graham and Harvey 10, Moody's, Flow of Funds.

## Preference Shocks Affect Learning

No Shock $\alpha \rightarrow \infty$



- Simple static model in Modigliani-Miller: firm solves optimal borrowing $b$ given internal finance $e$
- Optimal capital: $k\left(z_{L}\right)<k\left(z_{H}\right) \rightarrow b(e, z)=k(z)-e$ if $k(z)<e$


## Preference Shocks Affect Learning

Small Shocks

$$
\alpha=4
$$



- Plotting pdf
- 5-95 percentile, 10-90 percentile, and 25-75 percentile
- modal choice (black solid lines)


## Preference Shocks Affect Learning

## Small Shocks

$$
\alpha=4
$$




- Suppose I do not know firm's type and observe firm's choice (blue dots)
- Try to guess firm's type


## Preference Shocks Affect Learning

## Small Shocks

$$
\alpha=4
$$




- Most likely to be $z_{H}$ ( $\sim$ Bayesian inference) $\uparrow \operatorname{Pr}\left(z_{H}\right)$
- Small preference shocks create small noise $\rightarrow$ inference is easier


## Preference Shocks Affect Learning

Large Shocks

$$
\alpha=1
$$




- Large preference shocks create large noise
- Inference is harder and depends on prior $\uparrow$ or $\downarrow \operatorname{Pr}\left(z_{H}\right)$
- bondholders cannot distinguish whether action comes from $z$ or preference shocks


## Chapter 11 Reorganization

- Efficiency of liquidation of assets $s_{c 11}$
- Debt repayment reflects coordination:

1. (weak) bondholders receive cash flow $\max \left\{\exp (z) k^{\alpha_{k}}-f+s_{c 11}(1-\delta) k-f_{c 11}, 0\right\}$
2. (strong) bank lenders receive liquidation value from take-it-or-leave-it offer (Crouzet 17; Xiao 19)

## Chapter 7 Liquidation

- Efficiency of liquidation of assets $s_{c 7}$
- Debt repayment:
- all type of debtors receive liquidation value $s_{C 7} k$


## Bankruptcy by Size

## Small Firm Files Ch. 7

| Size Percentile | Probability of Bankruptcy |  |  |  | Fraction of Ch. 7 <br> (\%) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ch. 11 (\%) |  | Ch. 7 (\%) |  |  |  |
|  | $z_{L}$ | $z_{H}$ | $z_{L}$ | $z_{H}$ | $z_{L}$ | $z_{H}$ |
| Panel A: Internal Finance |  |  |  |  |  |  |
| <25\% | 1.11 | 2.20 | 0.57 | 0.00 | 33.83 | 0.00 |
| 25\%-50\% | 0.89 | 0.72 | 0.12 | 0.00 | 12.31 | 0.00 |
| 50-75\% | 0.68 | 0.26 | 0.01 | 0.00 | 1.12 | 0.00 |
| $>75 \%$ | 0.45 | 0.15 | 0.00 | 0.00 | 1.00 | 0.00 |
| Panel B: Total Assets |  |  |  |  |  |  |
| <25\% | 0.65 | 0.51 | 0.56 | 0.00 | 46.61 | 0.00 |
| 25\%-50\% | 1.21 | 0.83 | 0.01 | 0.00 | 0.73 | 0.00 |
| 50-75\% | 0.93 | 0.65 | 0.00 | 0.00 | 0.49 | 0.00 |
| >75\% | 2.25 | 0.41 | 0.00 | 0.00 | 0.00 | 0.00 |

## Birth and Death

## Exiting

- Exogenous exiting at rate $\eta$ with depreciation rate of value $1-\chi$


## Entry

- Entrants start from smallest internal finance
- Productivity is randomly drew from stationary distribution
- No track record (Diamond 89)


## Timing: 2 Sub-periods

1. Balance sheet choice stage:

- preference shocks $\varepsilon_{b, \phi, e^{\prime}}$ of scale parameter $\alpha$
- debt outstanding $b$; debt type $\phi \in\{\mathrm{M}($ artketdebt $), \mathrm{B}($ ankdebt $)\}$; next period internal finance $e^{\prime}$

2. Bankruptcy choice stage:

- preference shocks $\varepsilon_{\Delta}$ of scale parameter $\alpha_{\Delta}$
- bankruptcy $\Delta \in\{0$ (no bankruptcy), 1 (bankruptcy) $\}$
- choose bankruptcy chapters
- debt settlement, exit, and entry
- Bayesian learning of $s^{\prime}$ from public info $\left(b, \phi, e^{\prime} \Delta\right)$


# Timing: Diagram 



## Timing: Diagram



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## Timing: Diagram



## Recursive Problem Ream

## Dynamic Discrete Choice Model

- Manager maximizes lifetime utility:

$$
\begin{aligned}
W(e, z, s) & =\mathbb{E}_{\varepsilon_{b, \phi, e^{\prime}}}\left[\max _{b, \phi \in\{M, B\}, e^{\prime}} V+\varepsilon_{b, \phi, e^{\prime}}\right] \\
V & =\mathbb{E}_{\varepsilon_{\Delta}}\left[\max _{\hat{\Delta} \in\{0,1\}} v_{\hat{\Delta}}+\varepsilon_{\hat{\Delta}}\right]
\end{aligned}
$$

where $v_{\Delta=1}=\max \left\{v_{c 11}, v_{c 7}\right\}$

- $v_{\Delta}$ is value function at bankruptcy choice stage conditional on $\left\{e, z, s, b, \phi, e^{\prime}\right\}$
- Internal finance $e$ and debt outstanding $b$ lie on discrete grids
- Action specific preference shocks $\left\{\varepsilon_{b, \phi, e^{\prime}}, \varepsilon_{\Delta}\right\}$ are drawn from GEV distribution with scale parameters $\left\{\alpha, \alpha_{\Delta}\right\}$


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- Manager maximizes lifetime utility:

$$
\begin{aligned}
W(e, z, s) & =\frac{1}{\alpha} \ln \left(\sum_{b, \phi \in\{M, B\}, e^{\prime}} \exp (\alpha V)\right) \\
V & =\frac{1}{\alpha_{\Delta}} \ln \left(\sum_{\hat{\Delta} \in\{0,1\}} \exp \left(\alpha_{\Delta} v_{\hat{\Delta}}\right)\right)
\end{aligned}
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- Action specific preference shocks $\left\{\varepsilon_{b, \phi, e^{\prime}}, \varepsilon_{\Delta}\right\}$ are drawn from GEV distribution with scale parameters $\left\{\alpha, \alpha_{\Delta}\right\}$
- Closed form solution (McFadden 73; Rust 87)


## Value Function at Bankruptcy Choice Stage

Nonbankruptcy

$$
v_{\Delta=0}=\text { equity payout }- \text { external costs }+ \text { continuation value }
$$

Ch. 11

$$
v_{c 11}=\text { equity payout }- \text { external costs }+ \text { continuation value }
$$

Ch. 7

$$
v_{C 7}=\text { equity payout }- \text { external costs }
$$

## Value Function at Bankruptcy Choice Stage

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$$
\begin{align*}
v_{\Delta=0} & =\text { equity payout }- \text { external costs }+ \text { continuation value } \\
\text { equity payout } & =\exp (z) k^{\alpha_{k}}-f+(1-\delta) k-\operatorname{debt} \text { repayment }-e^{\prime} \tag{1}
\end{align*}
$$

Ch. 11

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v_{c 11} & =\text { equity payout }- \text { external costs }+ \text { continuation value } \\
\text { equity payout } & =\exp (z) k^{\alpha_{k}}-f+s_{c 11}(1-\delta) k-f_{c 11}-\text { debt repayment }-e^{\prime} \tag{2}
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$$

Ch. 7

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v_{c 7} & =\text { equity payout }- \text { external costs } \\
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\end{align*}
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Ch. 7

$$
\begin{align*}
v_{c 7} & =\text { equity payout }- \text { external costs } \\
\text { equity payout } & =s_{c 7} k-\text { debt repayment } \tag{3}
\end{align*}
$$

- Continuation value consists expectation of future $W\left(e^{\prime}, z^{\prime}, s^{\prime}\right)$ over $z^{\prime}$ and $s^{\prime}$


## Manager's Problem in Recursive Formula Ream

## Simple Model - Only Corporate Bonds, No Ch. 7, Zero Equity Issuance Costs

- Type score $s=\operatorname{Pr}\left(z=z_{H}\right)$

$$
\begin{aligned}
W(e, z, s) & =\mathbb{E}_{\varepsilon_{b, \phi, e^{\prime}}}[\max _{b, e^{\prime}} \mathbb{E}_{\varepsilon_{\Delta}}[\max _{\Delta} v_{\hat{\Delta}}+\underbrace{\varepsilon_{\hat{\Delta}}}_{\text {pereference shocks }}]+\underbrace{\varepsilon_{b, \phi, e^{\prime}}}_{\text {preference shocks }}] \\
\Pi_{\Delta=0} & =e^{z}(b+e)^{\alpha_{k}}+(1-\delta)(b+e) \\
\Pi_{\Delta=1} & =e^{z}(b+e)^{\alpha_{k}}+s_{c 11}(1-\delta)(b+e)-f_{c 11} \\
v_{\Delta=0} & =\Pi_{\Delta=0}-q_{M}^{-1} b-e^{\prime}+q \sum_{z^{\prime}, s^{\prime}} g_{z} g_{s} W\left(e^{\prime}, z^{\prime}, s^{\prime}\right) \\
v_{\Delta=1} & =\Pi_{\Delta=1}-\underbrace{\min \left\{q_{M}^{-1} b, \max \left\{\Pi_{\Delta=1}, 0\right\}\right\}}_{\text {debt repayment under Ch. } 11}-e^{\prime}+q \sum_{z^{\prime}, s^{\prime}} g_{z} g_{s} W\left(e^{\prime}, z^{\prime}, s^{\prime}\right)
\end{aligned}
$$

$s_{c 11}$ : liquidation efficiency (Ch. 11), $f_{c 11}$ : fixed costs for Ch. $11, q_{M}$ : market debt price, $q$ : discount factor, $g_{z}$ : transition prob of $z$, $g_{s}$ : transition prob of type score

- $g_{s}$ follows Bayes' rule given (i) public info and (ii) equilibrium policy functions


## Bankruptcy

## Chapter 7 Liquidation (Endogenous Exiting)

- Business terminates
- Liquidation value of assets $s_{c 7} k$


## Chapter 11 Reorganization

- Business continues (value depreciates by $\pi$ )
- Reduce debt burden
- borrower uses liquidation threat under Ch. 7 (take-it-or-leave-it offer) to bank lender
- corporate bond recovery at default depends on cash flow
- Liquidation value of assets $s_{c 11} k$
- Fixed costs $f_{c 11} \rightarrow$ small firm files Ch. 7


## Financial Frictions in Equity Markets

- Equity issuance is very costly in data
- Linear costs of equity financing $\lambda_{1}$ (Gomes 01)
- financial frictions in reduced form


## (Quantitative) Role of Bank Loan Markets

- Debt substitution mitigates reputation building
- Allows model estimation and validation (not every firms in Compustat universe issue corporate bonds in data)


## Theory

## Existence

## Theorem:

- There exists a stationary recursive competitive equilibrium

Sketch of proof: preference shocks eliminate off-the-equilibrium beliefs (CCDR 20)

## Consistency of Firm Distribution and Assessment of Firm's Productivity

## Proposition:

- Stationary cross-sectional firm distribution satisfies:


fraction of high producitvity firm from stationary dist.

Sketch of proof: mathematical induction + rational agents such that (i) entrant's belief is consistent with ergodic distribution; (ii) belief updating is Bayesian where $\Gamma$ : firm distribution

Return

## Parameters

| Description | Notation | Value | S.E. | Target/Reference |
| :--- | :--- | :---: | :--- | :--- |
| Panel A: Parameters Calibrated | Outside the Model |  |  |  |
| Capital elasticity of profits | $\alpha_{k}$ | 0.650 |  | Standard setting |
| Depreciation rate | $\delta$ | 0.150 |  | Standard setting |
| Persistency of productivity | $\rho$ | 0.700 |  | İmrohoroglu and Tïzel (2014) |
| Std. dev. of productivity shock | $\sigma$ | 0.270 |  | İmrohoroglu and Tüzel (2014) |
| Risk-free rate | $r_{f}$ | 0.040 |  | T-Bill rate |
| Exogenous exiting rate | $\eta$ | 0.008 |  | Exiting rate |
| Market intermediation costs | $\mu_{M}$ | 0.006 |  | AAA Corporate bond spread |
| Bank intermediation costs | $\mu_{B}-\mu_{M}$ | 0.017 |  | Schwert (2020) |
| Liquidation efficiency (exiting) | $\chi$ | 0.500 |  | Crouzet (2017) |
| Liquidation efficiency (Ch. 7) | $s_{c 7}$ | 0.380 |  | Bris et al. (2006) |
| Reorganization efficiency | $s_{c 11}$ | 0.869 |  | Bris et al. (2006) |
| Loss of continuation value | $\pi$ | 0.300 |  | Lang and Stulz (1992) |
| Panel B: Parameters Estimated Inside the Model |  |  |  |  |
| Extreme value scale parameter | $\alpha$ | 2.251 | $(0.300)$ | Variance of debt to assets |
| Extreme value scale parameter | $\alpha_{\Delta}$ | 0.102 | $(0.015)$ | Bankruptcy rate (Ch. 11+Ch. 7) |
| Fixed costs for production | $f$ | 4.099 | $(0.298)$ | Equity issuance/assets |
| Fixed costs for Ch. 11 | $f_{c 11}$ | 28.698 | $(4.468)$ | Bankruptcy rate (Ch. 11) |
| Linear external financing costs | $\lambda_{1}$ | 0.092 | $(0.021)$ | Variance of dividends to assets |

## Model Matches (Targeted and Untargeted) Moments

| Description | Model | Data | Source |
| :--- | :---: | :---: | :--- |
| Panel A: Target Moments |  |  |  |
| $\quad$ Bankruptcy prob. (Ch. 11) (\%) | 0.72 | 0.72 | Compustat |
| Bankruptcy prob. (Ch. 7) (\%) | 0.14 | 0.14 | Compustat |
| Variance of debt-to-assets | 0.06 | 0.07 | Compustat |
| Variance of dividends/total assets | 0.01 | 0.02 | Compustat |
| $\quad$ Equity issuance /total assets | 0.15 | 0.16 | Compustat |
| Panel B: Untarget Moments (Financial Ratios) |  |  |  |

- Model does a good job matching targeted moments


## Model Matches (Targeted and Untargeted) Moments

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| Variance of dividends/total assets | 0.01 | 0.02 | Compustat |
| Equity issuance /total assets | 0.15 | 0.16 | Compustat |
| Panel B: Untarget Moments (Financial Ratios) |  |  |  |
| Debt-to-assets | 0.39 | 0.24 | Compustat |
| Bank debt ratio | 0.33 | $[0.28,0.43]$ | CM (2018) |
| Aggregate bank debt ratio | 0.21 | 0.31 | Flow of Funds |
| Debt-to-EBITDA | 2.45 | 1.77 | Compustat |
| Dividends/total assets | 0.09 | 0.03 | Compustat |
| Spreads (Non-bankrupt) (bps) | 174 | n.a. | n.a. |
| Spreads (Ch. 11) (bps) | 378 | n.a. | n.a. |
| Spreads (Ch. 7) (bps) | 227 | n.a. | n.a. |
| Spreads of bank debt (bps) | 269 | $[251,301]$ | Strahan (1999) |

- Model does a good job matching targeted moments
- Model does a good job matching untargeted moments:
- bank debt ratio (intermediation costs $\left.\mu_{B}-\mu_{M}\right)$
- debt-to-EBITDA (fixed costs $f$ )
- spreads of bank debt (intermediation costs $\mu_{M}$ )

Note: CM (2018) refers to Crouzet and Mehrotra (2018).
Return

## Model Captures (Untargeted) Credit Losses

|  | Market Dobt | Bank Debl |  | Split sample into bond and loan dependent firms |
| :---: | :---: | :---: | :---: | :---: |
| Descripion | Model Data | Model Din | Source |  |
| Panel A: Leverage | $0.42 \quad 0.39$ | 0.32 | Compusat | ond issuers are highly leveraged - intermediation costs |

Panel C: Recovery Rates

## Panel D: Expected Recovery Rates

## Model Captures (Untargeted) Credit Losses

| Description | Market Debt |  | Bank Debt |  | Source | Split sample into bond and loan dependent firms |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Model | Data | Model | Data |  |  |
| Panel A: Leverage |  |  |  |  |  | - Bond issuers are highly leveraged |
| Debt-to-assets | 0.42 | 0.39 | 0.32 | 0.21 | Compustat | - intermediation costs |
| Panel B: Bankrupty Probabilities |  |  |  |  |  |  |
| Chapter 11 Reorganization (\%) | 0.76 | ${ }^{0.61}$ | 0.64 | ${ }_{0}^{0.74}$ | Compustat | - Bank dependent firm files more Ch. 7 |
| Chapter 7 Liquidation (\%) Fraction of Chapter 11 | ${ }_{0} 0.08$ | 0.08 | 0.25 0.72 | ${ }_{0}^{0.15}$ | ${ }_{\text {Compustat }}^{\text {Compustat }}$ | bankruptcy |
| Fraction of Chapter 11 Panel C: Recovery Rates | 0.90 | 0.88 | 0.72 | 0.83 | Compustat | bankruptcy |

[^0]Note: AK (2014) compute summary statistics from Moody's Ultimate Recovery Database. AK(2014) refers to Altman and Kalotay (2014)

## Model Captures (Untargeted) Credit Losses

| Description | Market Debt |  | Bank Debt |  | Source |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Model | Data | Model | Data |  |
| Panel A: Leverage |  |  |  |  |  |
| Debt-to-assets | 0.42 | 0.39 | 0.32 | 0.21 | Compustat |
| Panel B: Bankruptcy Probabilities |  |  |  |  |  |
| Chapter 11 Reorganization (\%) | 0.76 | 0.61 | 0.64 | 0.74 | Compustat |
| Chapter 7 Liquidation (\%) | 0.08 | 0.08 | 0.25 | 0.15 | Compustat |
| Fraction of Chapter 11 | 0.90 | 0.88 | 0.72 | 0.83 | Compustat |
| Panel C: Recovery Rates |  |  |  |  |  |
| Mean | 0.32 | 0.45 | 0.64 | 0.75 | AK (2014) |
| Standard deviation | 0.37 | 0.38 | 0.24 | 0.33 | AK (2014) |
| Interquartile range | 0.69 | 0.73 | 0.43 | 0.51 | AK (2014) |
| 10th percentile | 0.00 | 0.00 | 0.38 | 0.20 | AK (2014) |
| 90th percentile | 0.88 | 1.00 | 1.00 | 1.00 | AK (2014) |
| Panel D: Expected Recovery Rates |  |  |  |  |  |

- Split sample into bond and loan dependent firms
- Bond issuers are highly leveraged
- intermediation costs
- Bank dependent firm files more Ch. 7 bankruptcy
- Realized recovery rates
- lower recovery on average in market debt
- cash flow based debt is essential to match large heterogeneity in recovery rates Asset Based Debt

Note: AK (2014) compute summary statistics from Moody's Ultimate Recovery Database AK(2014) refers to Altman and Kalotay (2014)

## Model Captures (Untargeted) Credit Losses

| Description | Market Debt |  | Bank Debt |  | Source |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Model | Data | Model | Data |  |
| Panel A: Leverage |  |  |  |  |  |
| Debt-to-assets | 0.42 | 0.39 | 0.32 | 0.21 | Compustat |
| Panel B: Bankruptcy Probabilities |  |  |  |  |  |
| Chapter 11 Reorganization (\%) | 0.76 | 0.61 | 0.64 | 0.74 | Compustat |
| Chapter 7 Liquidation (\%) | 0.08 | 0.08 | 0.25 | 0.15 | Compustat |
| Fraction of Chapter 11 | 0.90 | 0.88 | 0.72 | 0.83 | Compustat |
| Panel C: Recovery Rates |  |  |  |  |  |
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| Interquartile range | 0.69 | 0.73 | 0.43 | 0.51 | AK (2014) |
| 10th percentile | 0.00 | 0.00 | 0.38 | 0.20 | AK (2014) |
| 90th percentile | 0.88 | 1.00 | 1.00 | 1.00 | AK (2014) |
| Panel D: Expected Recovery Rates |  |  |  |  |  |
| Mean (lowest type score) | 0.12 | n.a. | n.a. | n.a. |  |
| Mean (highest type score) | 0.86 | n.a. | n.a. | n.a. |  |

- Split sample into bond and loan dependent firms
- Bond issuers are highly leveraged
- intermediation costs
- Bank dependent firm files more Ch. 7 bankruptcy
- Realized recovery rates
- lower recovery on average in market debt
- cash flow based debt is essential to match large heterogeneity in recovery rates Asset Based Debt

Type difference of corporate bond expected recovery rates is large (highest to lowest is $74 \%$ pts)

## Other Validations

- Leverage and credit rating (=expected PD) dynamics before and after bankruptcy Ch. 7 Dynamics
- Expected PD and recovery rates at default by credit ratings E[PD] and E[RR]


## How Firm Uses Assessment of Firm's Productivity as Signal?

## Leverage $\uparrow$ and equity $\uparrow$

 $\Downarrow$- Other signal? Bankruptcy and debt structure are less informative Hypothese of signaling
- Signaling is not free: costs of bankruptcy; decreasing returns to scale; and costs of external equity issuance


## How Firm Uses Assessment of Firm's Productivity as Signal?



- Other signal? Bankruptcy and debt structure are less informative Hypotheses of signaling
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- Other signal? Bankruptcy and debt structure are less informative Hypotheses of signaling
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## Debt Pricing

## Corporate bond markets: cross-subsidization Bank Loan Pricing

- Competitive pricing from free entering in both debt markets $\rightarrow$ zero profit
- One-period corporate bond price menu $q_{M}\left(e, s, b, e^{\prime}\right)$ is contingent on size of borrowing (b), equity ( $e, e^{\prime}$ ), and assessment of firm's productivity $\left(s \equiv \operatorname{Pr}\left(z=z_{H}\right)\right.$ )
- where $q_{M}^{-1}$ : gross interest rate, $\mu_{M}$ : intermediation costs, $q$ : price of risk-free debt, PD: Probability of Default, RR: Recovery Rate at default, and Recovery: RR×Exposure At Default

$$
\underbrace{(1-E[\mathrm{PD}]) q_{M}^{-1} b}_{\text {debt repayment (no default) }}+\underbrace{E[\text { Recovery }]}_{\text {debt repayment (default) }}-\underbrace{\left(1+\mu_{M}\right) q^{-1} b}_{\text {funding costs }}=\underbrace{0}_{\text {profit }}
$$

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$$
\begin{align*}
q_{M} & =\frac{(1-E[\mathrm{PD}]) b}{\left(1+\mu_{M}\right) q^{-1} b-E[\text { Recovery }]}  \tag{4}\\
E[\text { Recovery }] & \simeq E[\mathrm{PD}] \times E[\mathrm{RR}] \times \underbrace{q_{M}^{-1} b}_{\text {Exposure At Default }} \tag{5}
\end{align*}
$$

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- where $q_{M}^{-1}$ : gross interest rate, $\mu_{M}$ : intermediation costs, $q$ : price of risk-free debt, PD: Probability of Default, RR: Recovery Rate at default, and Recovery: RR×Exposure At Default

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q_{M} & =\frac{(1-E[\mathrm{PD}]) b}{\left(1+\mu_{M}\right) q^{-1} b-E[\text { Recovery }]}  \tag{4}\\
E[\text { Recovery }] & \simeq E[\mathrm{PD}] \times E[\mathrm{RR}] \times \underbrace{q_{M}^{-1} b}_{\text {Exposure At Default }}  \tag{5}\\
E[\mathrm{PD}] & =(1-s) \times \operatorname{PD}\left(z_{L}, \cdots\right)+s \times \operatorname{PD}\left(z_{H}, \cdots\right) \\
E[\mathrm{RR}] & =(1-s) \times \operatorname{RR}\left(z_{L}, \cdots\right)+s \times \operatorname{RR}\left(z_{H}, \cdots\right)
\end{align*}
$$

## Debt Pricing

## Corporate bond markets: cross-subsidization Bank Loan Pricing

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- One-period corporate bond price menu $q_{M}\left(e, s, b, e^{\prime}\right)$ is contingent on size of borrowing (b), equity ( $e, e^{\prime}$ ), and assessment of firm's productivity $\left(s \equiv \operatorname{Pr}\left(z=z_{H}\right)\right.$ )
- where $q_{M}^{-1}$ : gross interest rate, $\mu_{M}$ : intermediation costs, $q$ : price of risk-free debt, PD: Probability of Default, RR: Recovery Rate at default, and Recovery: RR×Exposure At Default

$$
\begin{aligned}
E[\mathrm{PD}] & \neq \mathrm{PD}(z) \\
E[\mathrm{RR}] & \neq \operatorname{RR}(z)
\end{aligned}
$$

where $z \in\left\{z_{L}, z_{H}\right\}$ if $0<s<1, \operatorname{PD}\left(z_{H}\right) \neq \operatorname{PD}\left(z_{L}\right)$, and $\operatorname{RR}\left(z_{H}\right) \neq \operatorname{RR}\left(z_{L}\right)$

## Debt Pricing (Cont'd)

## Bank loan markets: benefits of monitoring and costs of intermediation $\mu_{B}$

- One-period bank loan price menu $q_{B}\left(e, z, s, b, \phi, e^{\prime}\right)$ is contingent on productivity $(z)$

$$
\begin{align*}
q_{B}(z, \cdots) & =\frac{(1-\operatorname{PD}(z, \cdots)) b}{\left(1+\mu_{B}\right) q^{-1} b-\operatorname{Recovery}(z, \cdots)}  \tag{4}\\
\text { Recovery }(z, \cdots) & \simeq \operatorname{PD}(z, \cdots) \times \underbrace{s_{c 7}(e+b)}_{\text {liquidation value }} \tag{5}
\end{align*}
$$

- Debt types trade-offs: (i) monitoring; (ii) intermediation costs; (iii) recovery at default
- Who borrows from bank lenders? High productivity firm with low assessment of firm's productivity


## Debt Structure Choice




- Type score $=$ assessment of firm's productivity $\left(s \equiv \operatorname{Pr}\left(z=z_{H}\right)\right)$
- Corporate bonds are mostly cheaper for safer firms because intermediation costs are smaller
- When firm borrowers from banks?
- small-sized firm because corporate bond recovery at default is low (interest rates are high)
- low type score firm because it pays info rents
- preference shocks


## Leverage and Equity Send Informative Signals s'

- Type score $\left(s=\operatorname{Pr}\left(z_{H}\right)\right)$ updating follows Bayes rule
- $s^{\prime}$ is mapping from public info $\left\{e, s, b, \phi, e^{\prime}\right.$ and $\left.\Delta\right\}$
- Simulated panel regressions to study determinants of type score $s^{\prime}$ :

$$
\begin{aligned}
s_{i, t} & =\alpha_{i}+\beta_{0}+\beta_{1} \text { Leverage }_{i, t-1}+\beta_{2} \ln \left(\text { Equity }_{i, t-1}\right)+\beta_{3} \text { Bankruptcy }_{i, t-1} \\
& +\beta_{4} \text { Market funding ratio }_{i, t-1}+\beta_{5} \ln \left(\text { Firm age }_{i, t-1}\right)+\beta_{6} s_{i, t-1}+\varepsilon_{i, t}
\end{aligned}
$$

- Type score updating is mostly explained by leverage and equity: Regresion
$-+1 \sigma$ leverage raises belief by $20 \%$ pts $(=\underbrace{0.81} \times 0.25)$
$-+1 \sigma$ equity raises belief by $11 \%$ pts $(=\underbrace{0.19} \times 0.60)$
- typical reputation proxies are not good (i.e., bankruptcy, market funding ratio, firm age)


## Regressions

|  | Dependent variable: Type score $\mathrm{s}_{t}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) | (4) |
| Leverage $_{t-1}$ | $\begin{aligned} & \hline 0.739 * * * \\ & (493.43) \end{aligned}$ |  | $\begin{aligned} & \hline 0.943 * * * \\ & (881.76) \end{aligned}$ | $\begin{aligned} & 0.806 * * * \\ & (789.83) \end{aligned}$ |
| $\ln$ (Internal finance ${ }_{t-l}$ ) |  | $\begin{aligned} & 0.212 * * * \\ & (325.37) \end{aligned}$ | $\begin{aligned} & 0.306^{* *} * \\ & (716.11) \end{aligned}$ | $\begin{aligned} & 0.191 * * * \\ & (386.23) \end{aligned}$ |
| Chapter 11 bankruptcy $_{\text {t-1 }}$ |  |  | $\begin{aligned} & 0.0283^{* * *} \\ & (13.07) \end{aligned}$ | $\begin{aligned} & 0.0314^{* * *} \\ & (16.44) \end{aligned}$ |
| Market funding ratio ${ }_{\text {t-1 }}$ |  |  | $\begin{aligned} & 0.00853^{* * *} \\ & (15.95) \end{aligned}$ | $\begin{aligned} & 0.0000488 \\ & (0.10) \end{aligned}$ |
| $\ln \left(\right.$ Firm age ${ }_{t-1}$ ) |  |  | $\begin{aligned} & -0.00424^{* * *} \\ & (-15.38) \end{aligned}$ | $\begin{aligned} & -0.0000297 \\ & (-0.12) \end{aligned}$ |
| Type score $\mathrm{s}_{t-1}$ |  |  |  | $\begin{aligned} & 0.346 * * * \\ & (360.18) \end{aligned}$ |
| Number of observations | 475568 | 475568 | 475568 | 475568 |
| $\mathrm{R}^{2}$ | 0.339 | 0.182 | 0.696 | 0.762 |
| Fixed effects | No | No | Yes | Yes |

## Good (Bad) Type Score Reduces (Increases) Interest Rate



Firms with High Type Issue More Corporate Bonds





# Signaling Theory in Corporate Finance 

Signaling Alleviates Asym Info

## Possibility (This Paper):

- Leverage (Ross 77; Hennessy, Livdan and Miranda 10) $\checkmark$
- Internal finance (Leland and Pyle 76) $\checkmark$
- Bankruptcy filing (Diamond 89, 91) X
- Debt structure (Houston and James 96) X
- Firm age (Datta, Iskandar-Datta, and Patel 99) $x$


## Asset Based Debt

## Alternative Benchmark

- Corporate bond recovery: cash flow based $\rightarrow$ asset based

|  | Data | Benchmark <br> (i) | Counterfactual <br> (ii) | Alternative benchmark <br> (iii) | Counterfactual <br> (iv) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Panel A: Techonology |  |  |  |  |  |
| Monitoring by bondholders |  |  | $\checkmark$ |  | $\checkmark$ |
| Bond flexibility under Ch .11 |  |  |  | $\checkmark$ | $\checkmark$ |
| Panel B: Capital Structure and Welfare |  |  |  |  |  |
| Debt | n.a. | 20.80 | 22.74 | 18.04 | 18.36 |
| Debt (zL) | n.a. | 3.22 | 3.22 | 3.66 | 3.66 |
| Debt (zH) | n.a. | 17.58 | 19.52 | 14.37 | 14.69 |
| Equity | n.a. | 24.24 | 21.86 | 24.36 | 24.01 |
| Equity (zL) | n.a. | 9.52 | 8.57 | 8.98 | 8.85 |
| Equity (zH) | n.a. | 14.72 | 13.28 | 15.38 | 15.16 |
| Aggregate bank debt ratio | 0.31 | 0.21 | 0.15 | 0.24 | 0.22 |
| Consumption | n.a. | 1.380 | 1.398 | 1.281 | 1.283 |
| Change in \% compared to full info | n.a. | n.a. | 1.35 | n.a. | 0.14 |
| Output | n.a. | 12.81 | 12.77 | 12.29 | 12.29 |
| Capital | n.a. | 45.03 | 44.60 | 42.40 | 42.37 |
| Change in \% compared to full info | n.a. | n.a. | -0.97 | n.a. | -0.08 |
| Capital (zL) | n.a. | 12.74 | 11.80 | 12.65 | 12.51 |
| Capital ( zH ) | n.a. | 32.30 | 32.80 | 29.75 | 29.86 |
| TFP | n.a. | 1.079 | 1.082 | 1.076 | 1.077 |
| Change in \% compared to full info | n.a. | n.a. | 0.29 | n.a. | 0.05 |
| Panel C: Bankruptcy |  |  |  |  |  |
| Bankruptcy prob. (Ch. 11) (\%) | 0.72 | 0.72 | 0.85 | 0.72 | 0.76 |
| Bankruptcy prob. (Ch. 7) (\%) | 0.14 | 0.14 | 0.12 | 0.19 | 0.18 |
| Panel D: Market Debt Recovery Rates |  |  |  |  |  |
| Mean | 0.45 | 0.32 | 0.36 | 0.62 | 0.61 |
| Standard deviation | 0.38 | 0.37 | 0.34 | 0.20 | 0.20 |
| Interquartile range | 0.73 | 0.69 | 0.66 | 0.27 | 0.24 |
| 10th percentile | 0.00 | 0.00 | 0.00 | 0.41 | 0.41 |
| 90 th percentile | 1.00 | 0.88 | 0.81 | 1.00 | 0.98 |

## (Untarget) Model Dynamics Around Ch. 11 Are Close to Data

- Credit ratings is mapping of $E[P D]$ to 6 buckets (e.g., top 4\% of safest bonds are categorized as "AAA/AA")

- Mean reversions in leverage and credit rating
- which arise from productivity process and costly equity issuance


## Dynamics

## Model



Leverage


## Data



- Model is also consistent with dynamics around Ch. 7


## $E[P D]$ and $E[R R]$ Conditional on Credit Rating

In real-world data:

- $\mathrm{E}[\mathrm{PD}]=$ Historical Bankruptcy Rate
- E[Recovery Rate]=Recovery Rating
- recovery ratings are only available for speculative grades

|  | S\&P Credit Rating |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Investment Grade |  | Speculative Grade |  |  |  |
|  | AAA/AA | A | BBB | BB | B | CCC/C |
| Panel A: Share (\%) |  |  |  |  |  |  |
| Model | 4.00 | 15.00 | 24.00 | 27.00 | 27.00 | 3.00 |
| Data | 3.97 | 14.32 | 23.75 | 27.26 | 27.27 | 3.43 |
| Panel B: Bankruptcy and Default of Market Debt |  |  |  |  |  |  |
| Expected bankruptcy rates (\%) |  |  |  |  |  |  |
| Historical annual bankruptcy rates (\%) |  |  |  |  |  |  |
| Data 1 year | 0.00 | 0.00 | 0.07 | 0.12 | 0.57 | 14.13 |
| 3 years | 0.05 | 0.03 | 0.13 | 0.53 | 1.32 | 7.35 |
| Panel C: Expected Recovery Rates at Default of Market Debt |  |  |  |  |  |  |
| Model Mean | 1.00 | 0.98 | 0.85 | 0.39 | 0.25 | 0.26 |
| Std. Dev. | 0.01 | 0.03 | 0.19 | 0.36 | 0.29 | 0.23 |
| Data Mean | n.a. | n.a. | n.a. | 0.43 | 0.38 | 0.38 |
| Std. Dev. | n.a. | n.a. | n.a. | 0.26 | 0.30 | 0.32 |
| Number of observations | n.a. | n.a. | n.a. | 1150 | 728 | 248 |

- Distributions of PD and Recovery Rates in model are consistent with data


## Asym Info (Benchmark) Model is Closer to Data

- Moody's LGD assessment is $E[1$ - Recovery Rates]


Note: Data sample is from 2008 to 2010

- Realized recovery rates $\neq$ expected recovery rates


## Misallocation

TFP $=$ Aggregate Capital $^{\alpha_{k}} /$ Aggregate Output

|  | Benchmark | Counterfactual |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | (i) | Perfect <br> Monitoring | Partial Monitoring |  |
|  |  | (ii) | (iii) | (iv) |
| Panel A: Techonology |  |  |  |  |
| Monitoring on PD |  | $\checkmark$ | $\checkmark$ |  |
| Monitoring on recovery at default |  | $\checkmark$ |  | $\checkmark$ |
| Panel B: Capital Structure and Welfare |  |  |  |  |
| Debt | 20.80 | 22.74 | 22.38 | 21.13 |
| Debt (zL) | 3.22 | 3.22 | 3.22 | 3.19 |
| Debt (zH) | 17.58 | 19.52 | 19.16 | 17.95 |
| Equity | 24.24 | 21.86 | 22.36 | 23.66 |
| Equity (zL) | 9.52 | 8.57 | 8.78 | 9.32 |
| Equity ( 2 H ) | 14.72 | 13.28 | 13.59 | 14.34 |
| Aggregate bank debt ratio | 0.21 | 0.15 | 0.16 | 0.19 |
| Consumption | 1.380 | 1.398 | 1.404 | 1.389 |
| Change in \% compared to benchmark | n.a. | 1.35 | 1.80 | 0.65 |
| Output | 12.81 | 12.77 | 12.79 | 12.78 |
| Capital | 45.03 | 44.60 | 44.74 | 44.79 |
| Change in \% compared to benchmark | n.a. | -0.97 | -0.64 | -0.54 |
| Capital (zL) | 12.74 | 11.80 | 12.00 | 12.50 |
| Capital (zH) | 32.30 | 32.80 | 32.74 | 32.29 |
| Panel C: Allocation Efficiency |  |  |  |  |
| TFP | 1.079 | 1.082 | 1.081 | 1.079 |
| Change in \% compared to benchmark | n.a. | 0.29 | 0.24 | 0.05 |
| Avrg. output-weighted productivity | 1.179 | 1.185 | 1.184 | 1.181 |
| Avrg. productivity | 1.037 | 1.037 | 1.037 | 1.037 |
| Cov (productivity,output weights) | 0.143 | 0.149 | 0.148 | 0.144 |
| Variance of $\mathrm{mpk} \times 100$ | 2.87 | 2.52 | 2.58 | 2.79 |
| Variance of productivity | 7.28 | 7.28 | 7.28 | 7.28 |
| Variance of log capital | 4.76 | 5.37 | 5.23 | 4.83 |
| $\operatorname{Cov}$ (z, capital) | -9.18 | -10.13 | -9.93 | -9.32 |
| Panel D: Bankruptcy |  |  |  |  |
| Bankruptey prob. (Ch. 11) (\%) | 0.72 | 0.85 | 0.82 | 0.73 |
| Bankruptcy prob. (Ch. 7) (\%) | 0.14 | 0.12 | 0.13 | 0.14 |

## Interaction of Financial Markets

|  | No bank debt |  | Zero external equity financing costs |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Alternative benchmark | Counterfactual | Alternative benchmark | Counterfactual |
| Panel A: Techonology |  |  |  |  |
| Monitoring by bondholders |  | $\checkmark$ |  | $\checkmark$ |
| Panel B: Capital Structure and Welfare |  |  |  |  |
| Debt | 21.77 | 23.65 | 19.48 | 20.80 |
| Equity | 24.77 | 21.69 | 28.57 | 26.73 |
| Consumption | 1.476 | 1.482 | 1.857 | 1.843 |
| Change in \% to full info | n.a. | 0.42 | n.a. | -0.72 |
| Output | 13.11 | 12.94 | 13.32 | 13.25 |
| Capital | 46.54 | 45.34 | 48.05 | 47.53 |
| Change in \% to full info | n.a. | -2.58 | n.a. | -1.09 |
| TFP | 1.080 | 1.084 | 1.075 | 1.077 |
| Change in \% to full info | n.a. | 0.36 | n.a. | 0.18 |

- Substitution between corporate bonds and bank loans amplifies the change in consumption
- improvement is less than $1 / 3$ in model w/o bank debt
- More info might be inefficient in misspecified model w/o costly equity issuance


## Simpler Model Delivers Different Quantitative Results

No Bank Debt and Zero Equity Costs


Alternative models

- How much economy is willing to pay for intermediation costs (e.g., monitoring costs)?
- $\uparrow$ intermediation costs $\rightarrow \downarrow$ consumption
- break even intermediation costs +7 bps


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[^0]:    Panel D: Expected Recovery Rates

